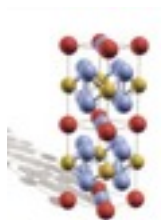


# Complex correlated materials from the Dynamical Mean Field Perspective.

RUTGERS  
THE STATE UNIVERSITY  
OF NEW JERSEY

Kristjan Haule



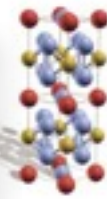
Support:



ACS  
Chemistry for Life™

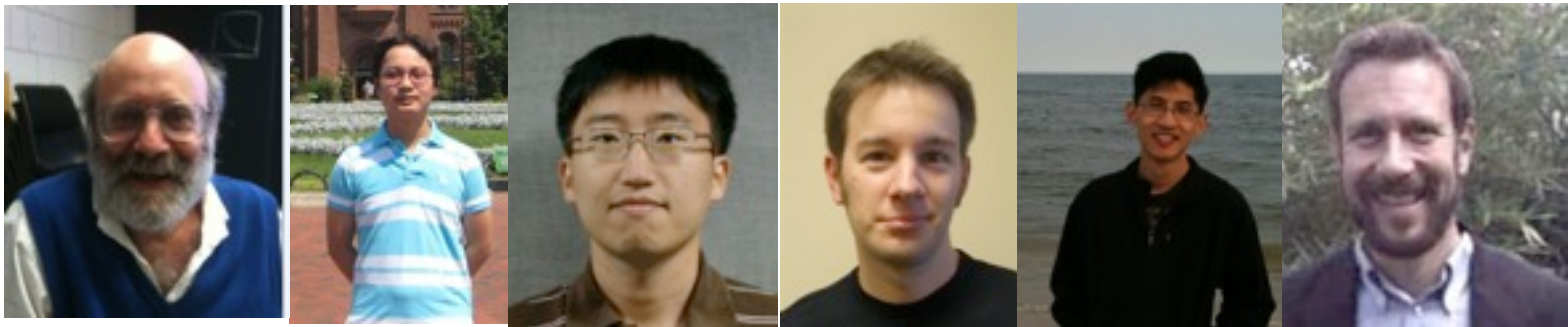
Tallahassee, 2012

# Thanks To

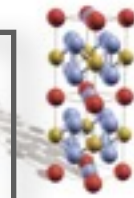


Collaborators:

Gabriel Kotliar, Zhiping Yin, Hyowon Park,  
Chuck-Hou Yee, Jan Tomczak, Ronald Cohen



# Motivation



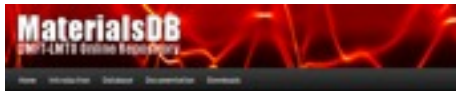
*Motivation: Testing our ability to understand the electronic structure of complex correlated materials.*

The driving force:  
Experimental probes  
Optics, APRES, STM,  
...

interplay

Computational tool  
is (DFT, DMFT)

*Developing DMFT into an electronic structure tool, understanding qualitatively universal and system specific aspects.*



[http:// hauleweb.rutgers.edu](http://hauleweb.rutgers.edu)

Compound	Results	Input Files	Files
CaFeO3	000 00000 000 00 00 000000 000000 00 00 0000 0000		
CaFeO3	000 00000 000 00 00 000000 000000 00 00 0000 0000		
CaFeO3_001	000 00000 000 00 00 000000 000000 00 00 0000 0000		
CaFeO3_002	000 00000 000 00 00 000000 000000 00 00 0000 0000		
CaFeO3_003	000 00000 000 00 00 000000 000000 00 00 0000 0000		
CaFeO3_004	000 00000 000 00 00 000000 000000 00 00 0000 0000		
CaFeO3_005	000 00000 000 00 00 000000 000000 00 00 0000 0000		
CaFeO3_006	000 00000 000 00 00 000000 000000 00 00 0000 0000		
CaFeO3_007	000 00000 000 00 00 000000 000000 00 00 0000 0000		
CaFeO3_008	000 00000 000 00 00 000000 000000 00 00 0000 0000		
CaFeO3_009	000 00000 000 00 00 000000 000000 00 00 0000 0000		
CaFeO3_010	000 00000 000 00 00 000000 000000 00 00 0000 0000		
CaFeO3_011	000 00000 000 00 00 000000 000000 00 00 0000 0000		
CaFeO3_012	000 00000 000 00 00 000000 000000 00 00 0000 0000		
CaFeO3_013	000 00000 000 00 00 000000 000000 00 00 0000 0000		
CaFeO3_014	000 00000 000 00 00 000000 000000 00 00 0000 0000		
CaFeO3_015	000 00000 000 00 00 000000 000000 00 00 0000 0000		

Wien2K+DMFT

multiorbital CTQMC, full potential basis, charge self-consistent.

Thermoelectricity in FeSi  
as Hunds semiconductors

J.Tomczak, KH, G. Kotliar, PNAS (2012)

MIT in FeO

K. Ohta, R. Cohen, KH, PRL (2012)

Computational tools allow to  
identify system specific  
fingerprints which give us  
confidence in our  
understanding of  
correlated electron materials

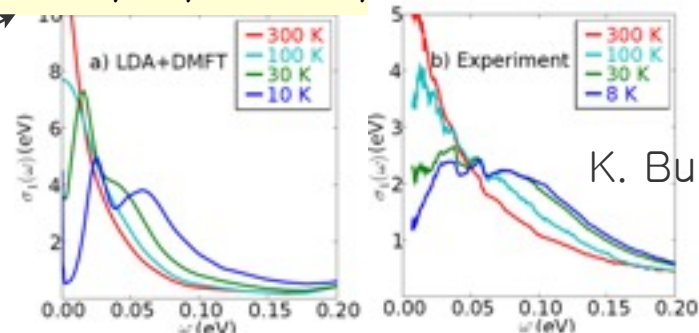
Magnetism and Charge Dynamics  
in Iron Pnictides.

Z. P. Yin, KH, G. Kotliar, Nature Physics (2011)

Z. P. Yin, KH, G. Kotliar, Nature Materials (2011)

Protracted screening and multiple  
hybridization Gaps in Ce115's.

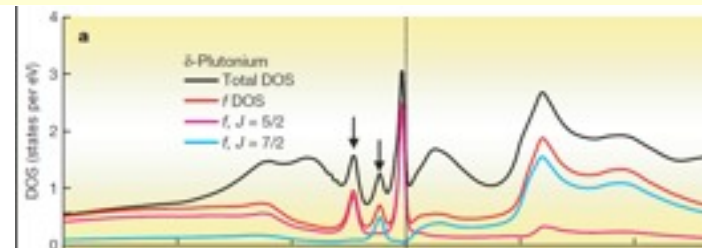
J.H.Shim, KH, G.Kotliar, Science 318. 1615 (2007)



K. Burch et.al.

Quasiparticle multiplets in Plutonium  
and its Compounds.

J.H.Shim, KH, G.Kotliar, Nature 446, 513 (2007).

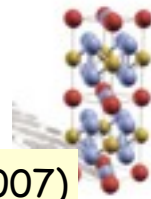


Strength of correlations in e and h doped  
cuprates.

C Weber, KH, G. Kotliar, Nature Physics 10, 1038 (2010)

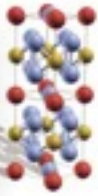
Hidden Order in URu2Si2. Kondo effect  
and hexadecapole order.

KH, G. Kotliar, Nature Physics 5, 796 - 799 (2009).

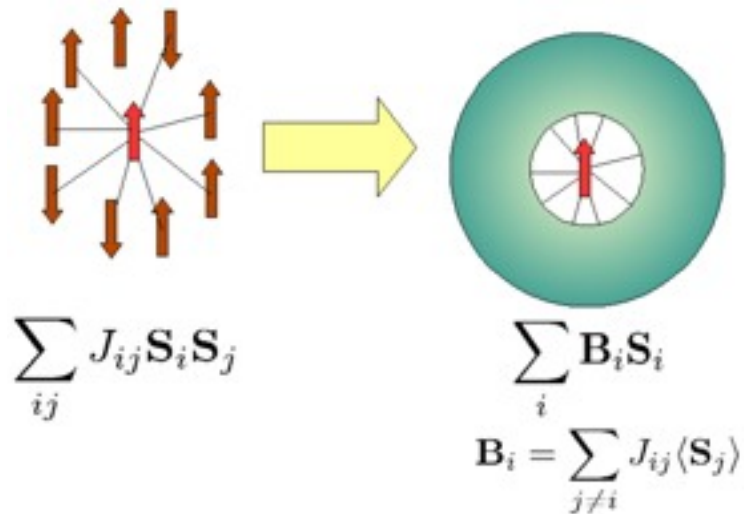




# Bright Future: Dynamical Mean Field



Weiss mean field theory for spin systems  
Exact in the limit of large  $z$



Classical problem of spin in  
a magnetic field

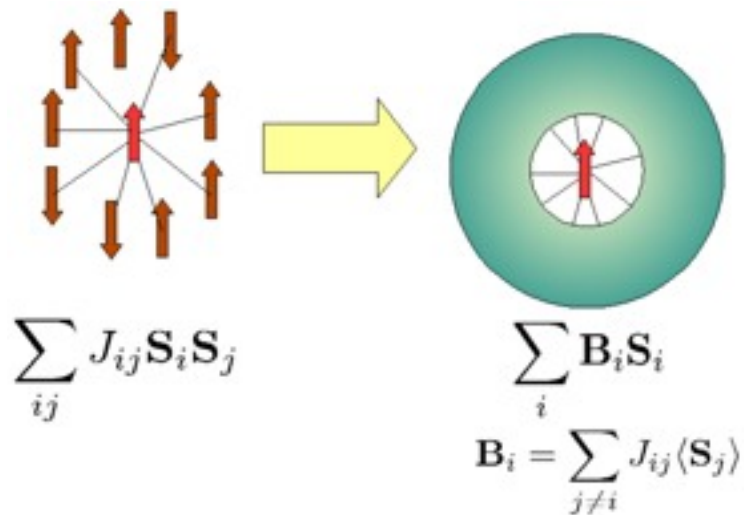
# Bright Future: Dynamical Mean Field



(G. Kotliar S. Savrasov K.H., V. Oudovenko O. Parcollet and C. Marianetti, RMP 2006).

Weiss mean field theory for spin systems

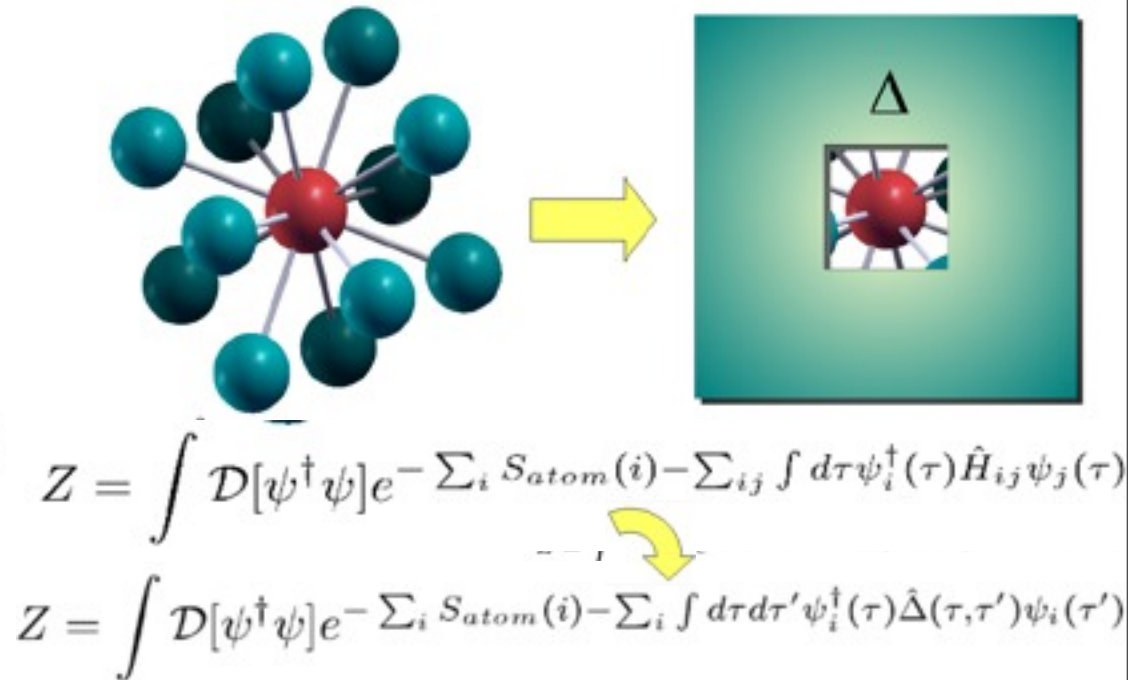
Exact in the limit of large  $z$



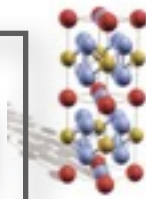
Classical problem of spin in  
a magnetic field

Dynamical mean field theory (DMFT)

for the electronic problem  
exact in the limit of large  $z$



# Bright Future: Dynamical Mean Field



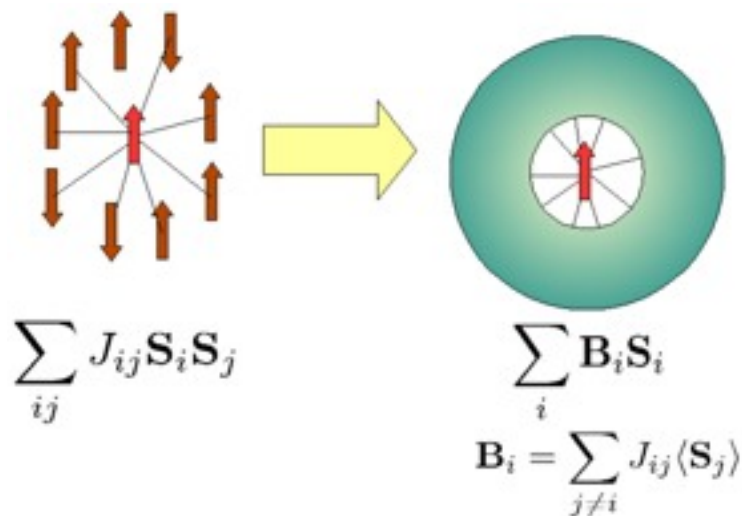
(G. Kotliar S. Savrasov K.H., V. Oudovenko O. Parcollet and C. Marianetti, RMP 2006).

Weiss mean field theory for spin systems

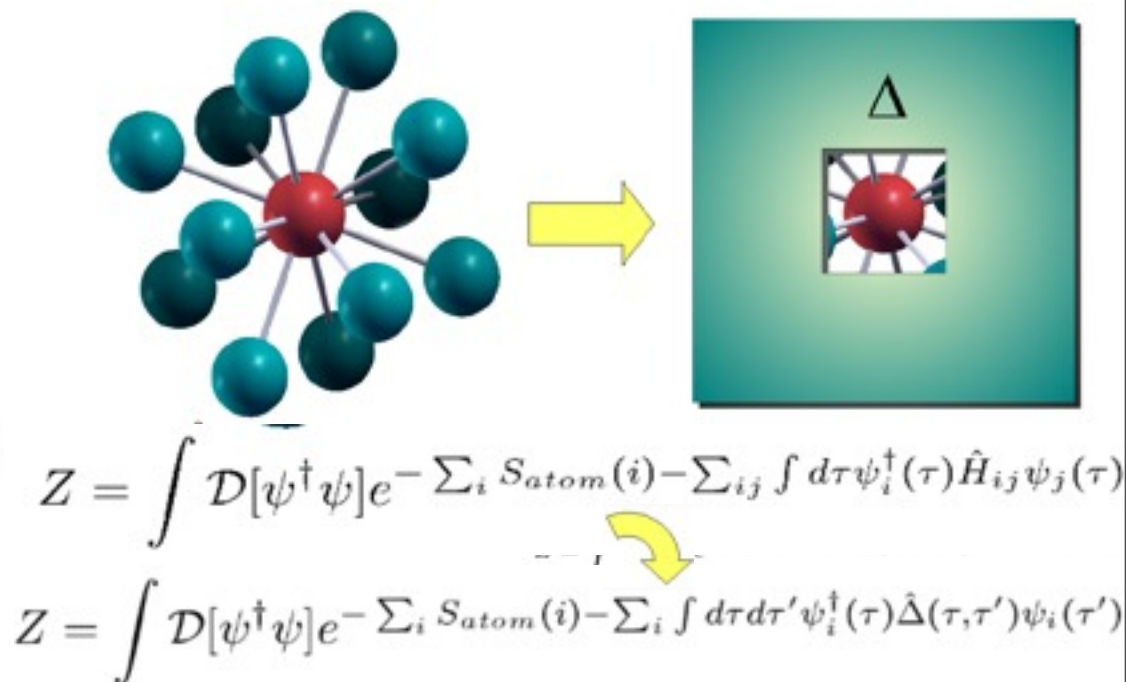
Dynamical mean field theory (DMFT)

Exact in the limit of large  $z$

for the electronic problem  
exact in the limit of large  $z$

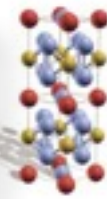


Classical problem of spin in  
a magnetic field



Problem of a quantum impurity    Space fluctuations are ignored,  
(atom in a fermionic band)    time fluctuations are treated exactly

# Bright Future: Dynamical Mean Field



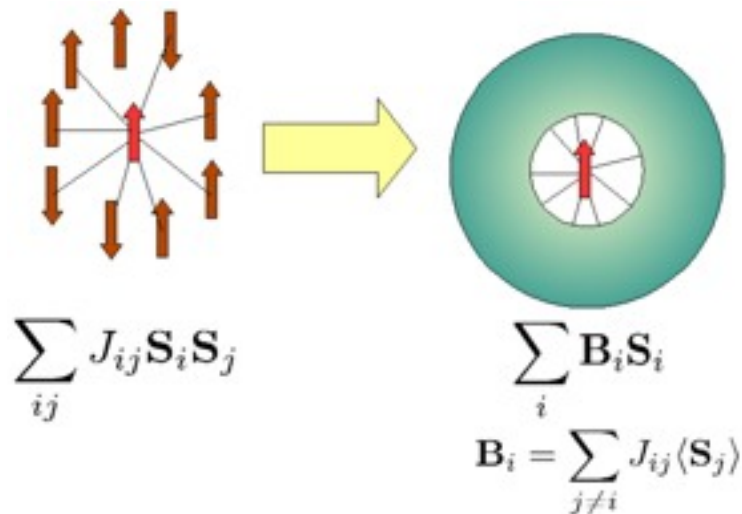
(G. Kotliar S. Savrasov K.H., V. Oudovenko O. Parcollet and C. Marianetti, RMP 2006).

Weiss mean field theory for spin systems

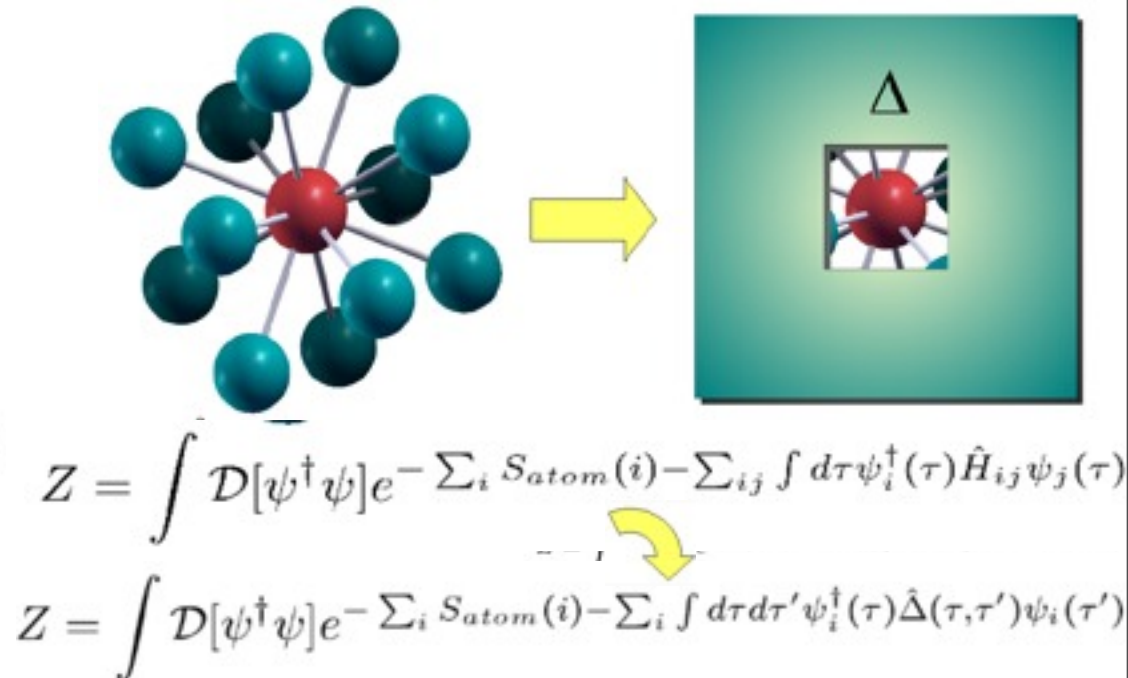
Dynamical mean field theory (DMFT)

Exact in the limit of large  $z$

for the electronic problem  
exact in the limit of large  $z$



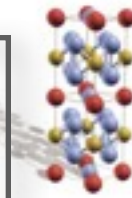
Classical problem of spin in  
a magnetic field



Improvements:

- Impurity solvers (Numerically exact continuous time QMC method)
- Charge SC implementation, avoids construction of low energy models

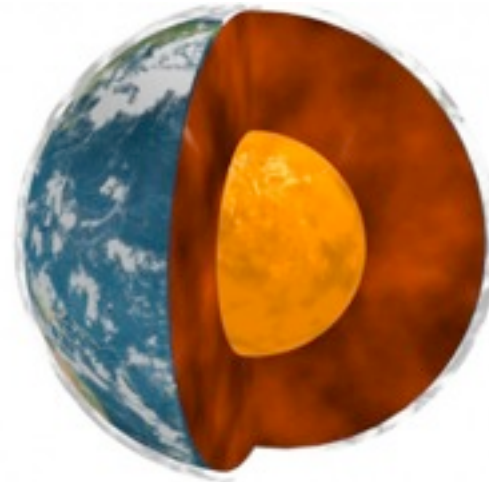
# IRON OXIDE



Very common in life:

$\text{Fe}^{2+}$  pigment, in cosmetics & tattoo inks

$\text{Fe}^{3+}$  corrosion

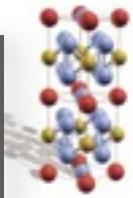


Wüstite,  $\text{FeO}$ , is important constituent of the Earth's lower mantle and possibly in the core

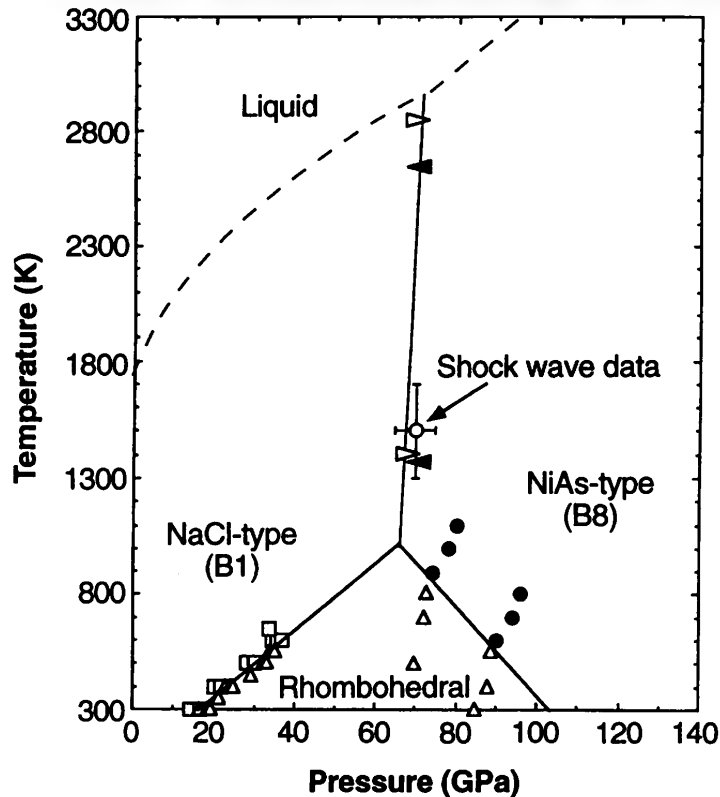
Physical properties under high pressure still poorly understood.  
Important for geophysical science : origin of the Earth's magnetic field

Is  $\text{FeO}$  insulating/conducting in the lower mantle under high pressure and high  $T$ ?  
How does B-field (created in the lower mantle) propagate to the surface?  
What is magnetomechanical coupling between the Earth's mantle and core?

# FeO phase diagram

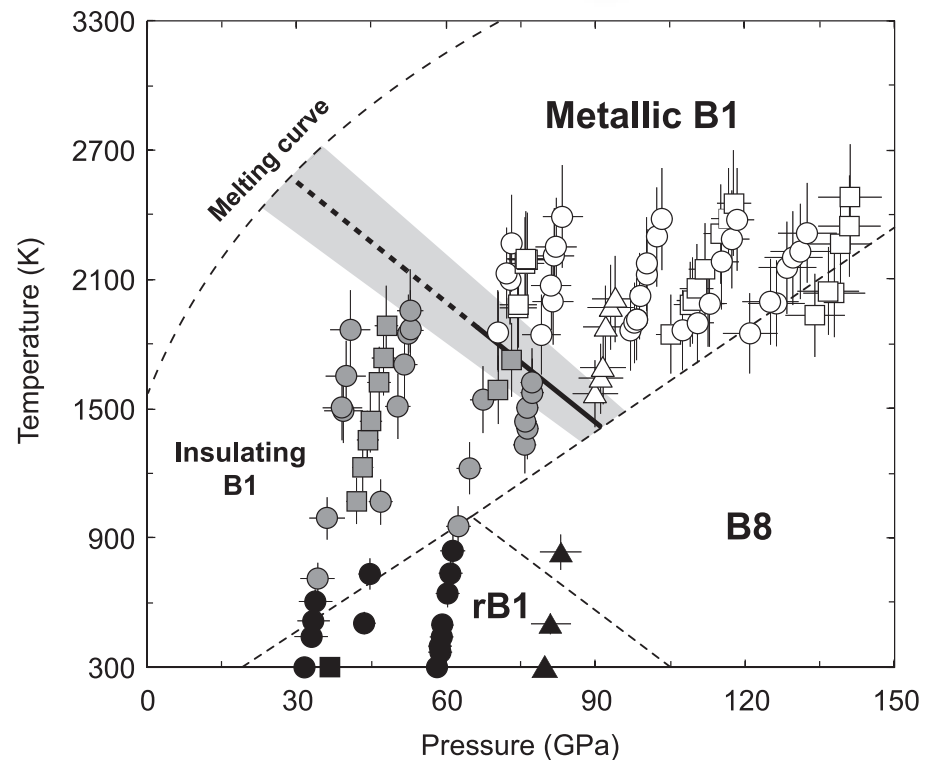


Prior understanding of the PD



Yingwei Fei and Ho-kwang Mao  
Science **266**, 1678 (1994).

New Phase Diagram 2011



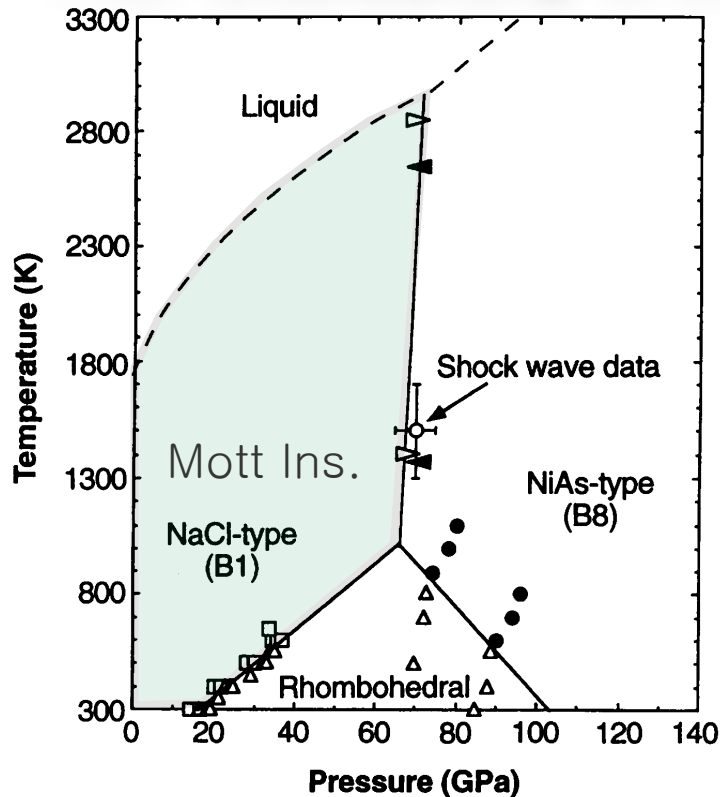
K. Ohta, R.E. Cohen, K. Hirose, K. Haule,  
K. Shimizu, Y. Ohishi, PRL 2012



# FeO phase diagram

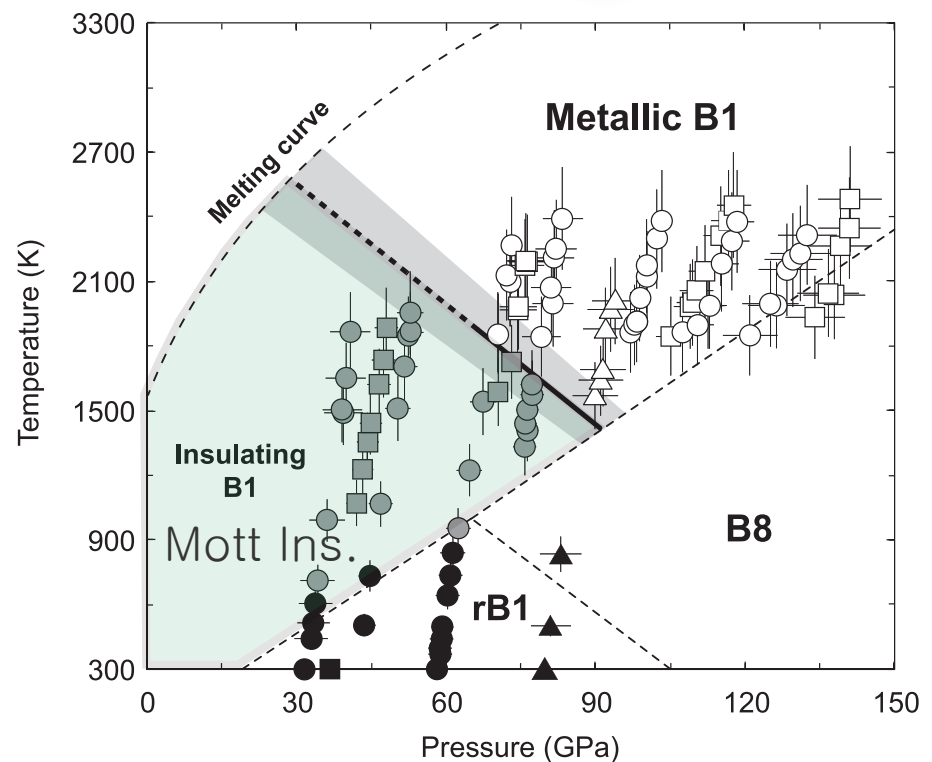


Prior understanding of the PD



Yingwei Fei and Ho-kwang Mao  
Science **266**, 1678 (1994).

New Phase Diagram 2011

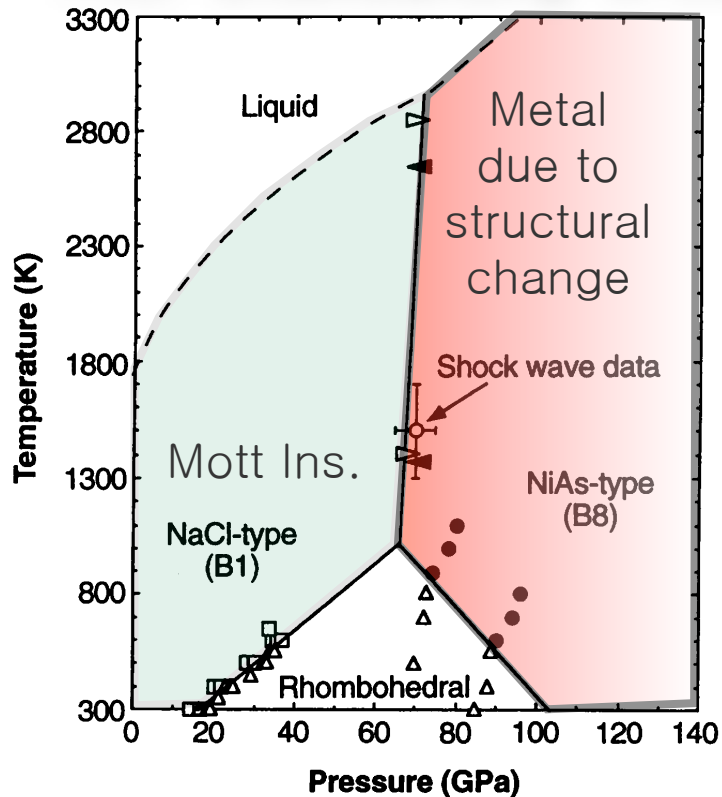


K. Ohta, R.E. Cohen, K. Hirose, K. Haule,  
K. Shimizu, Y. Ohishi, PRL 2012

# FeO phase diagram

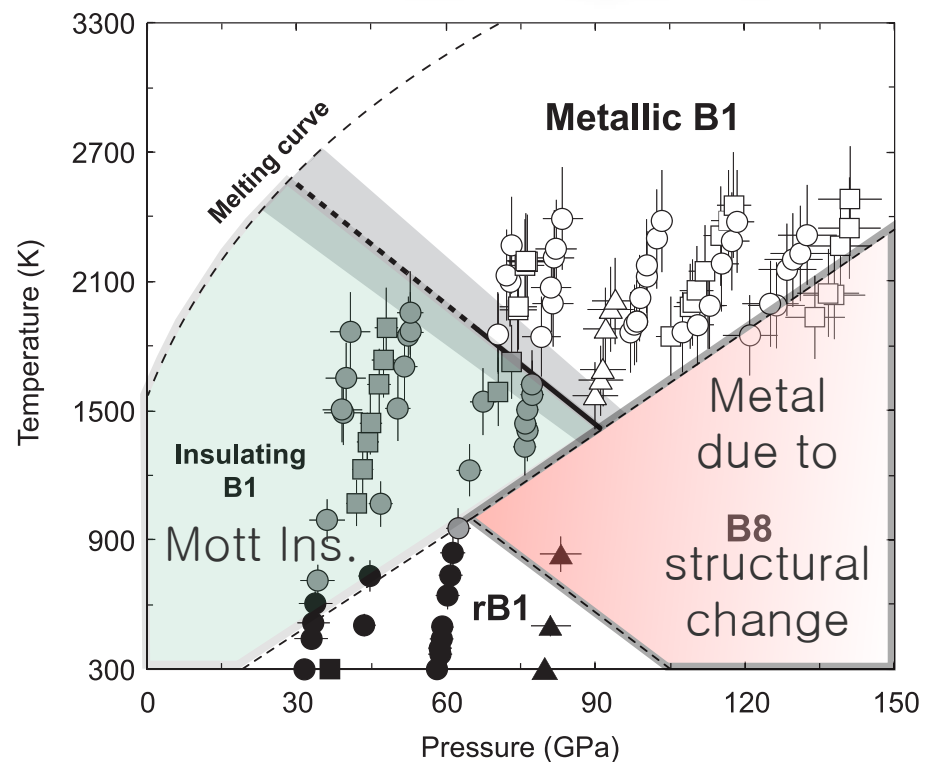


Prior understanding of the PD



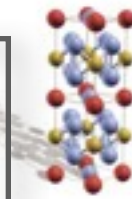
Yingwei Fei and Ho-kwang Mao  
Science **266**, 1678 (1994).

New Phase Diagram 2011

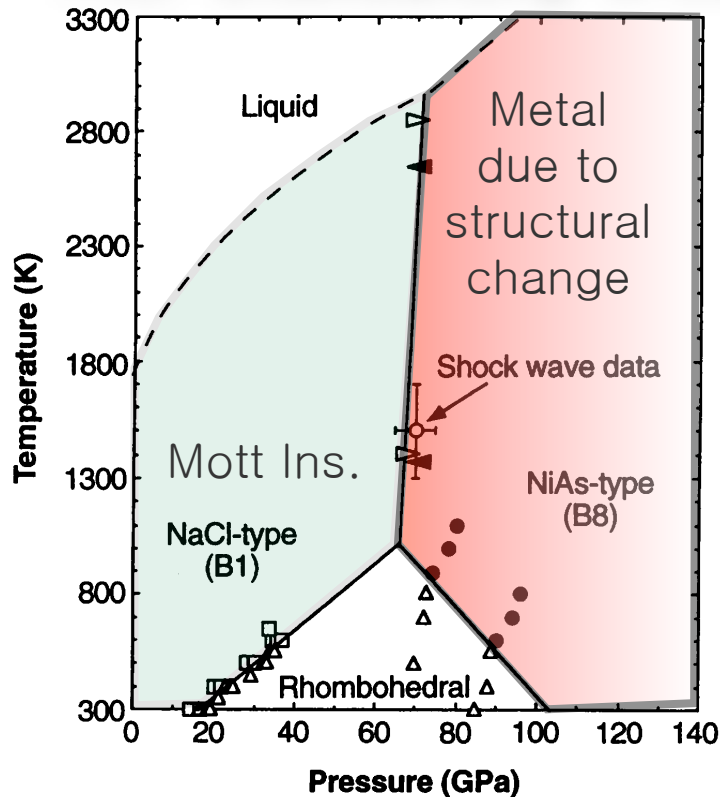


K. Ohta, R.E. Cohen, K. Hirose, K. Haule,  
K. Shimizu, Y. Ohishi, PRL 2012

# FeO phase diagram

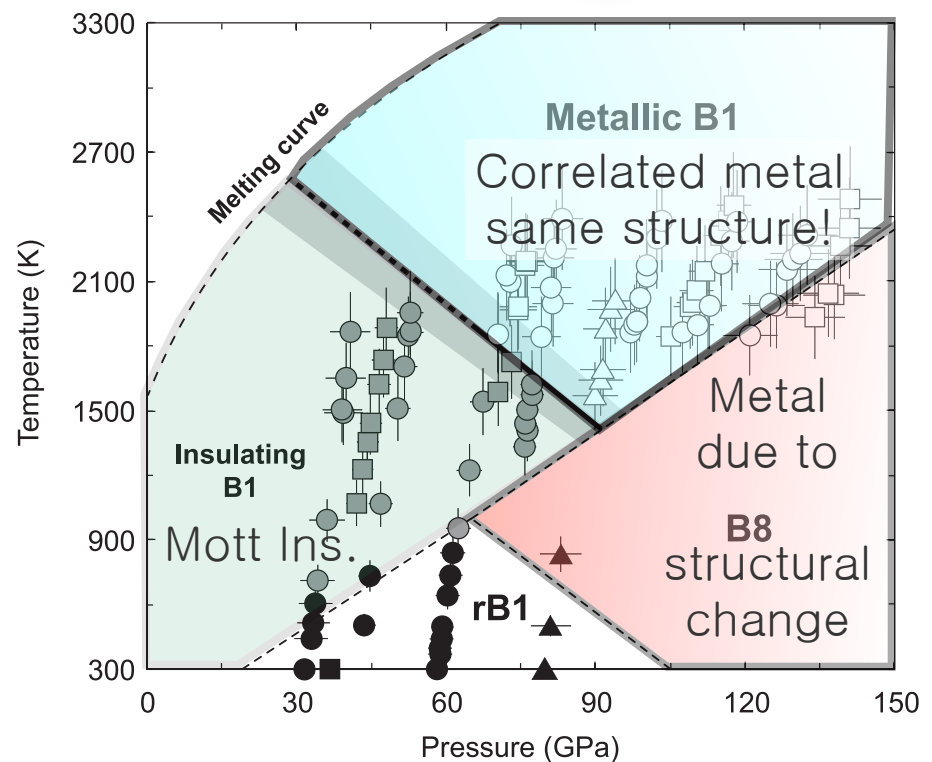


Prior understanding of the PD



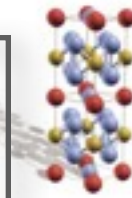
Yingwei Fei and Ho-kwang Mao  
Science **266**, 1678 (1994).

New Phase Diagram 2011

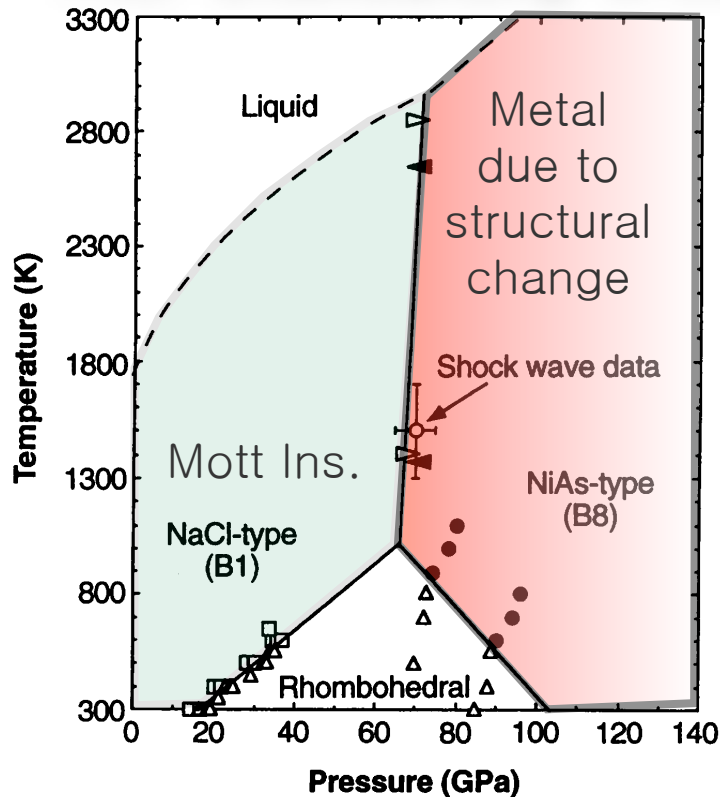


K. Ohta, R.E. Cohen, K. Hirose, K. Haule,  
K. Shimizu, Y. Ohishi, PRL 2012

# FeO phase diagram

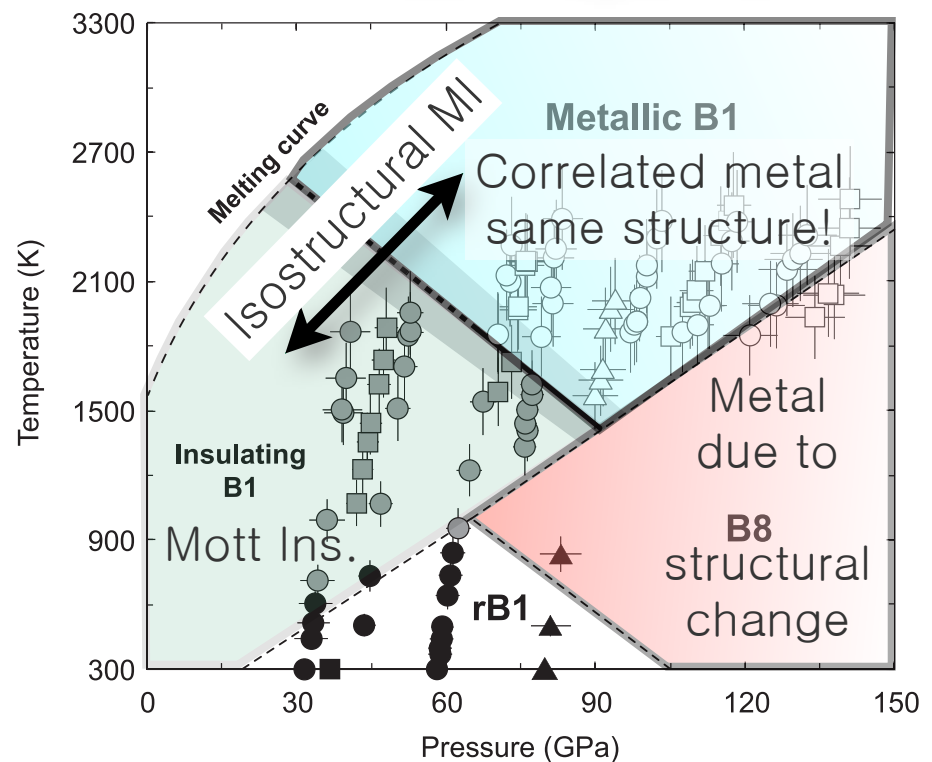


Prior understanding of the PD



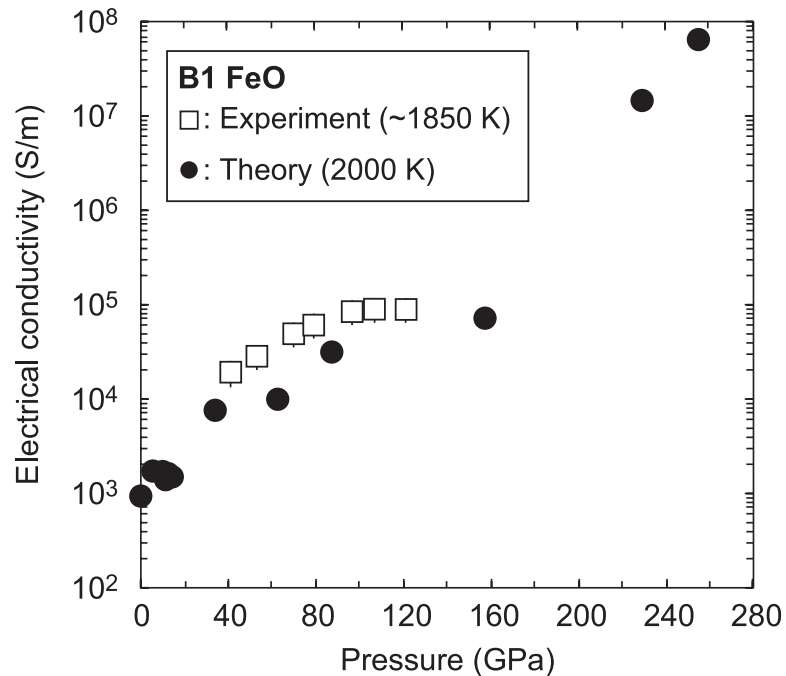
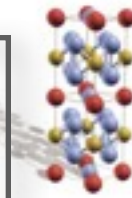
Yingwei Fei and Ho-kwang Mao  
Science **266**, 1678 (1994).

New Phase Diagram 2011



K. Ohta, R.E. Cohen, K. Hirose, K. Haule,  
K. Shimizu, Y. Ohishi, PRL 2012

# FeO conductivity



Mott state in FeO at  
high temperature  
unstable

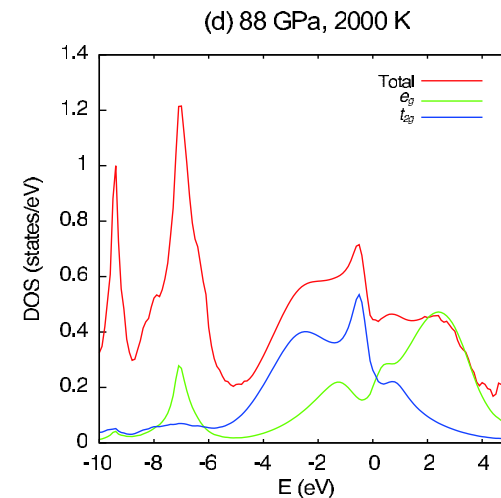
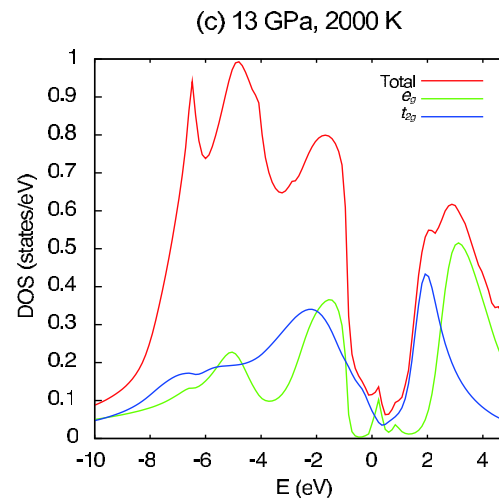
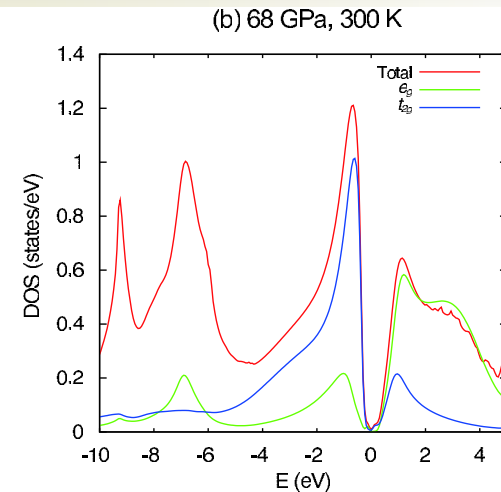
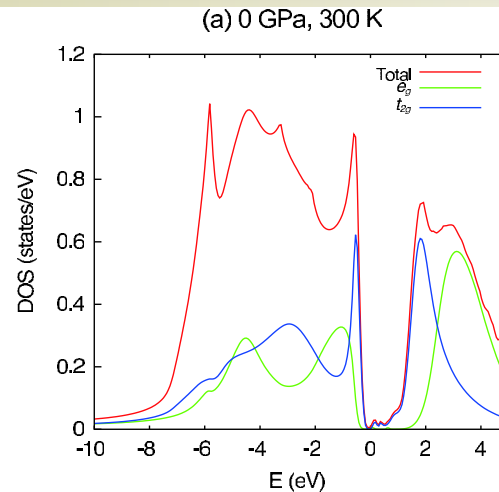
K. Ohta, R.E. Cohen, K. Hirose, K. Haule,  
K. Shimizu, Y. Ohishi, PRL 2012

*Conductivity increases by  
orders of magnitude*  
No sharp phase transition  
more like crossover

# FeO spectra



Low-T insulator  
stable under pressure:

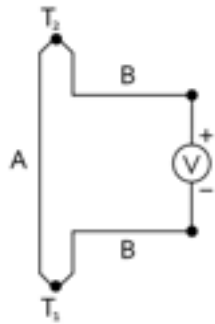
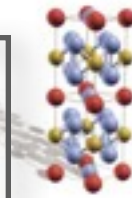


bad insulator  
in high-spin state

bad metal  
in low-spin state



# Thermoelectricity



Temperature gradient creates electric field

Existing materials only small efficiency

Figure of merit of unity is “good”,  
“best” is 2–3

$$ZT = \frac{S^2 \sigma T}{\kappa + \kappa_{\text{phonon}}}$$

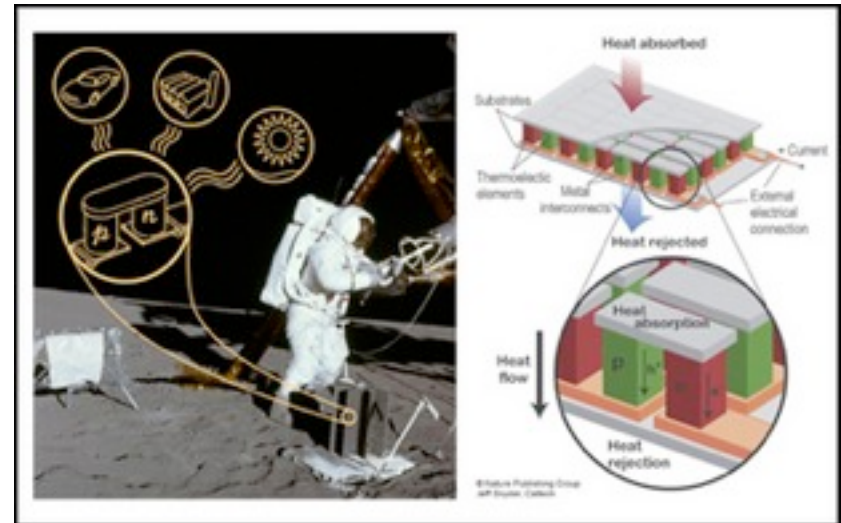
$L = \kappa / (\sigma T)$  Lorenz number

$$L \approx \frac{\pi^2}{3} (k_B/e)^2 = 2.44 \times 10^{-8} V^2/K^2$$

$$S = \sqrt{ZT \times L} \approx 156 \mu V/K \sqrt{ZT}$$



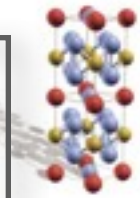
Volkswagen & BMW have developed thermoelectric generators that recover waste heat from a car engine.



Voyagers 1&2 ( 10 billion miles beyond Neptune's orbit, 30 years old) still functioning!

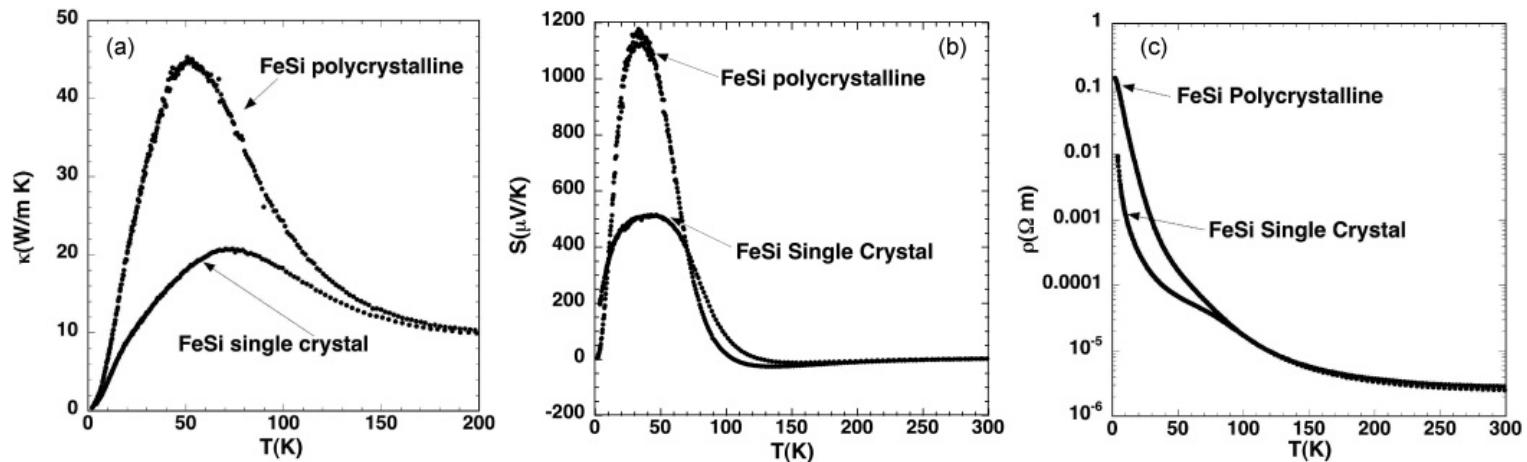
Running on thermoelectric generators, converting heat to electricity.

# FeSi thermoelectric



Best thermoelectrics are

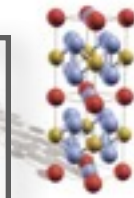
- lightly doped semiconductors ( $\text{Bi}_2\text{Te}_3$ ) or
- correlated semiconductors  $\text{FeSb}_2$ ,  $\text{Na}_x\text{CoO}_2$ ,  $\text{FeSi}$



What is the origin? Previous proposals:

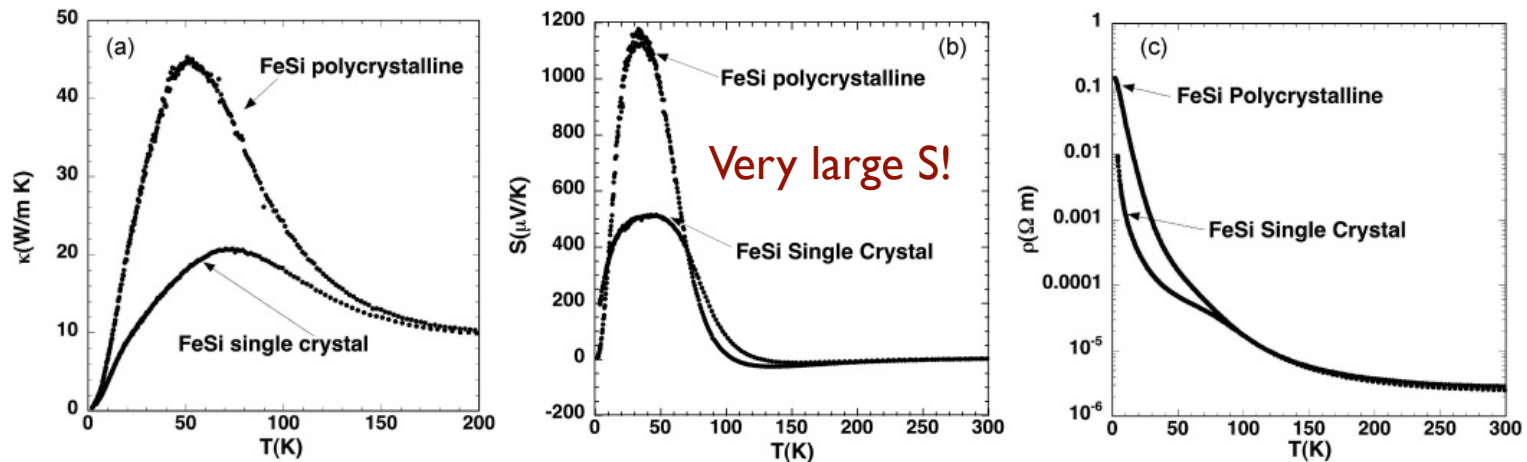
- lattice degrees of freedom
- electron-electron correlations due to Hubbard physics
- spin fluctuations
- spin-state transitions : high-spin to low spin
- thermally induced mixed valence

# FeSi thermoelectric



Best thermoelectrics are

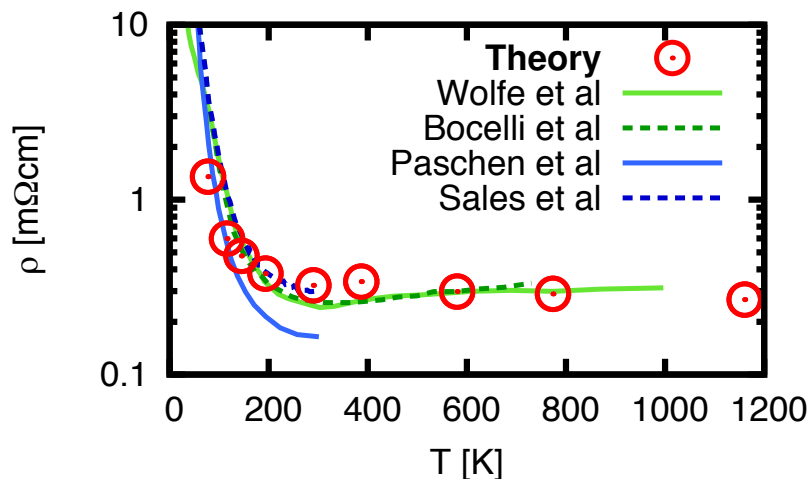
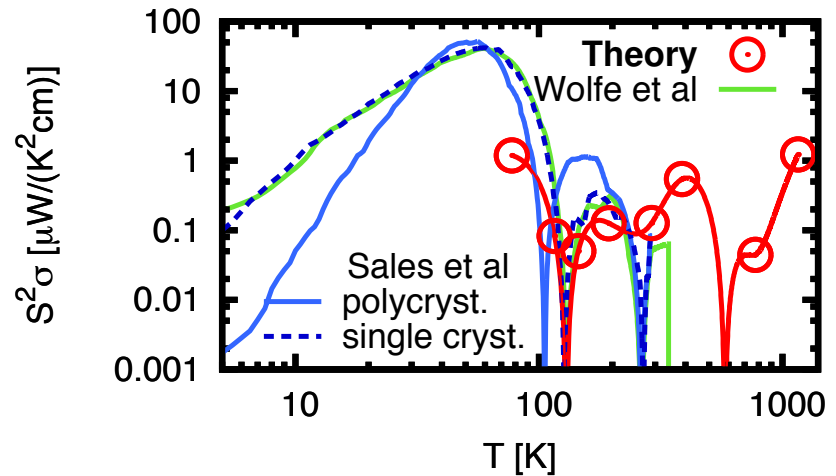
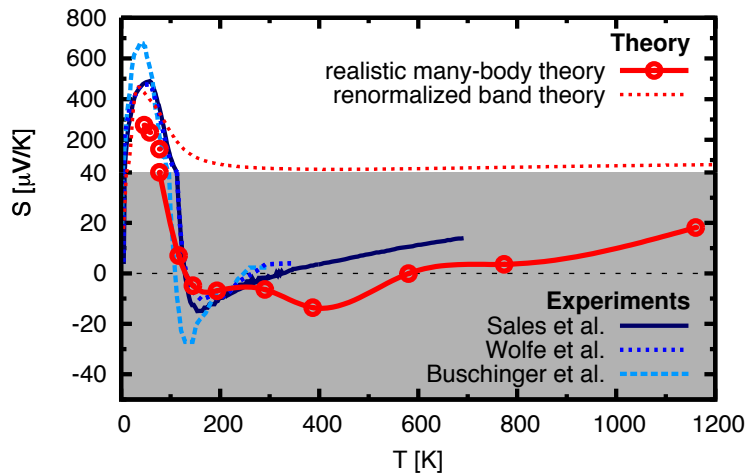
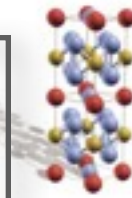
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What is the origin? Previous proposals:

- lattice degrees of freedom
- electron-electron correlations due to Hubbard physics
- spin fluctuations
- spin-state transitions : high-spin to low spin
- thermally induced mixed valence

# FeSi by DFT+DMFT

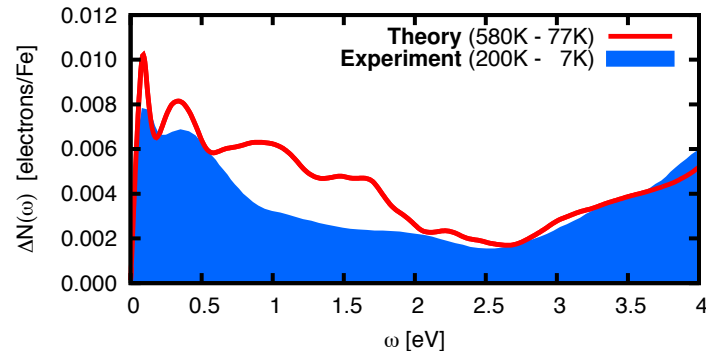
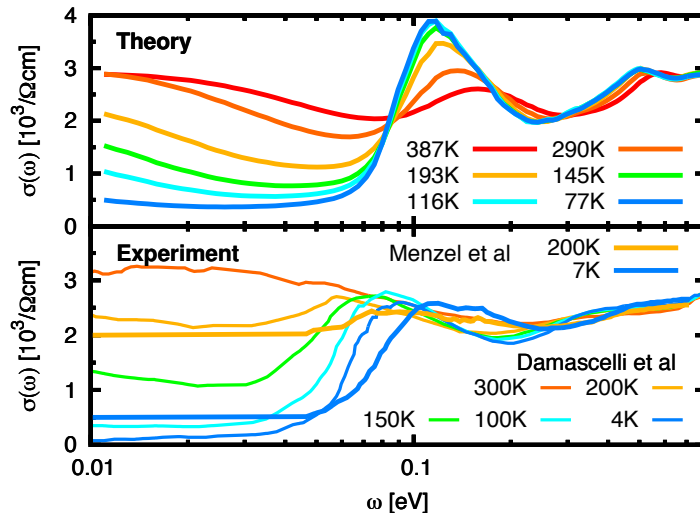


Transport well explained by DFT+DMFT.

J.M. Tomczak, K. Haule, G. Kotliar,  
Proceedings of the National  
Academy of Sciences (2012)

(a.)

# Dynamics of FeSi

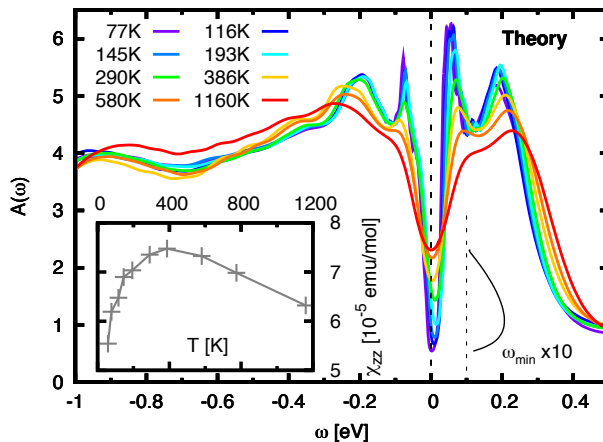


$$N_T(\omega) = \frac{2m_e V}{\pi e^2} \int_0^\omega d\omega' \sigma(\omega', T)$$

$$\Delta N(\omega) = N_{T_1}(\omega) - N_{T_2}(\omega)$$

Even temperature dependent spectral weight transfer well explained by DMFT!

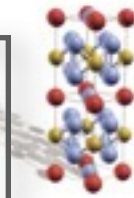
- Closing of the gap is due to incoherence at finite T!
- The origin of strong incoherence is in Hund's coupling



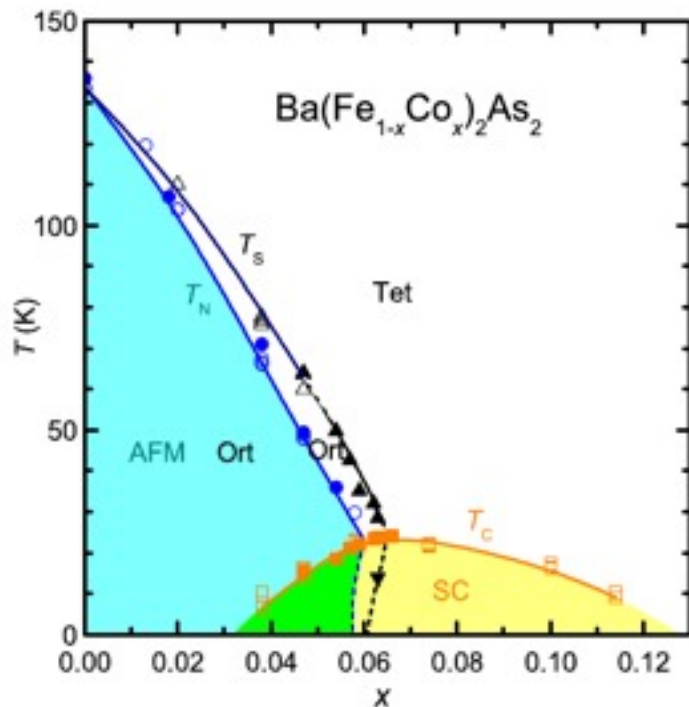
Hund's semiconductor!  
(see later for Hund's metals)

J.M. Tomczak, K. Haule, G. Kotliar,  
Proceedings of the National Academy  
of Sciences (2012)

# Fe pnictides



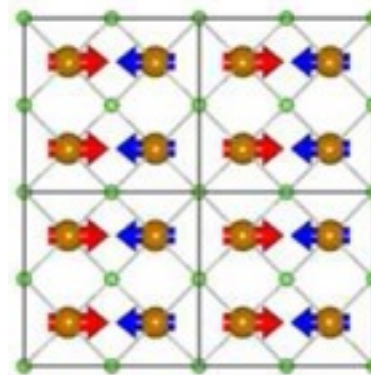
Proximity to magnetic state:  
Important to understand nature of SC.  
Correlation effects?



Two types of orderings:

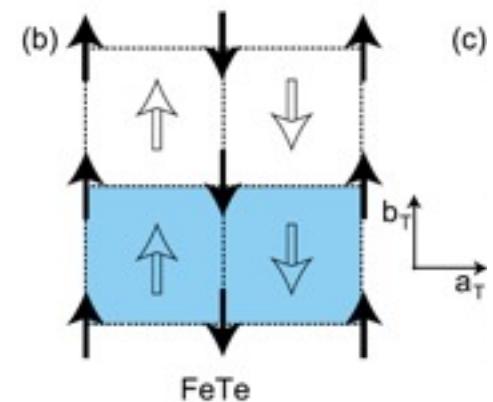
SDW

$$(\pi, 0, \pi)$$



DSDW

$$(\pi/2, \pi/2, \pi)$$

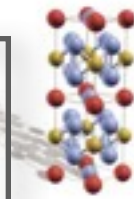


Neutrons by: Clarina de la Cruz et.al, Nature 453, 899 (2008).

W. Bao et al., PRL 102, 247001 (2009).



# Early DMFT predictions



PRL **100**, 226402 (2008)

PHYSICAL REVIEW LETTERS

week ending  
6 JUNE 2008



## Correlated Electronic Structure of $\text{LaO}_{1-x}\text{F}_x\text{FeAs}$

K. Haule, J. H. Shim, and G. Kotliar

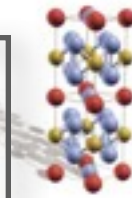
*Department of Physics, Rutgers University, Piscataway, New Jersey 08854, USA*

(Received 9 March 2008; published 2 June 2008)

phonon mediated. Indeed an explicit calculation of the phonon coupling constants within the DFT, using the code of Ref. [5], gives a value too small to explain the observed critical temperature ( $T_c < 1$  K).

The situation is different in the doped compound [see Fig. 4(b)] where the electron pockets clearly cross the Fermi level. The band velocity and effective mass are considerably enhanced (3–5 times) while the scattering rate still remains large. Finally, the hole pockets around  $\Gamma$  remain highly scattered.

# Early DMFT predictions



PRL **100**, 226402 (2008)

PHYSICAL REVIEW LETTERS

week ending  
6 JUNE 2008



## Correlated Electronic Structure of $\text{LaO}_{1-x}\text{F}_x\text{FeAs}$

K. Haule, J. H. Shim, and G. Kotliar

*Department of Physics, Rutgers University, Piscataway, New Jersey 08854, USA*

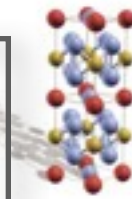
(Received 9 March 2008; published 2 June 2008)

phonon mediated. Indeed an explicit calculation of the phonon coupling constants within the DFT, using the code of Ref. [5], gives a value too small to explain the observed critical temperature ( $T_c < 1$  K).

Unconventional SC  
Phonon  $T_c < 1$  K

The situation is different in the doped compound [see Fig. 4(b)] where the electron pockets clearly cross the Fermi level. The band velocity and effective mass are considerably enhanced (3–5 times) while the scattering rate still remains large. Finally, the hole pockets around  $\Gamma$  remain highly scattered.

# Early DMFT predictions



PRL **100**, 226402 (2008)

PHYSICAL REVIEW LETTERS

week ending  
6 JUNE 2008



## Correlated Electronic Structure of $\text{LaO}_{1-x}\text{F}_x\text{FeAs}$

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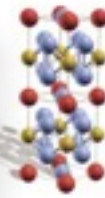
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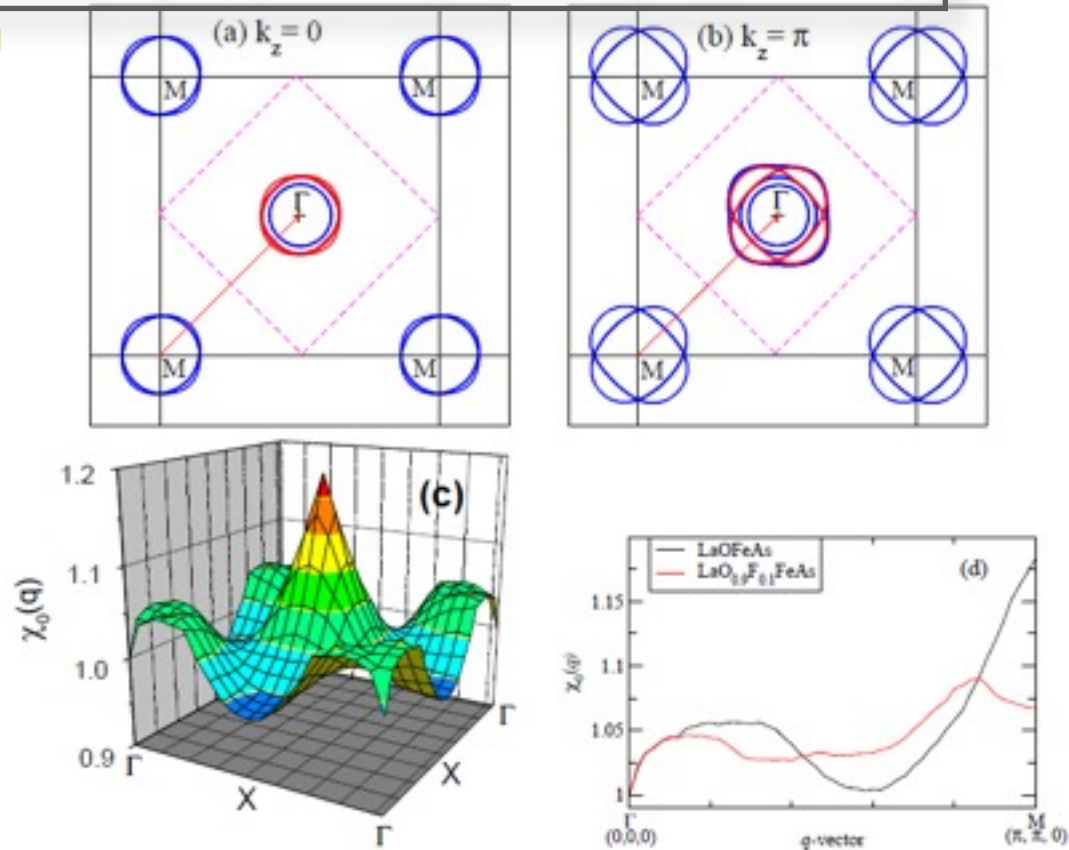
Importance of correlations  
Mass enhancement 3–5



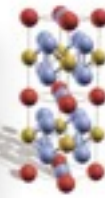
# Magnetic state in standard theory (LDA)



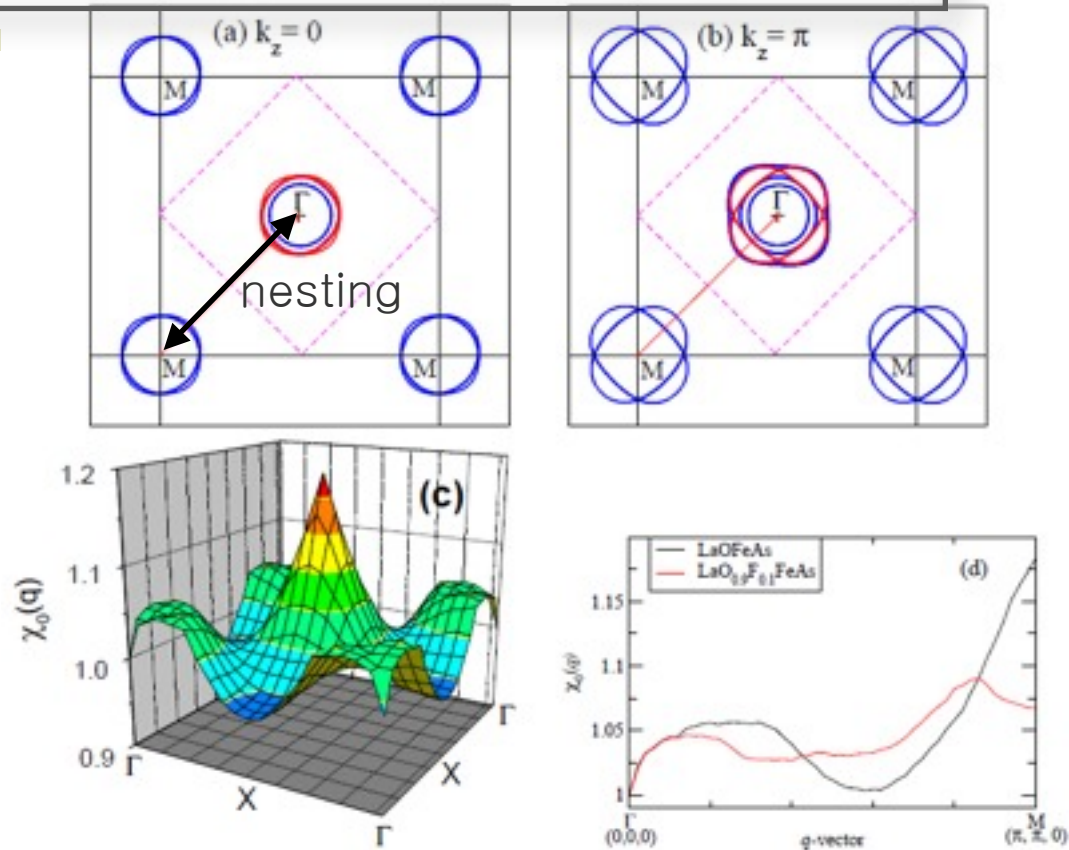
Magnetic ordering correctly predicted by LDA, (nesting)



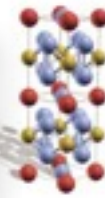
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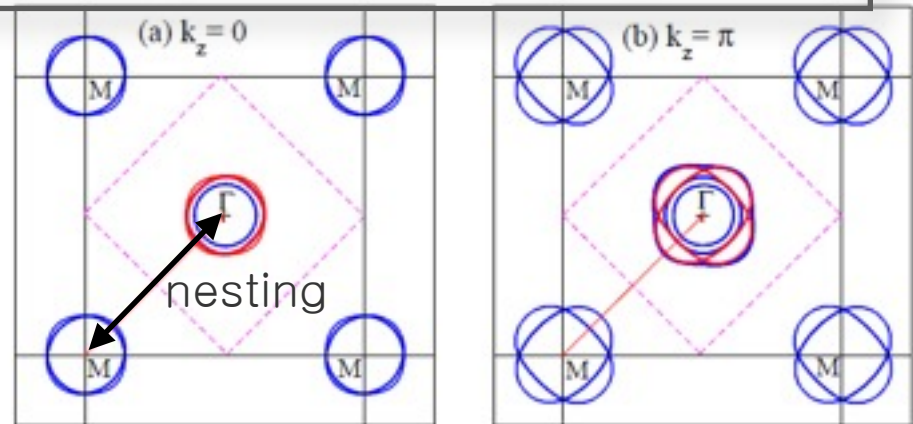
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# Magnetic state in standard theory (LDA)



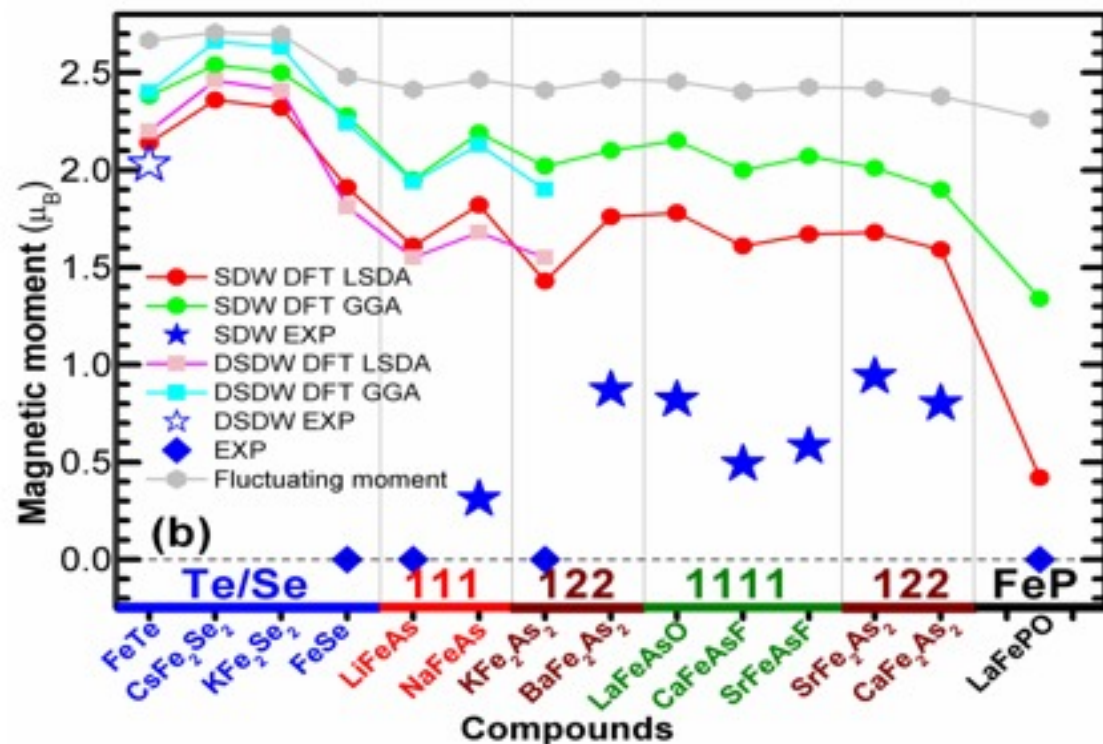
Magnetic ordering correctly predicted by LDA, (nesting)



Magnetic moment:

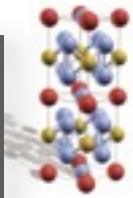
LDA  $\sim 2\mu_B$ ,  
exp  $\sim 0-0.9\mu_B$  (2 in FeTe)  
too large moment!

Wrong trend in the size of the moment across compounds

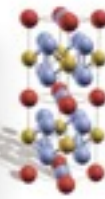




# Mass enhancement & Magnetic moment

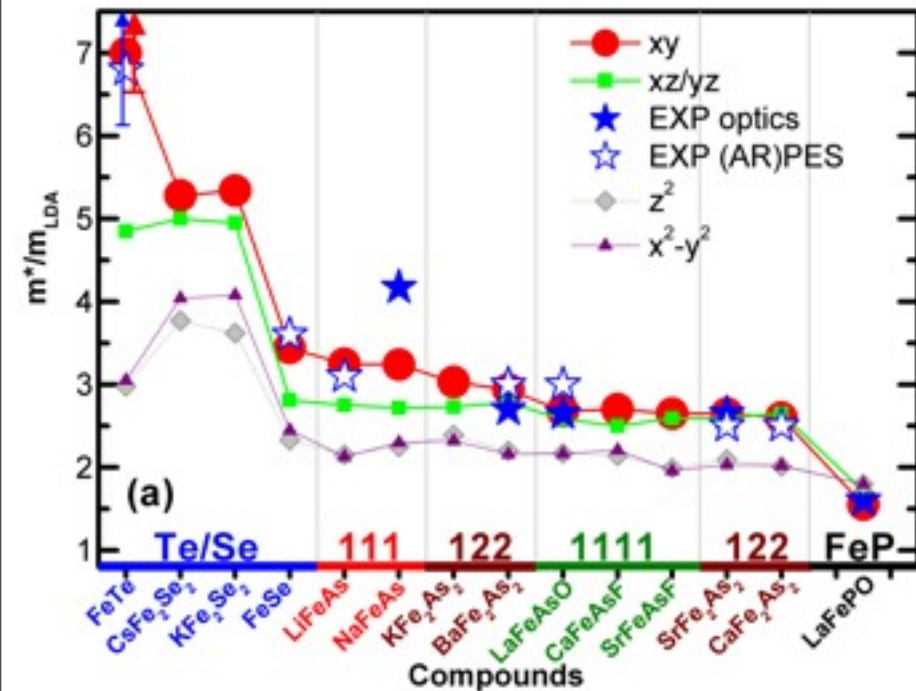


# Mass enhancement & Magnetic moment



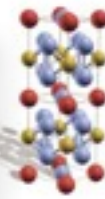
Z. P. Yin, K. H., G. Kotliar, Nature Materials (2011)

Correlation diagram of Hund's metals



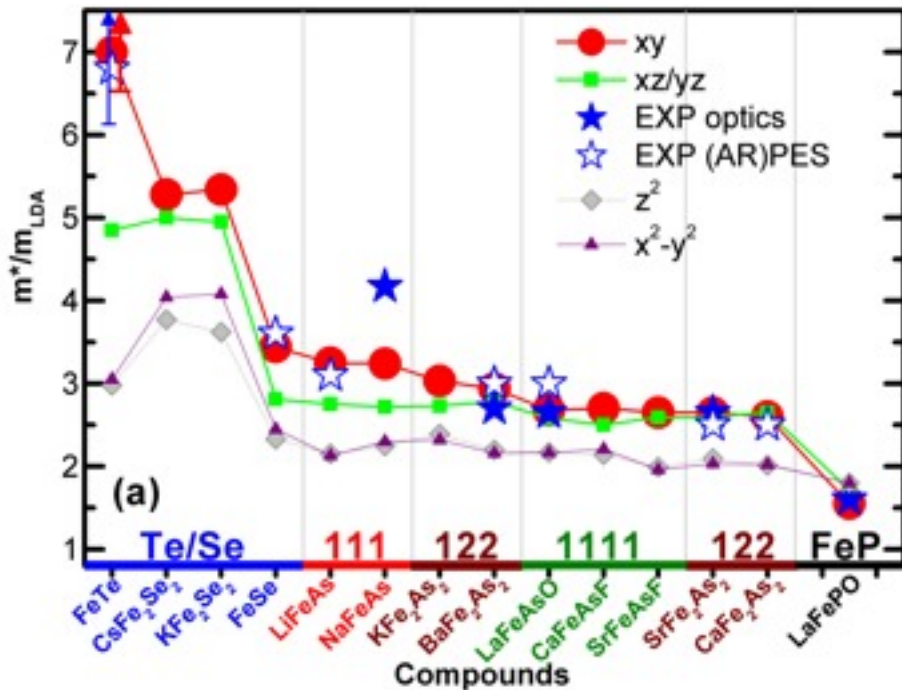
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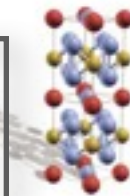
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Good agreement with experiment!

We fixed  $U=5\text{eV}$  and  $J=0.8\text{eV}$  to  
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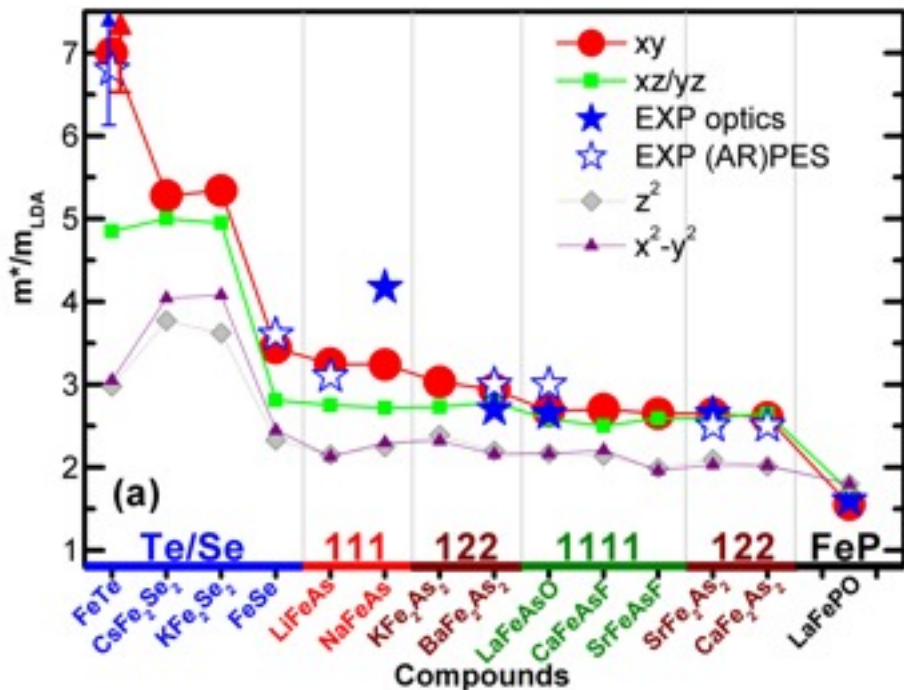
([PRB 82, 045105 \(2010\)](#)).

# Mass enhancement & Magnetic moment



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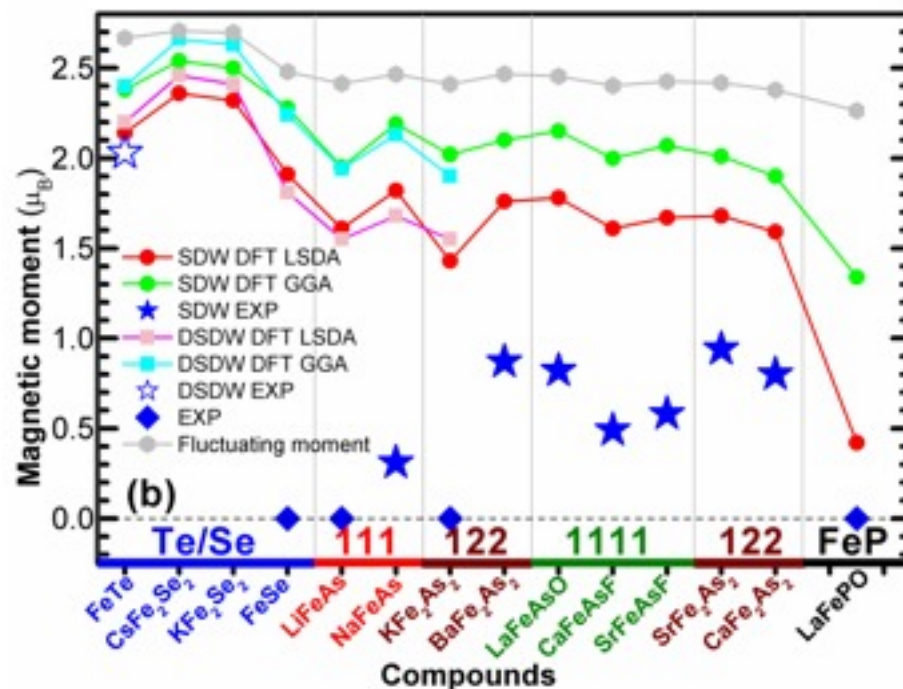
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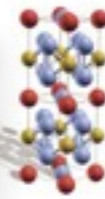
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## Static ordered moment within DFT

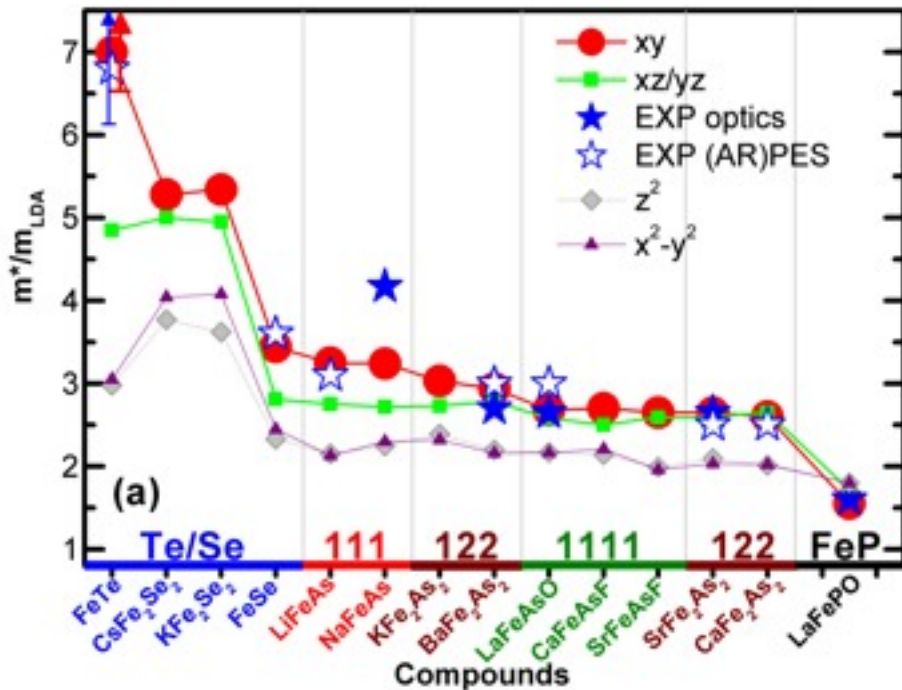


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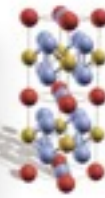
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([PRB 82, 045105 \(2010\)](#)).



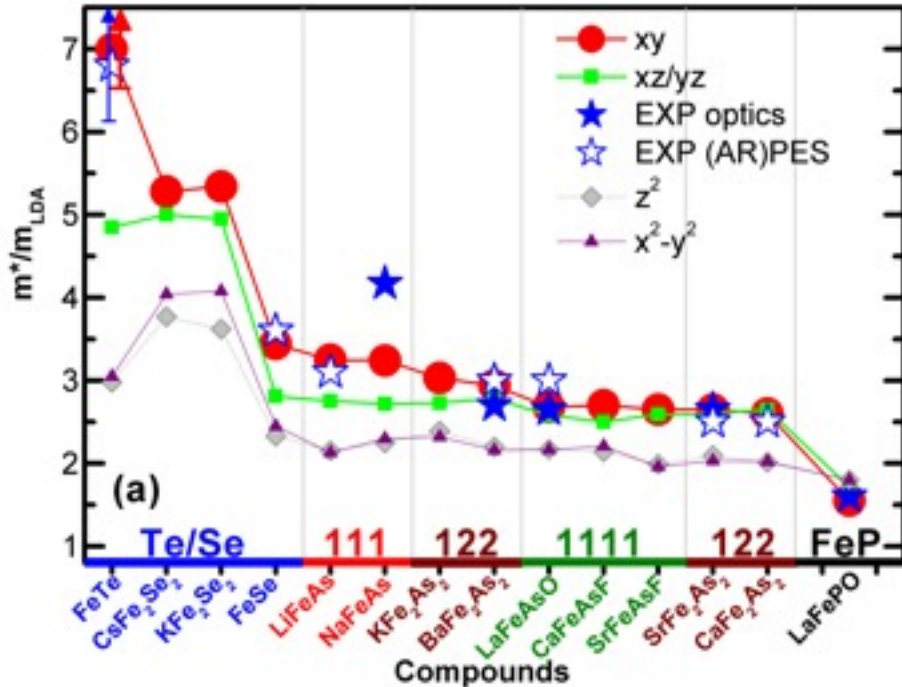
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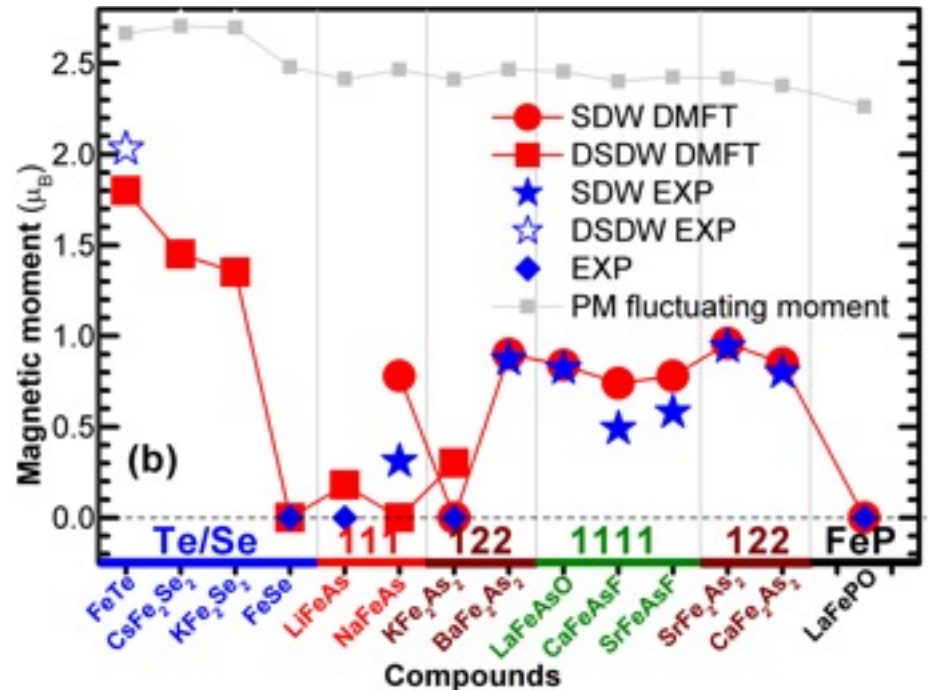
Static ordered moment within LDA+DMFT



Mass enhancement substantial  
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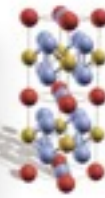
([PRB 82, 045105 \(2010\)](#)).



Static ordered moment very small



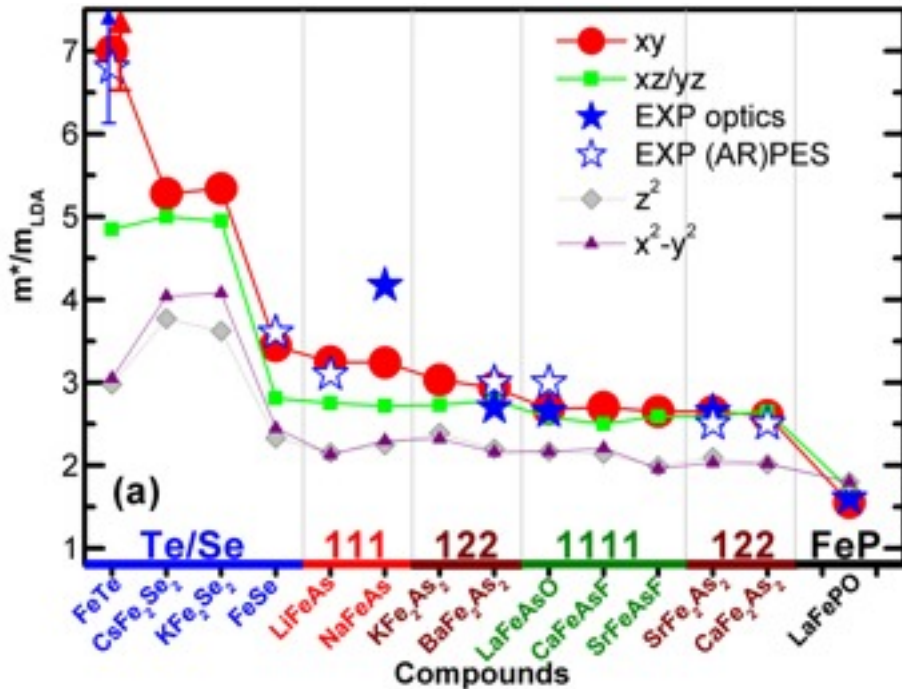
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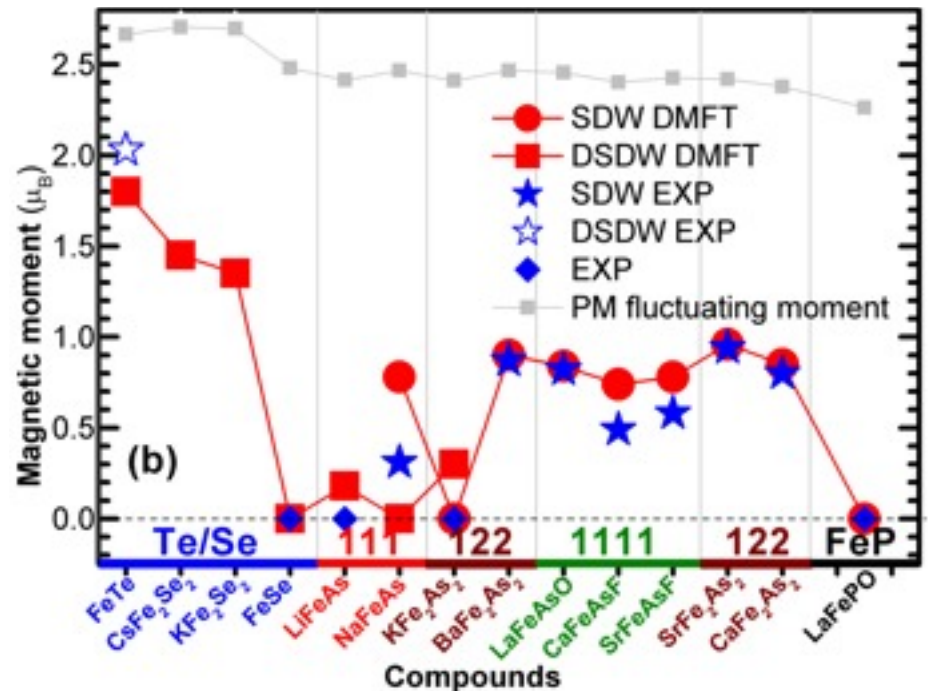
Correlation diagram of Hund's metals

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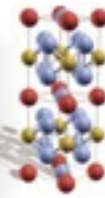


Static ordered moment very small

moment  $\leftrightarrow$  mass

Some similarity, but also many differences!

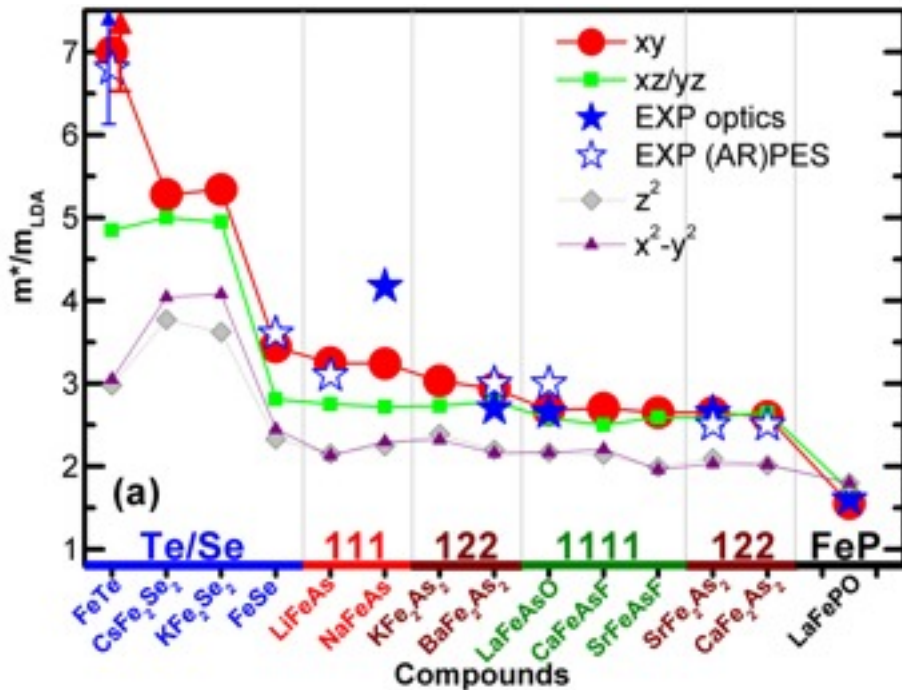
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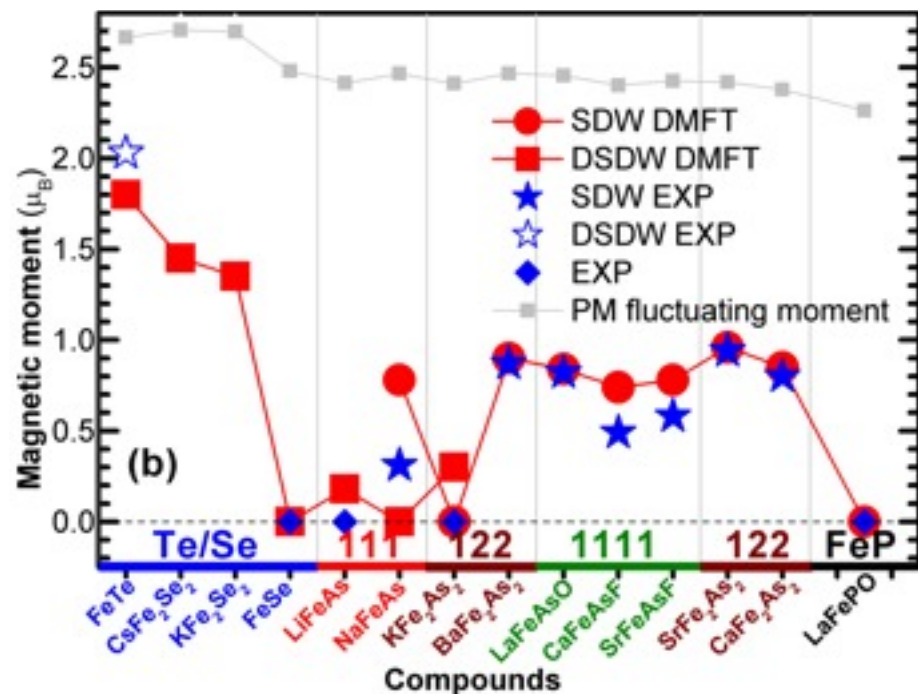
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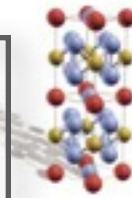


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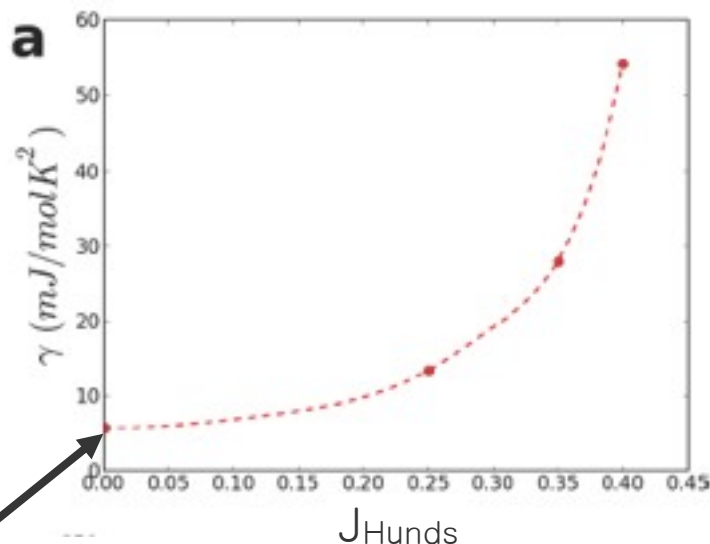
NO FITTING PARAMETER

# Importance of Hund's rule



Hubbard  $U$  is not the “relevant” parameter.

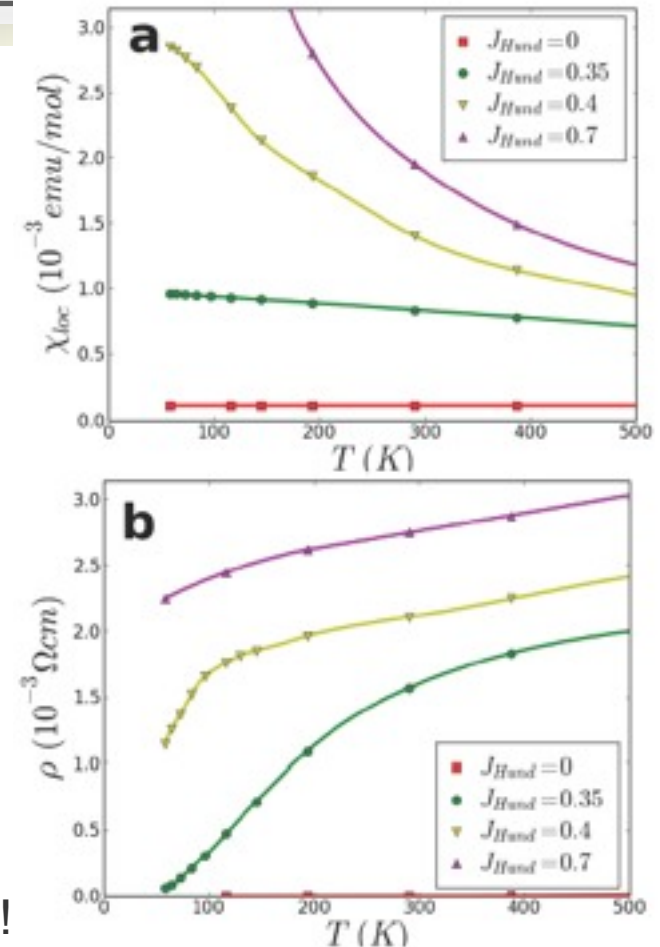
The **Hund's coupling** brings correlations!



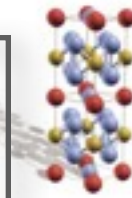
LDA value

For  $J=0$  there is negligible mass enhancement at  $U \sim W$ !

[New Journal of Physics Volume 11 February 2009](#)

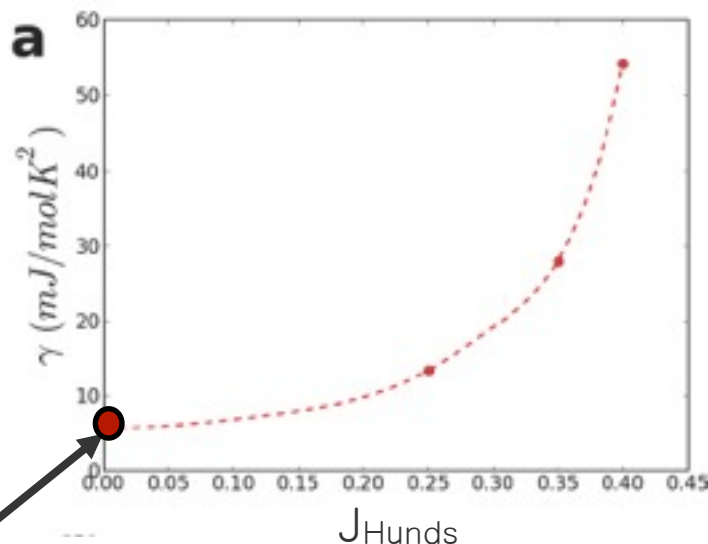


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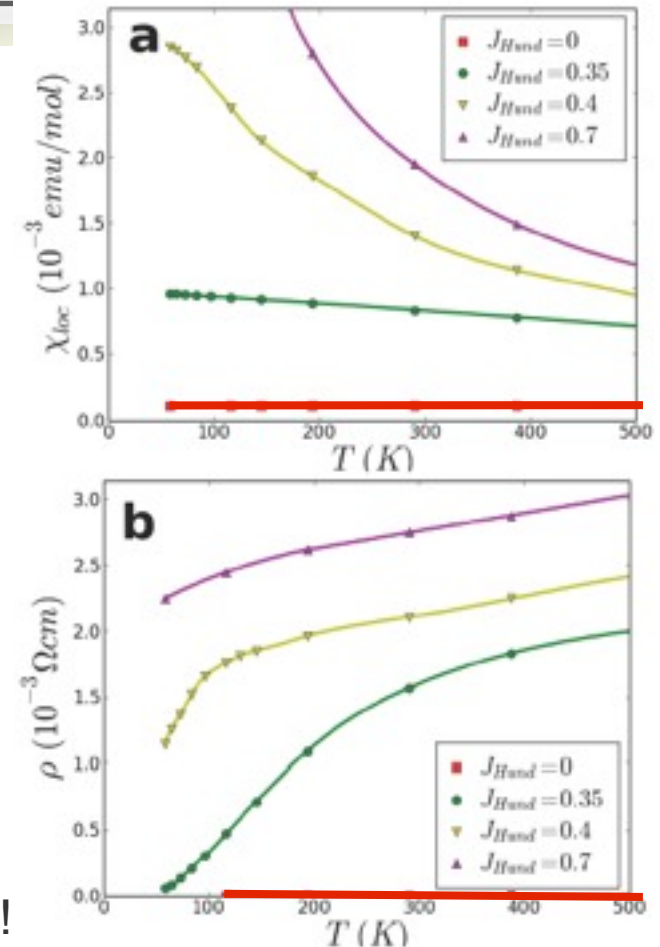


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The **Hund's coupling** brings correlations!



$J=0$

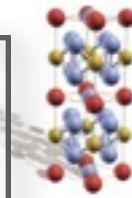


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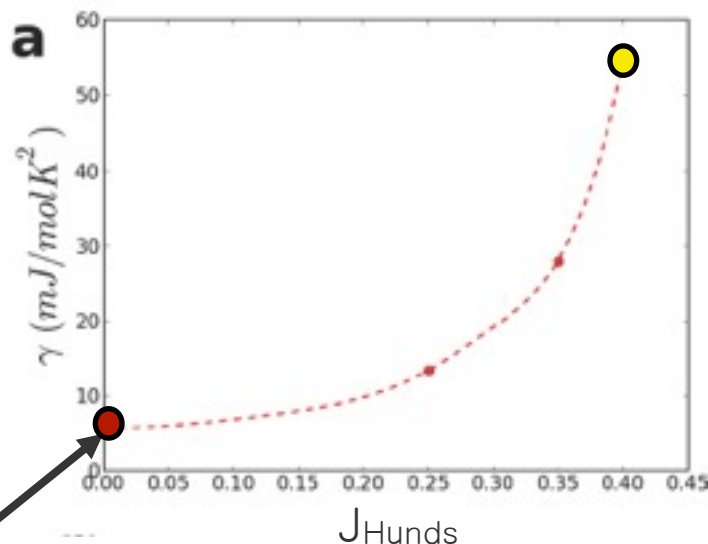


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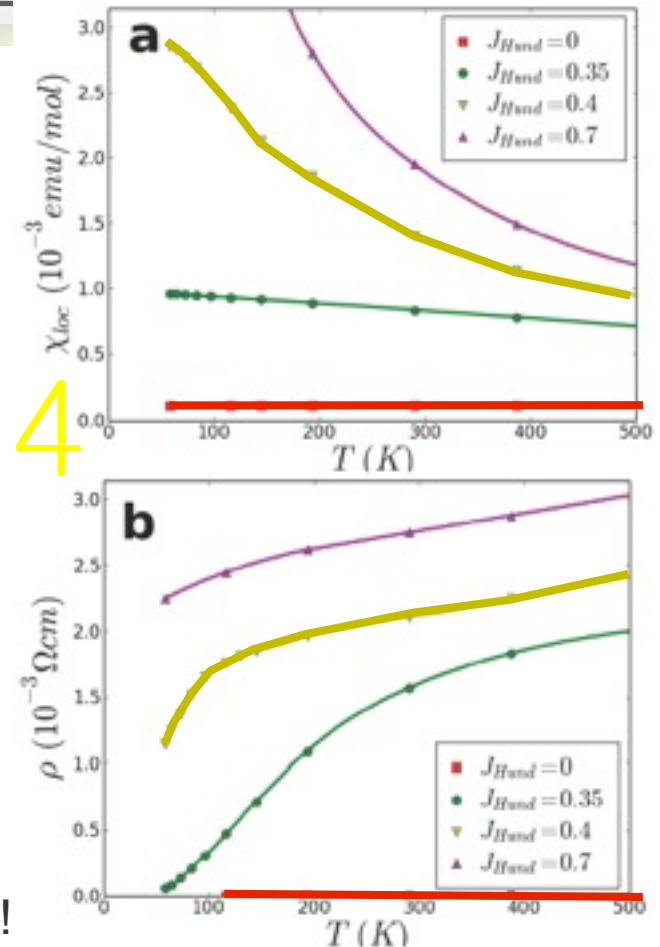


LDA value

$J=0.4$

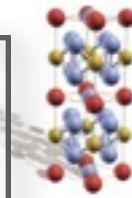
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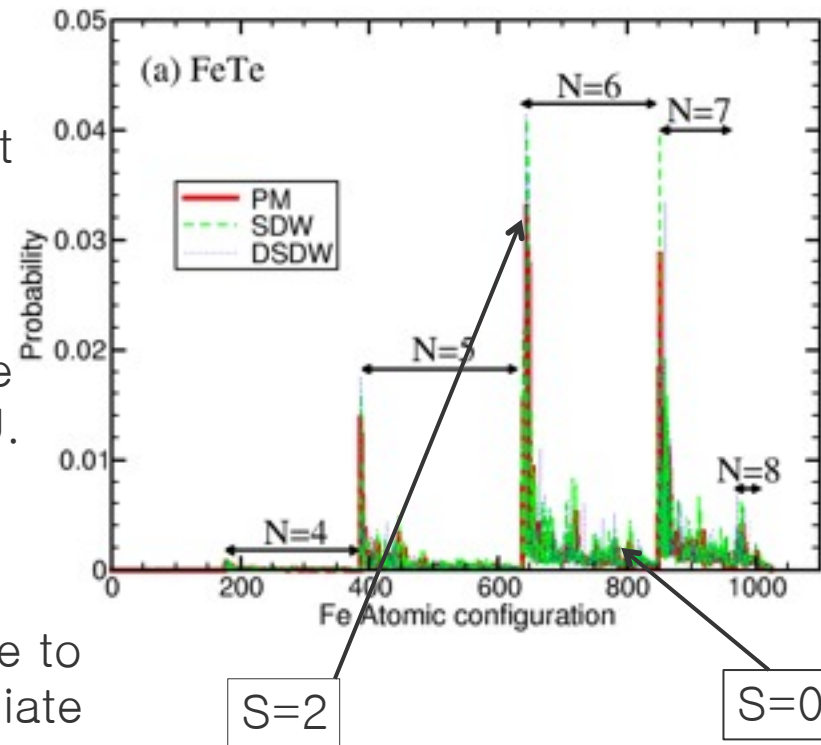
# Histogram of Hund's metals



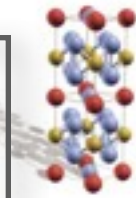
In oxides, only a few atomic states (one in each valence) with significant Probability

In pnictides, many states with large probability  $\rightarrow$  charge fluctuations are not efficiently blocked by Coulomb  $U$ . (more itinerant system)

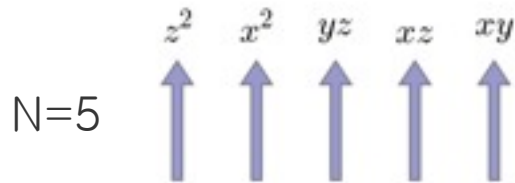
States with high spin more probable than those with low spin  $\rightarrow$  gives rise to non-Fermi liquid physics at intermediate temperatures, and heavy quasiparticles at Low temperatures.



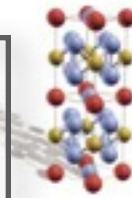
# What reduces Kondo screening?



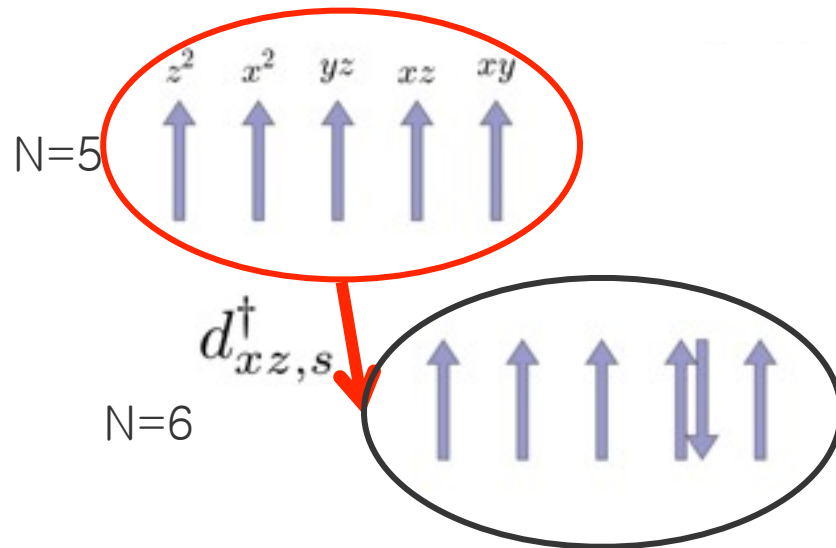
Orbital & spin blocking  
due to Hund's coupling



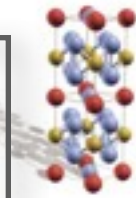
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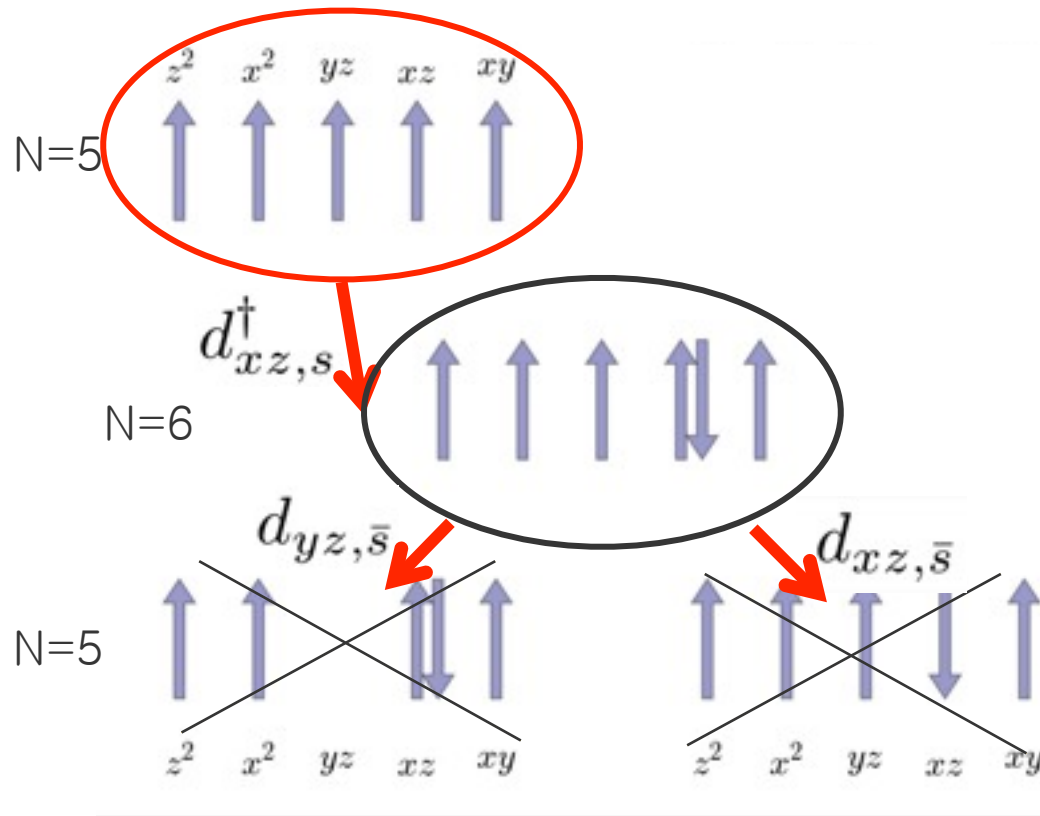
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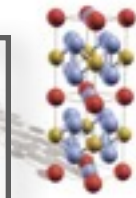
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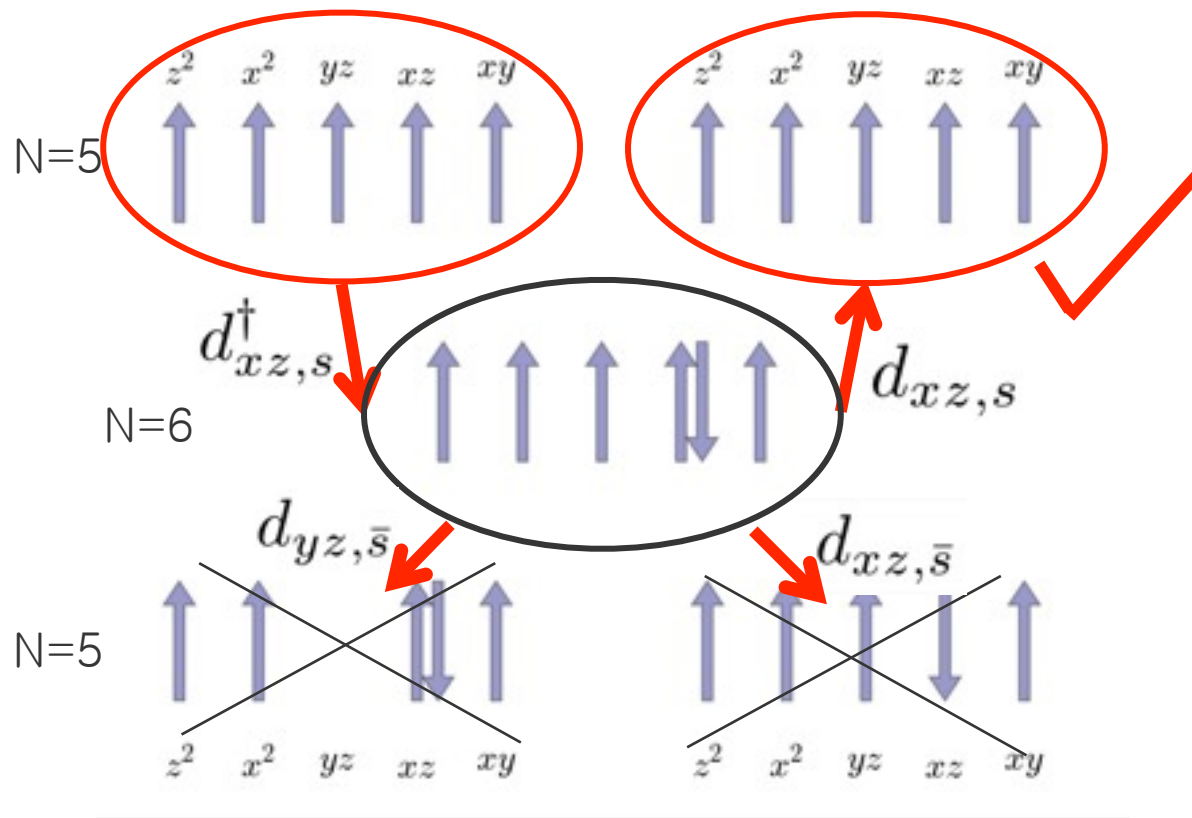
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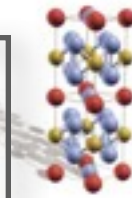


Orbital & spin blocking  
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# What reduces Kondo screening?



Orbital & spin blocking  
due to Hund's coupling

Low energy Kondo-like Hamiltonian

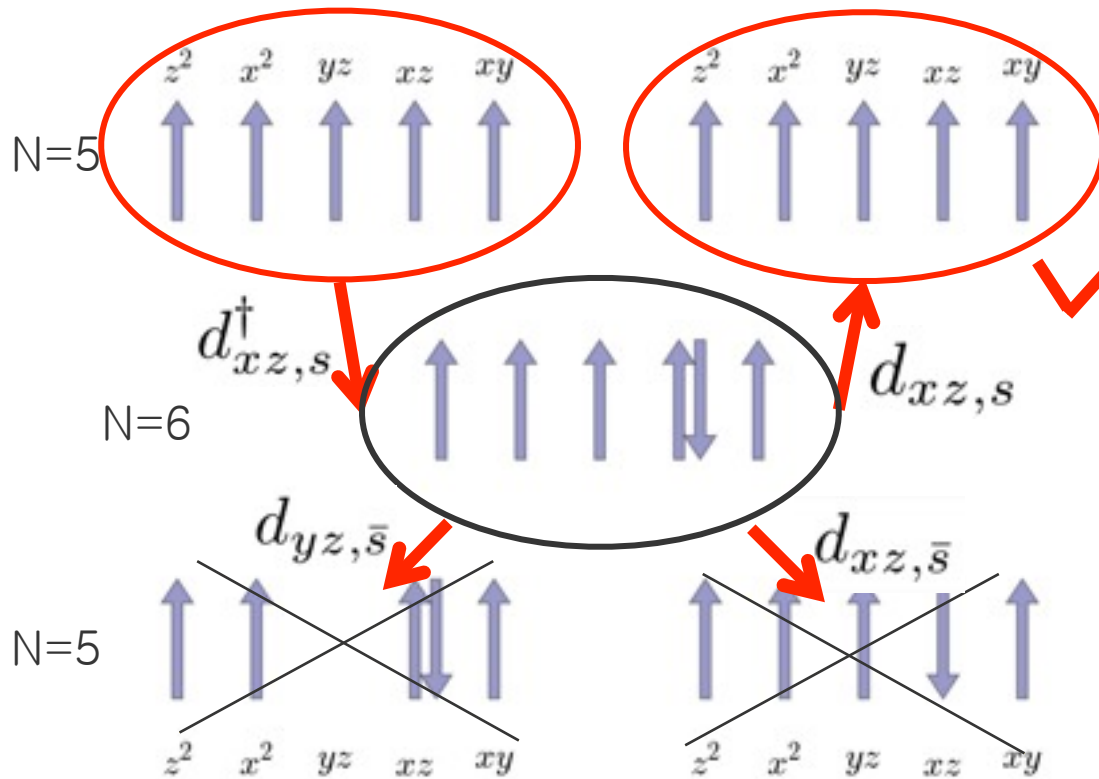
$$J_K d_{\alpha,s}^\dagger d_{\beta,s'} c_{\beta,s'}^\dagger c_{\alpha,s} = 0$$

unless  $\alpha = \beta$

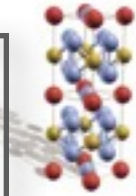
Only diagonal Kondo coupling

$$J_K \vec{S}_\alpha \vec{\sigma}_\alpha$$

+Schrieffer-Wolf tr.



# What reduces Kondo screening?

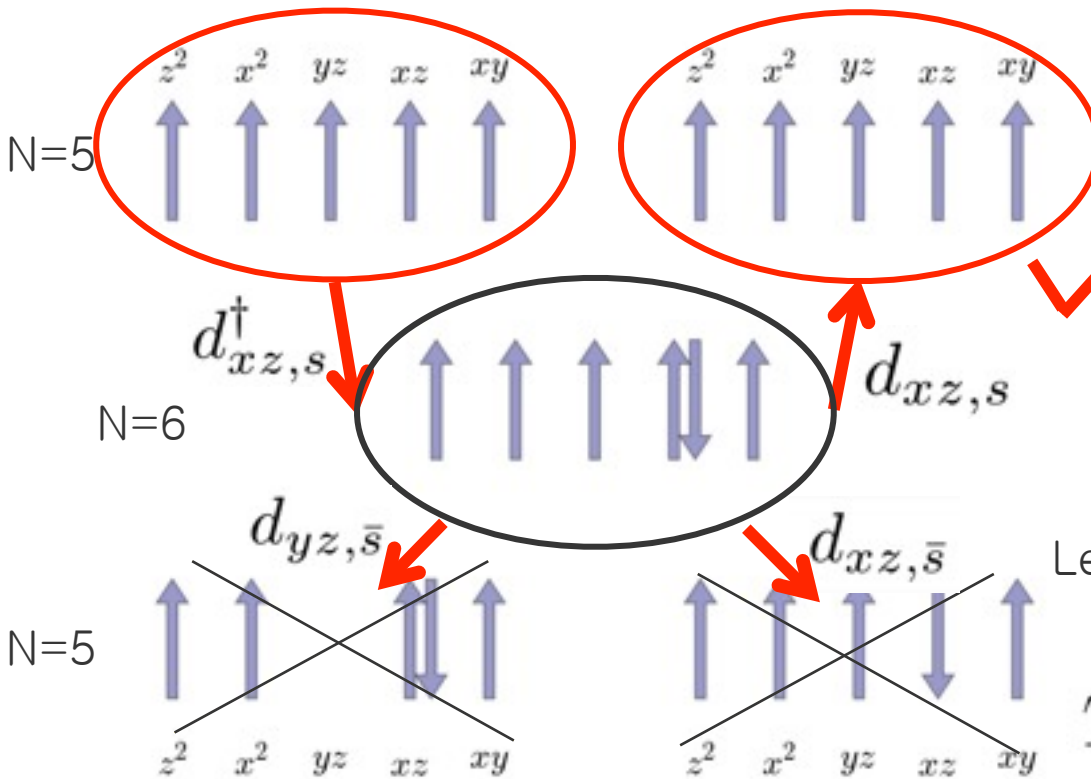


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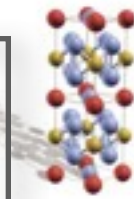
+Schrieffer-Wolf tr.

Leads to coherence temperature:

$$T^* \propto \exp \left( -\frac{(2S+1)^2}{\rho J_K} \right)$$

I. Okada, K. Yoshida,  
Progress of Theoretical Physics 49, 1483 (1973).

# What reduces Kondo screening?

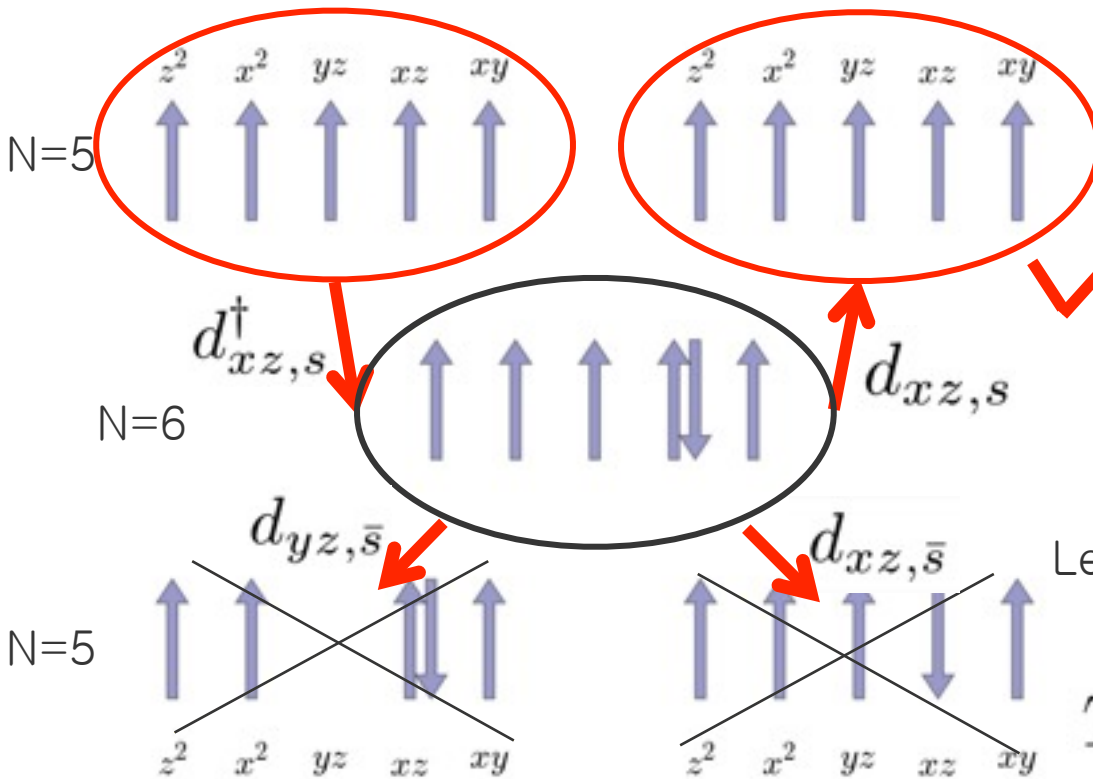


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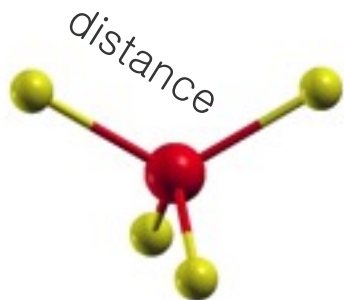
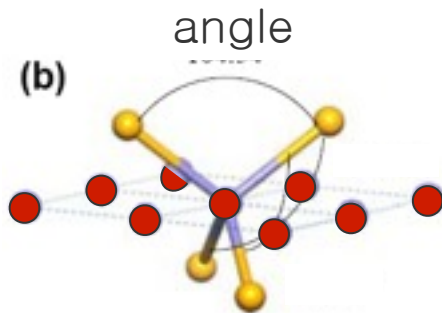
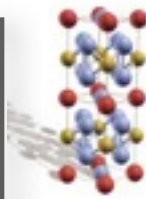
+Schrieffer-Wolf tr.

Leads to coherence temperature:

$$T^* \propto \exp \left( -\frac{25}{\rho J_K} \right)$$

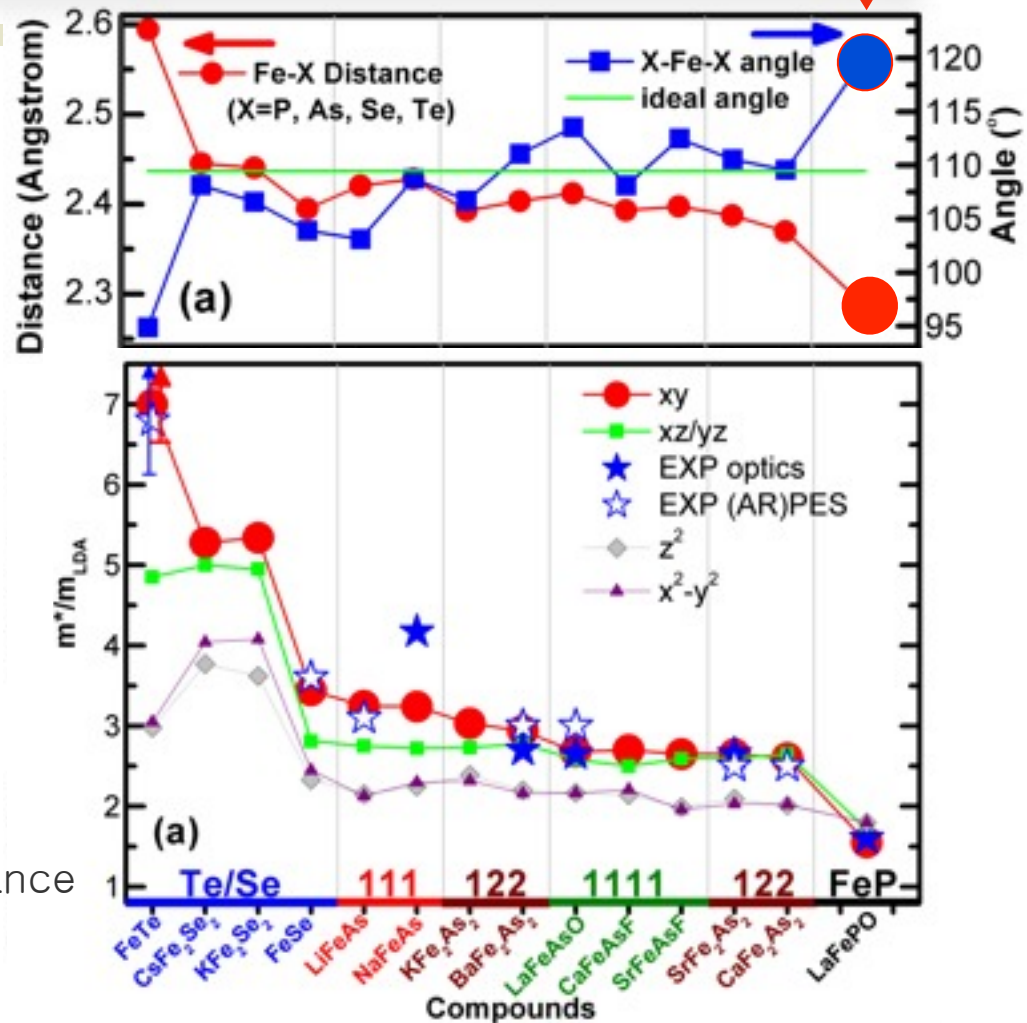
I. Okada, K. Yoshida,  
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# Strength of correlations

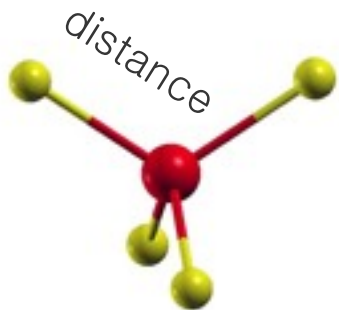
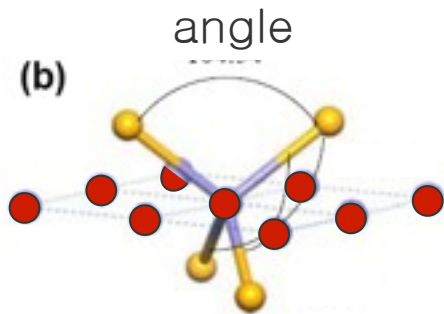


Overall trend consistent with Fe-As distance

Hybridization with pnictogen

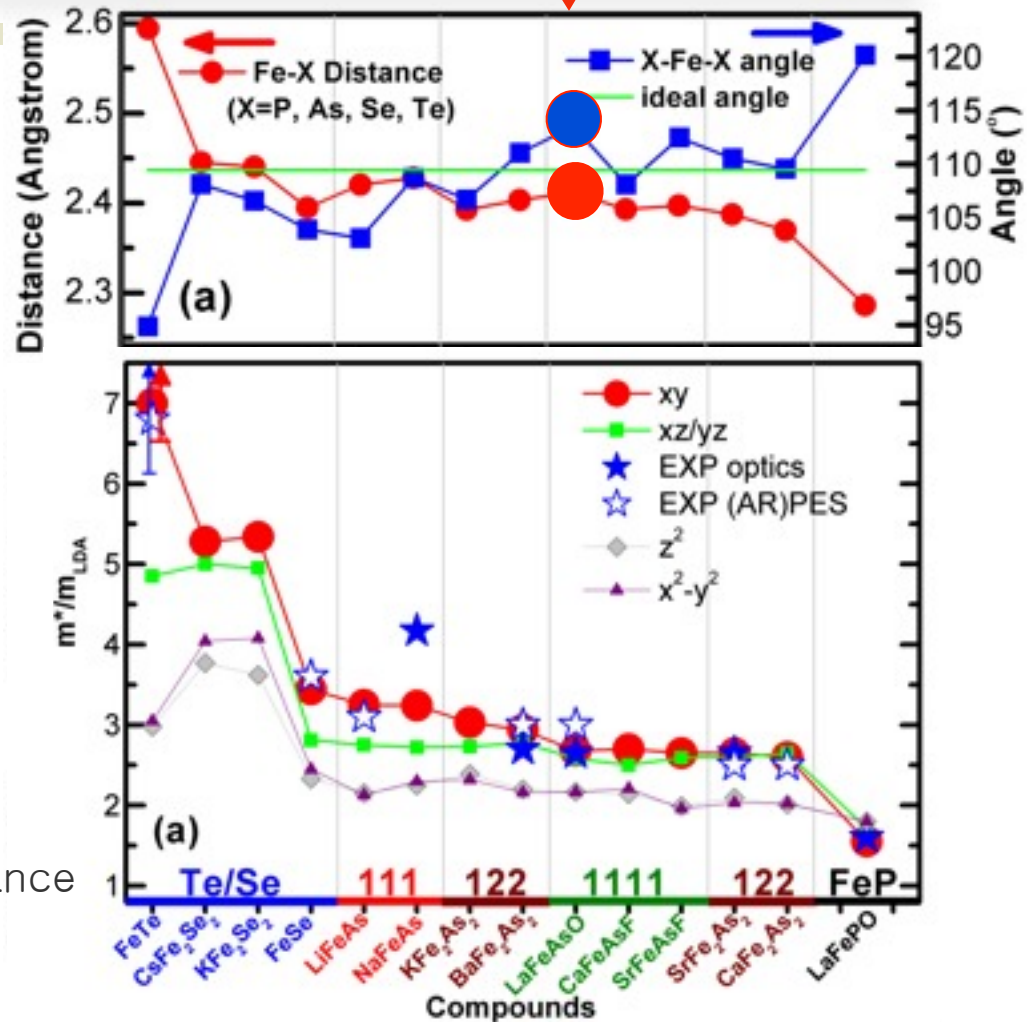


# Strength of correlations



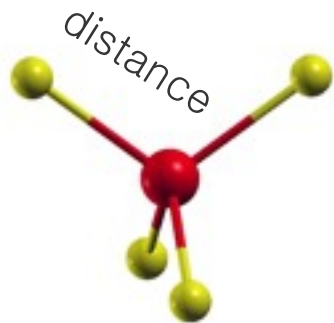
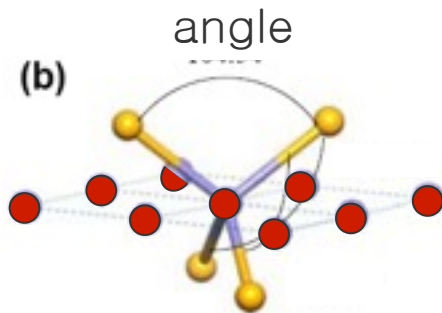
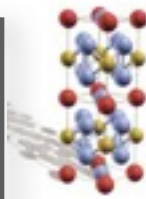
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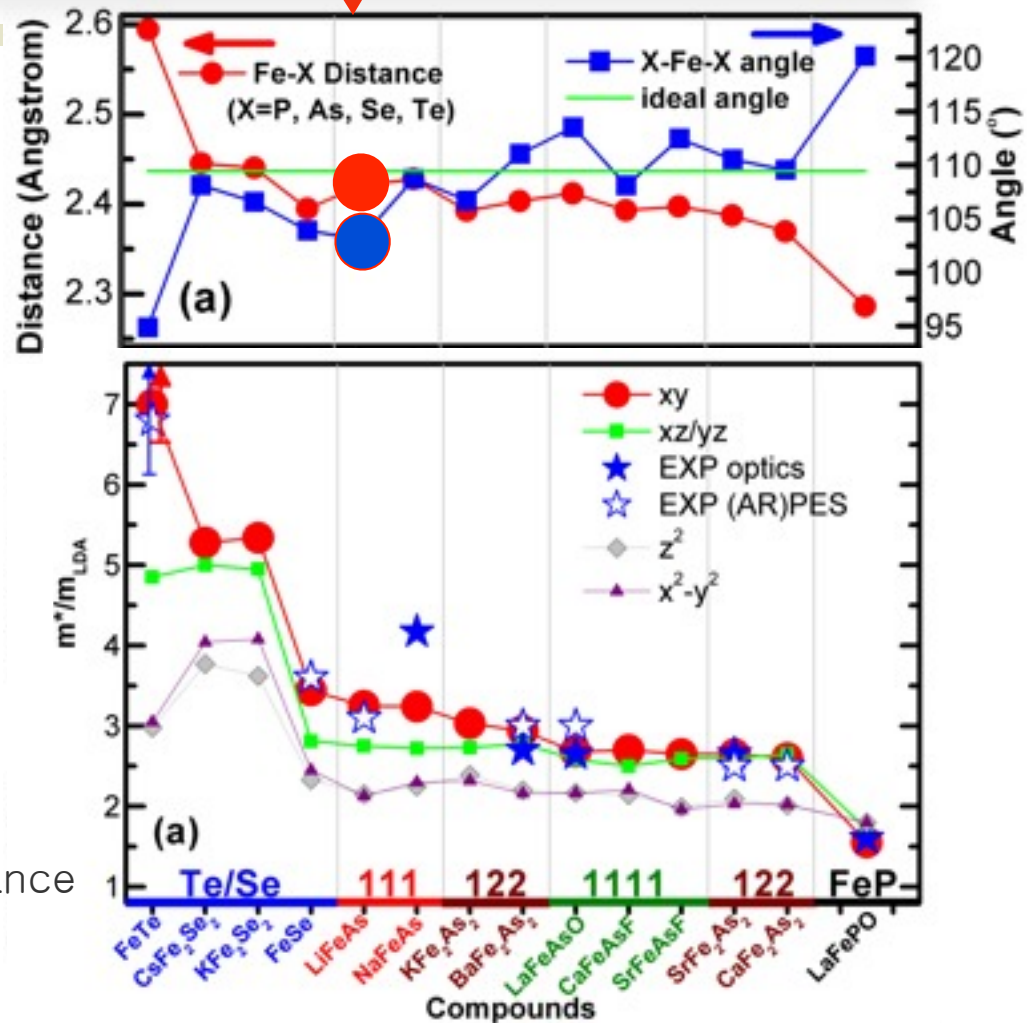


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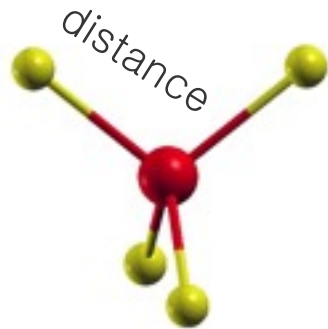
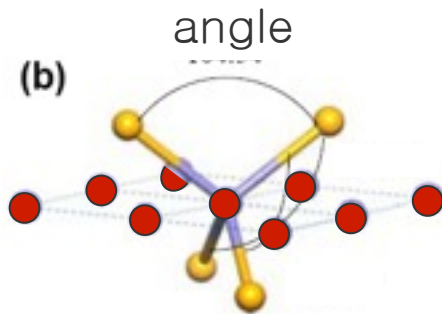
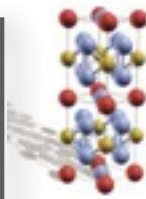


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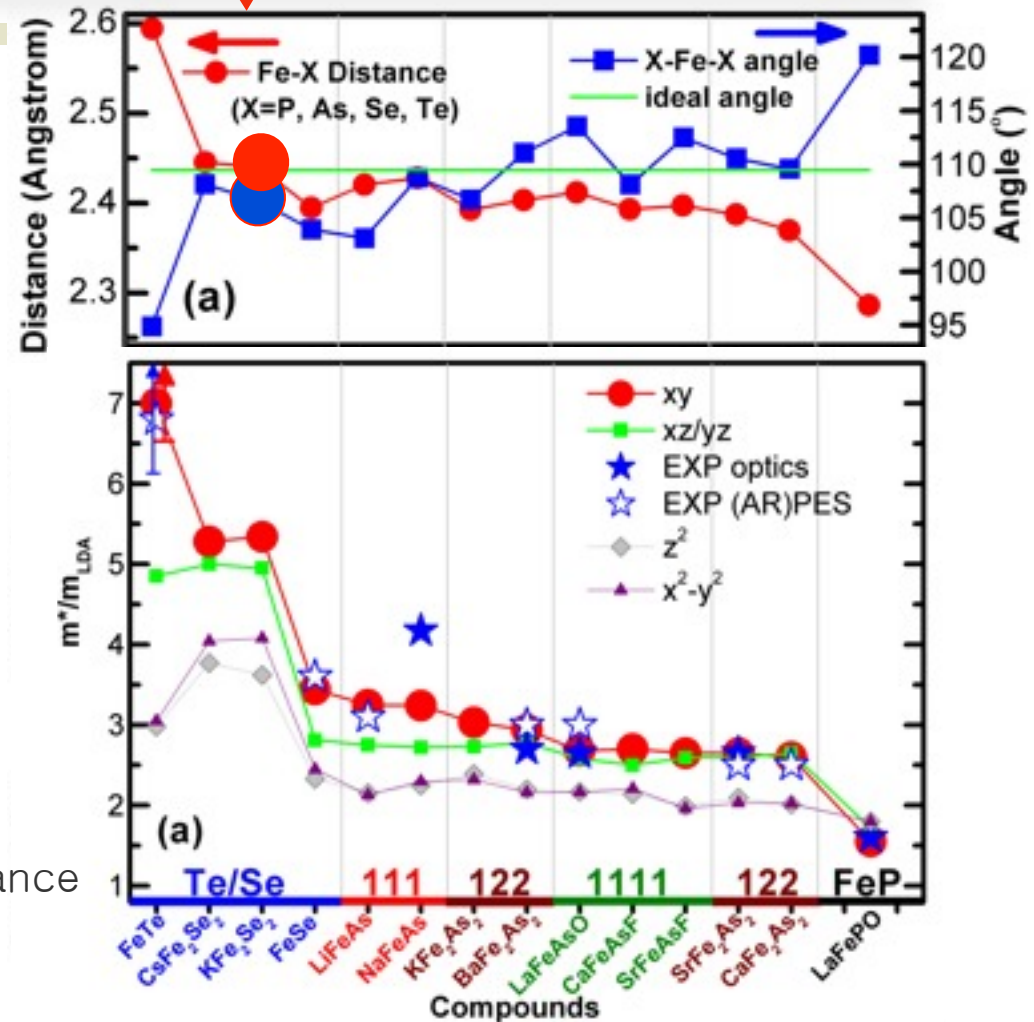


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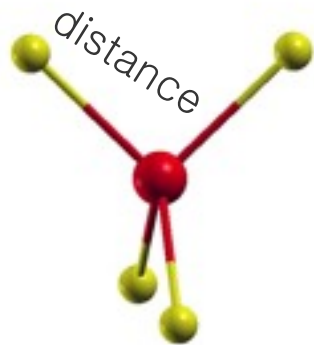
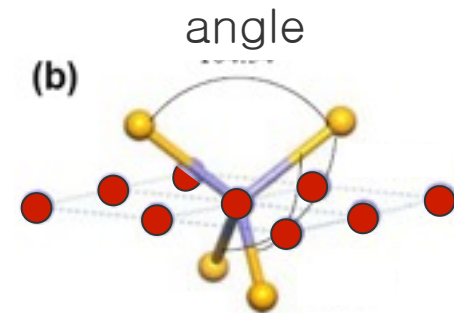


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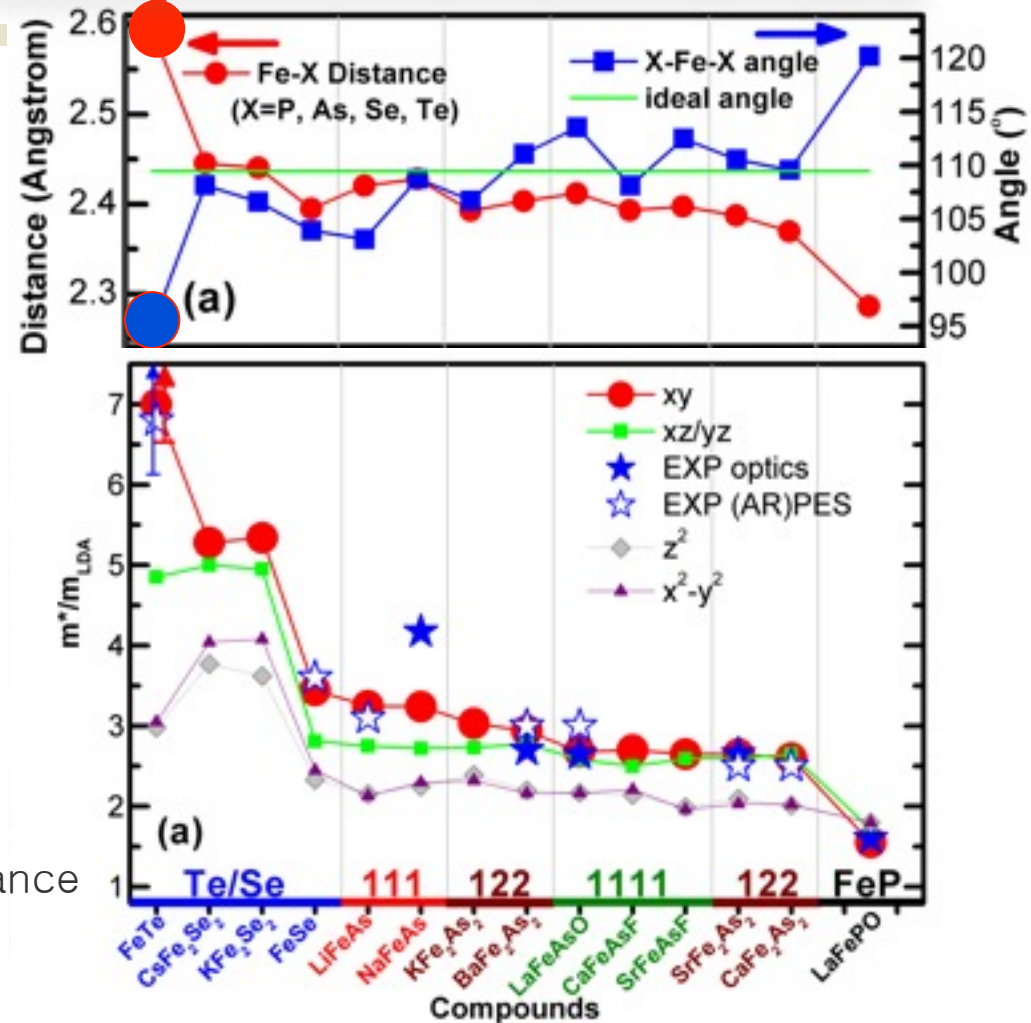


# Strength of correlations

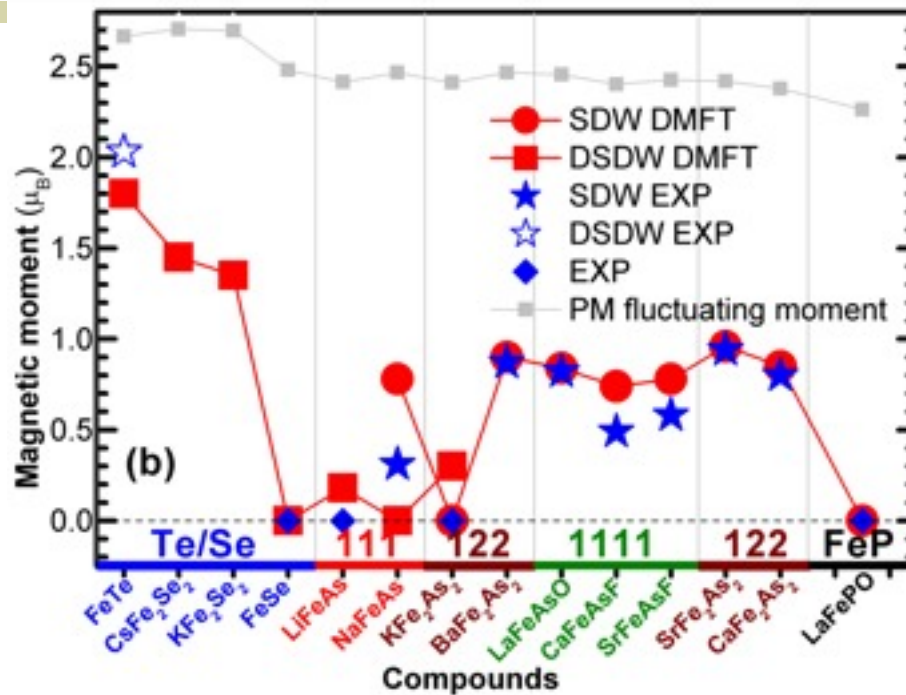


Overall trend consistent with Fe-As distance

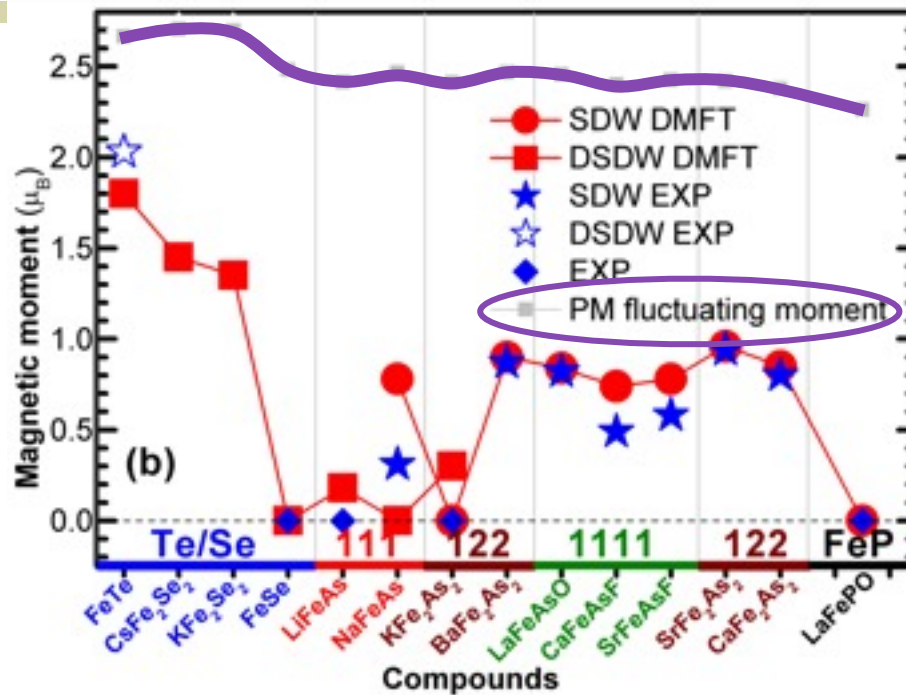
Hybridization with pnictogen



# Fluctuating moment

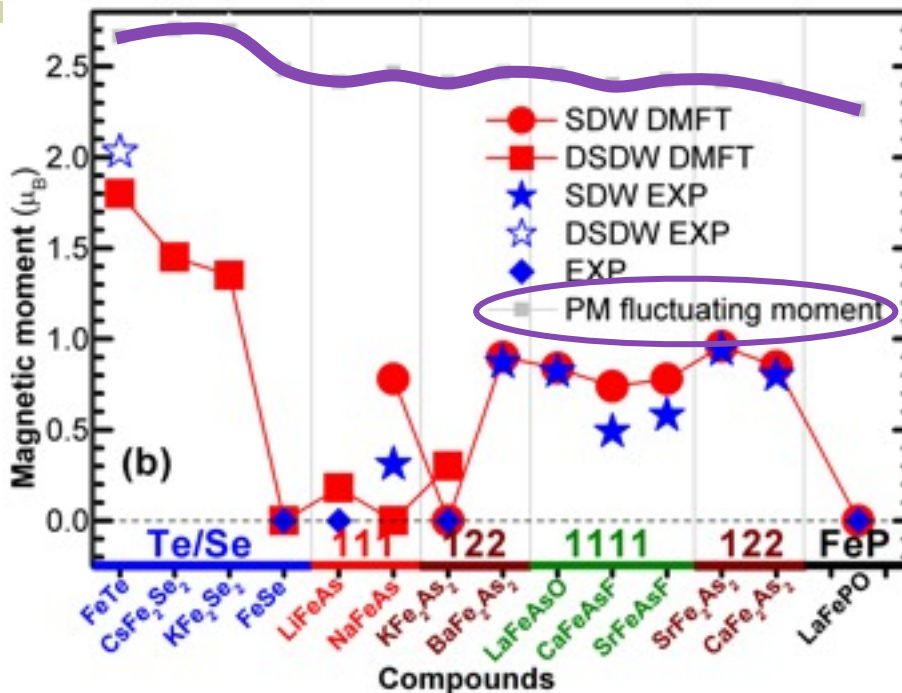
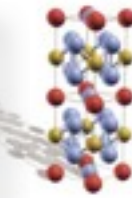


# Fluctuating moment





# Fluctuating moment

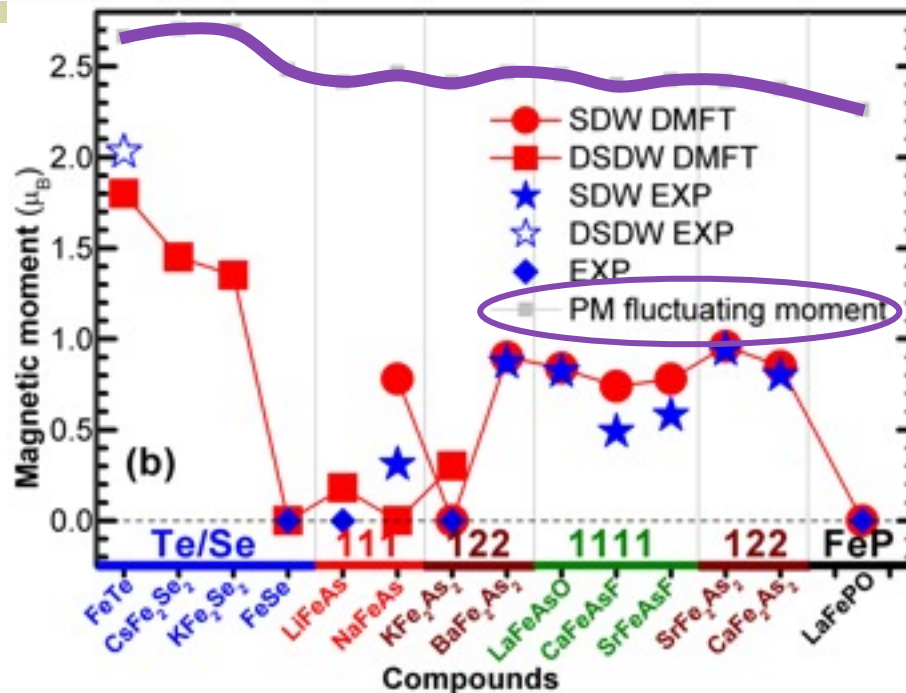
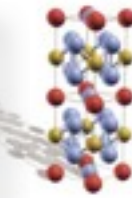


High spin states gain weight with  
Increased correlations,  
fluctuating moment larger

Due to itinerancy, fluctuating moment  
reduced from  $4\mu_B$  to  $\sim 2.5\mu_B$ !



# Fluctuating moment

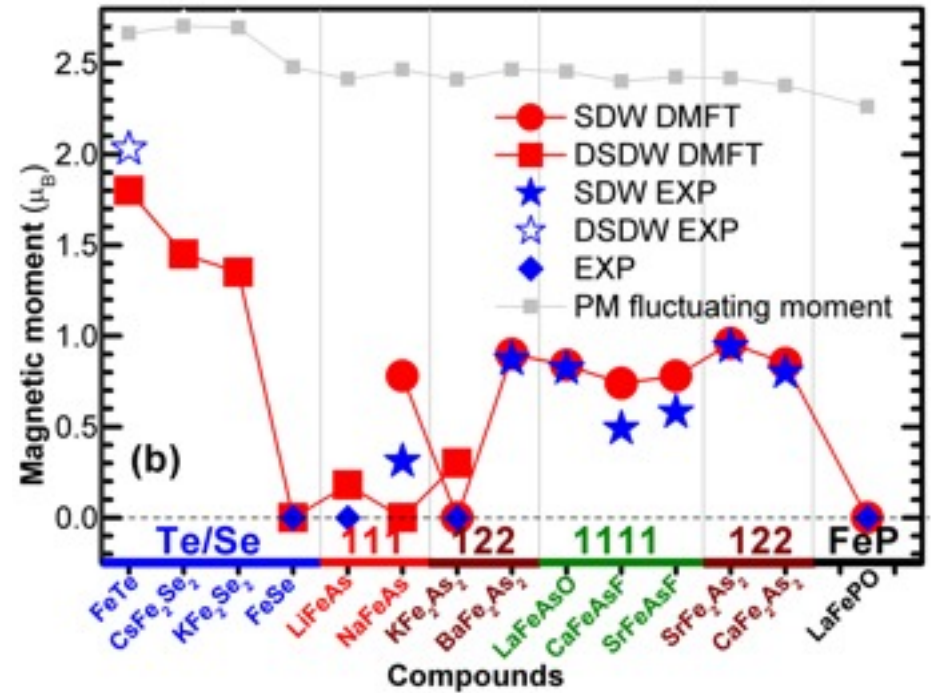
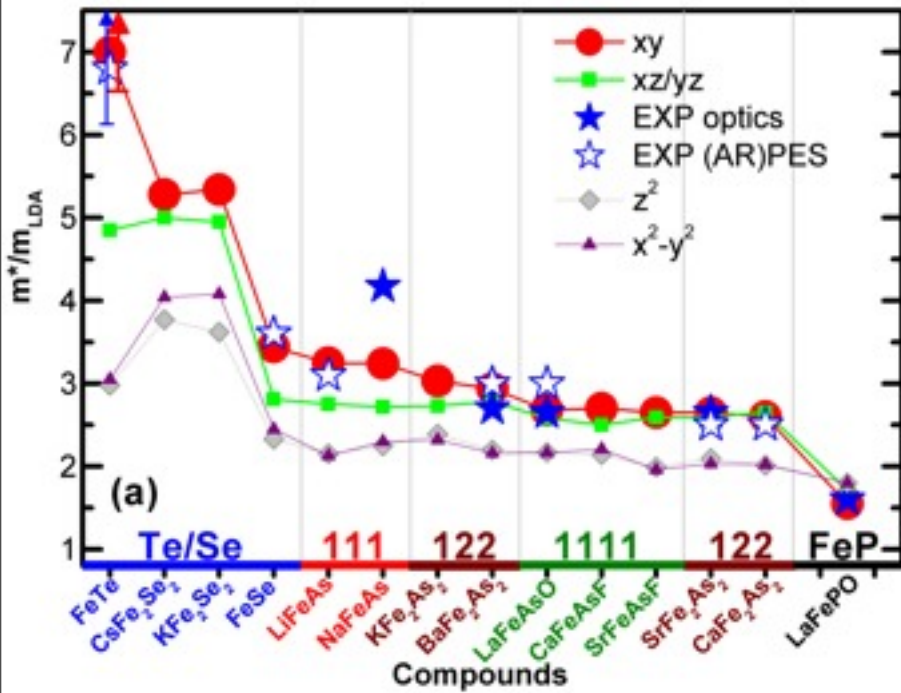


High spin states gain weight with  
Increased correlations,  
fluctuating moment larger

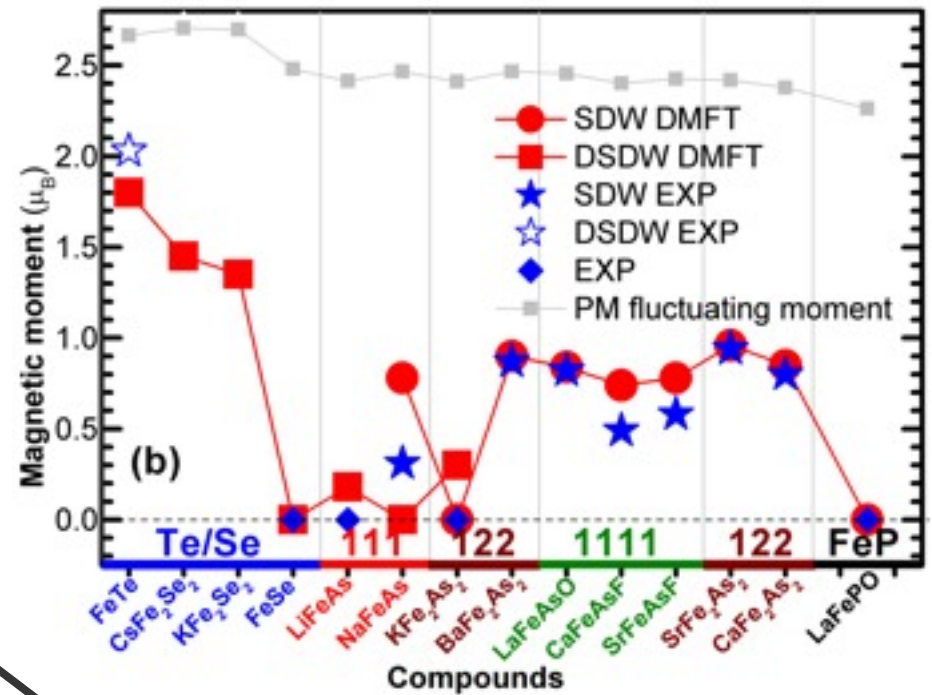
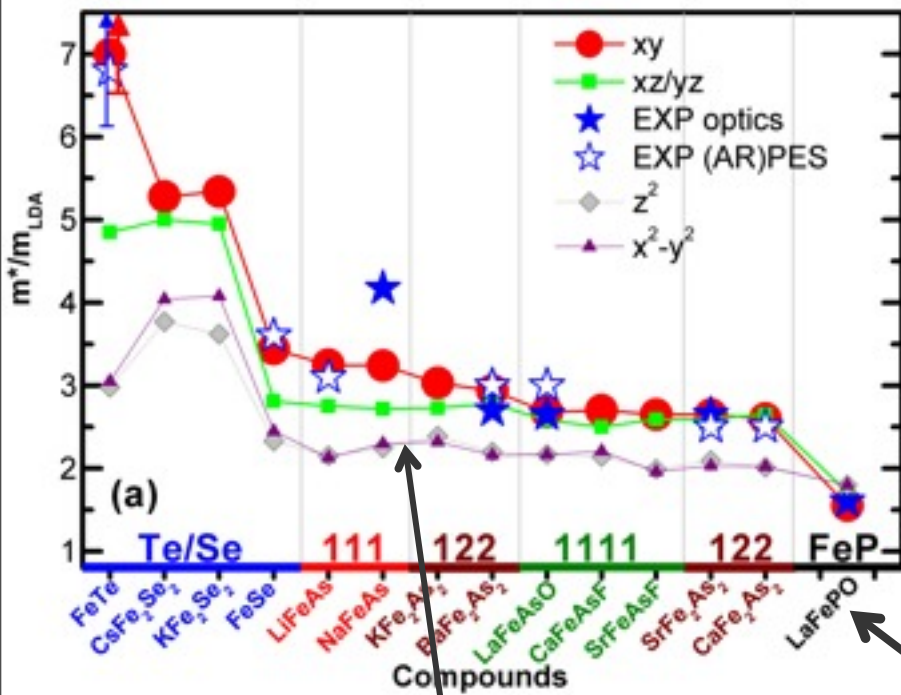
Due to itinerancy, fluctuating moment  
reduced from  $4\mu_B$  to  $\sim 2.5\mu_B$ !

Only small fraction of the fluctuating moment orders!

# Orbital differentiation



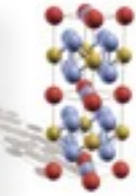
# Orbital differentiation



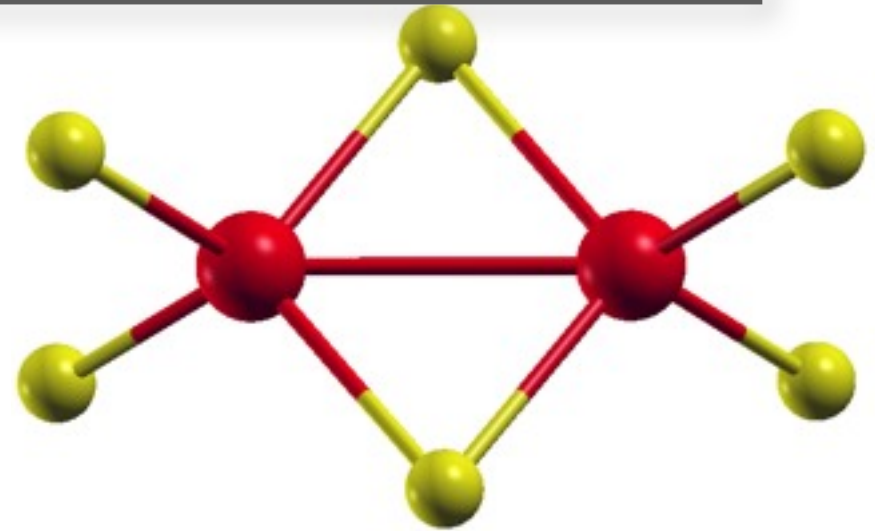
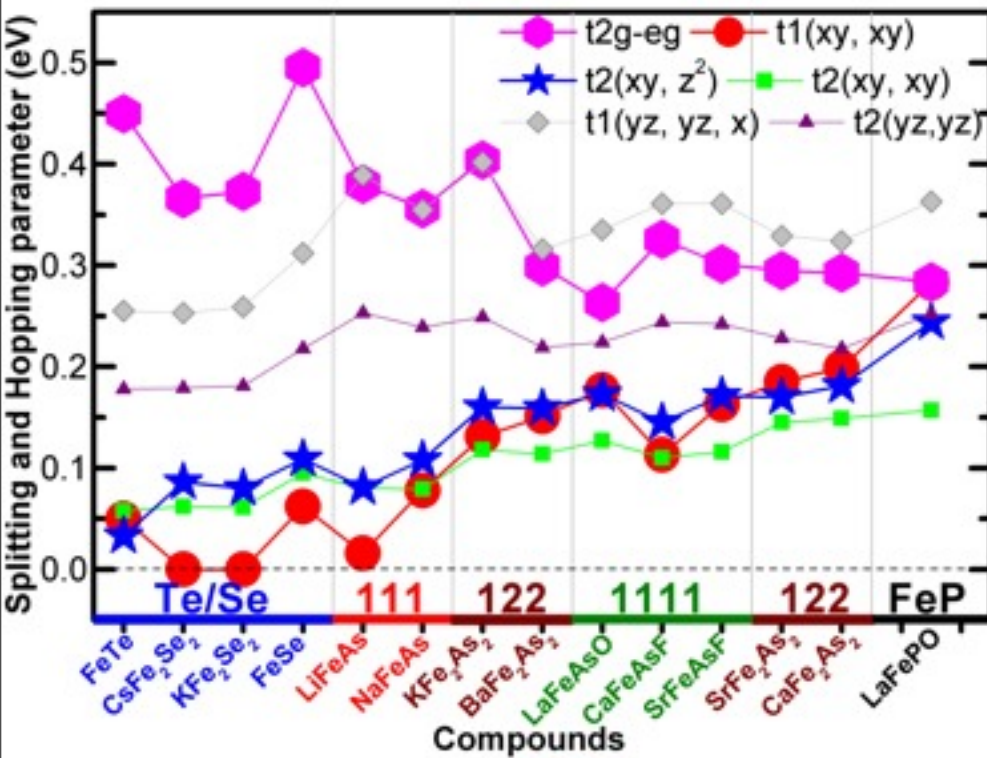
eg orbitals too itinerant to contribute to static magnetic order

Too itinerant to order  
kinetic frustration large

# Kinetic frustration

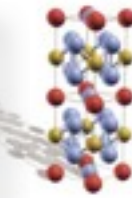


Effective low energy hoppings

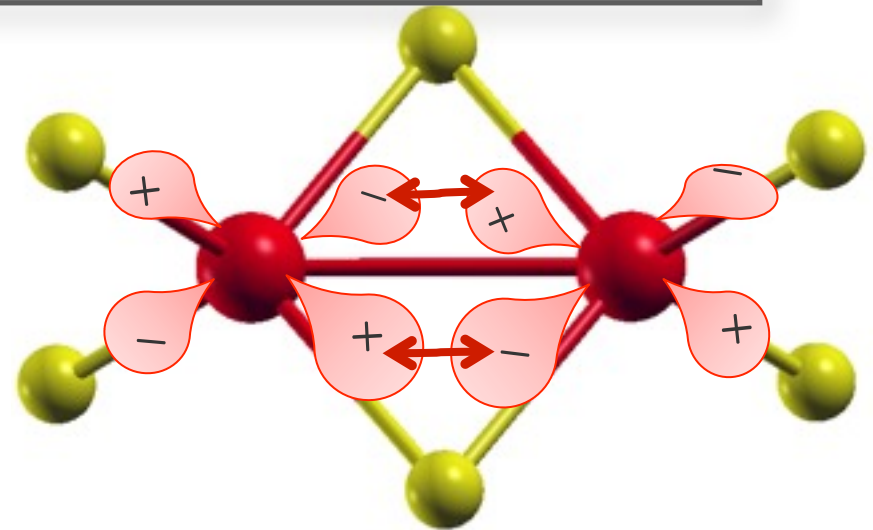
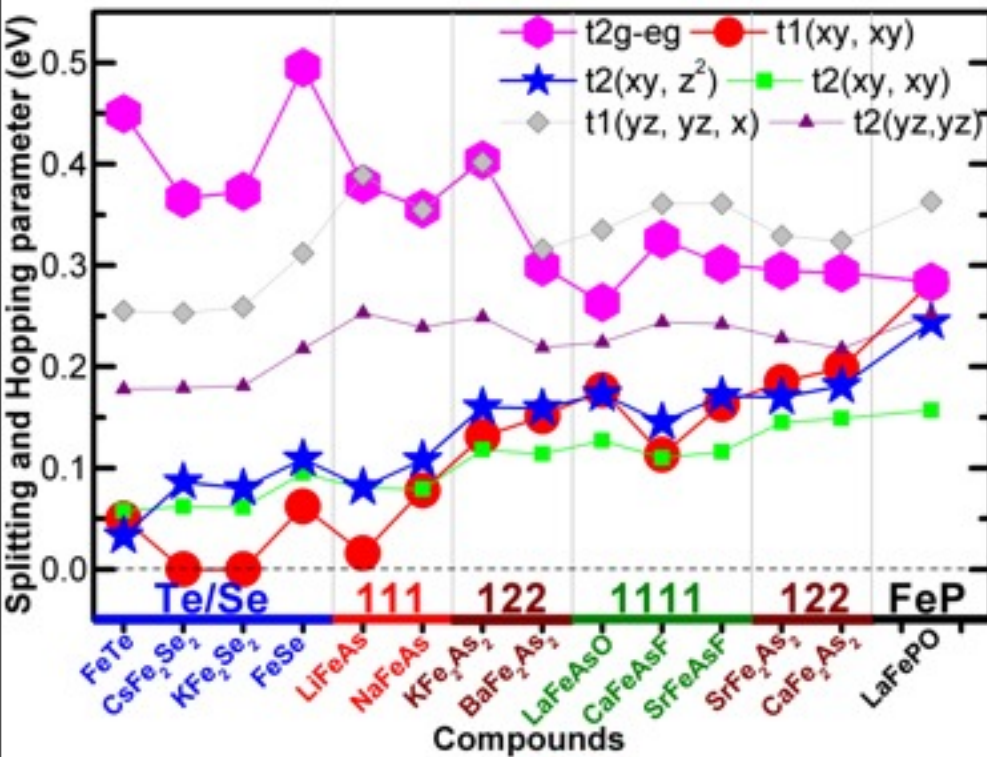




# Kinetic frustration

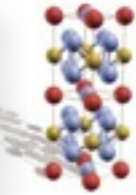


Effective low energy hoppings

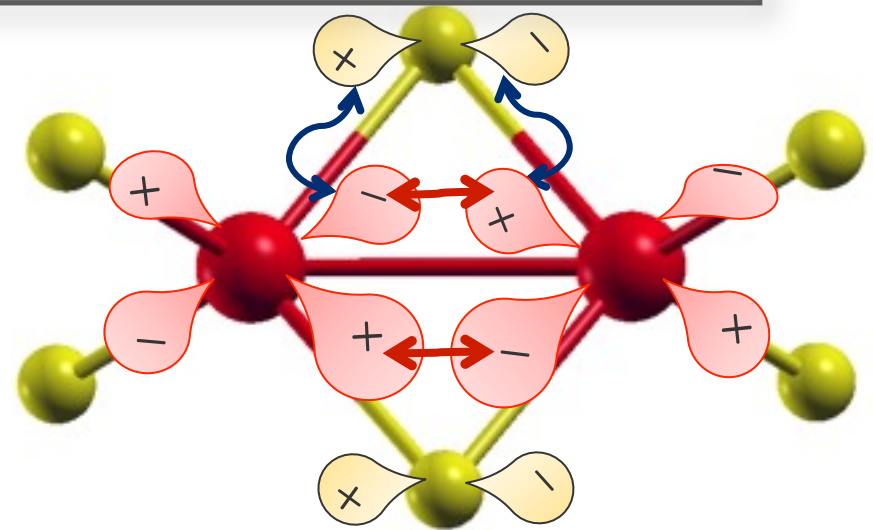
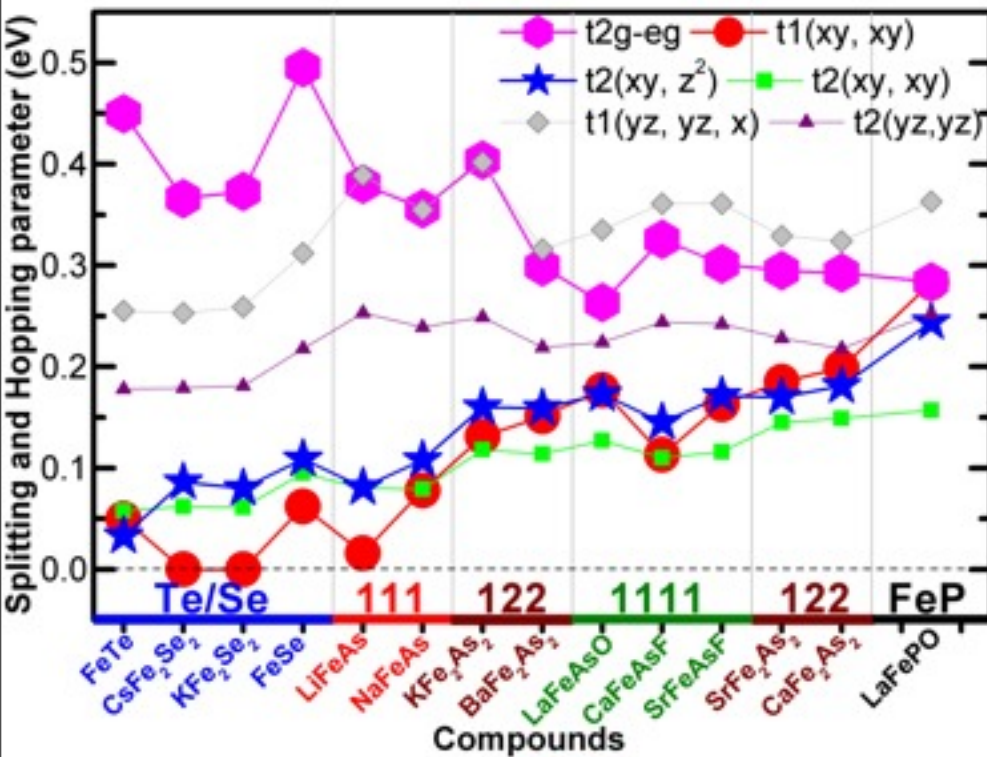


$$t_{xy,xy}^{direct} < 0$$

# Kinetic frustration



Effective low energy hoppings

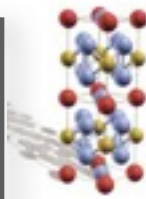


$$t_{xy,xy}^{direct} < 0$$

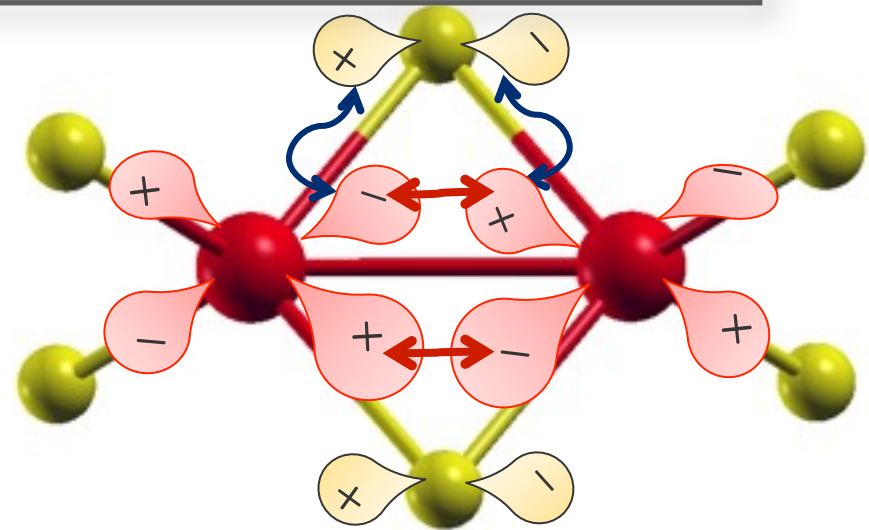
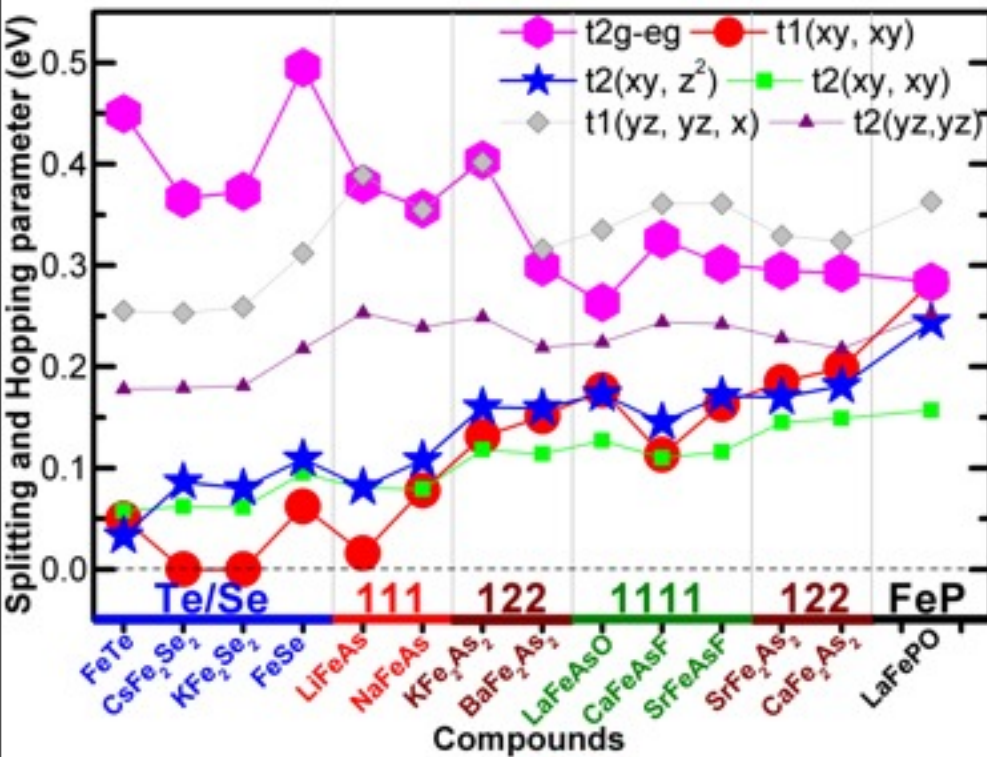
$$t_{xy,xy}^{As} > 0$$



# Kinetic frustration



Effective low energy hoppings



$$t_{xy,xy}^{direct} < 0$$

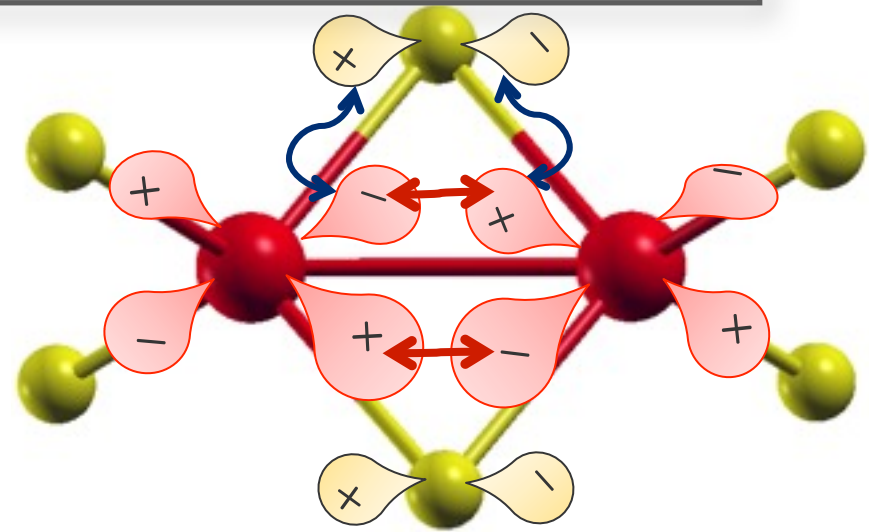
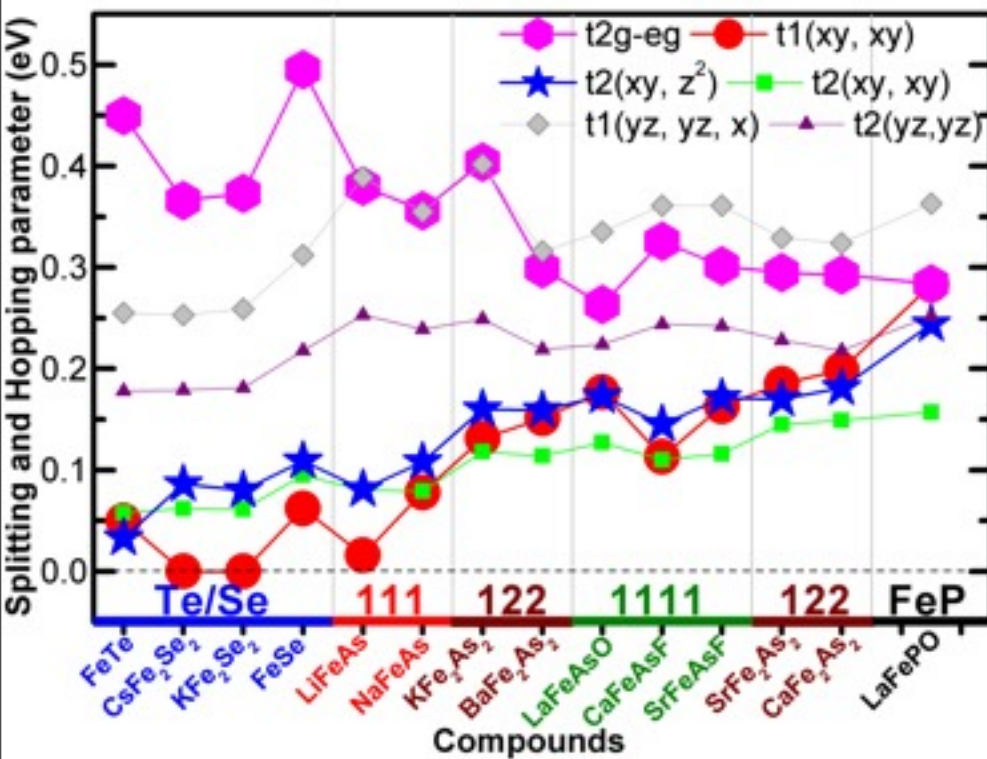
$$t_{xy,xy}^{As} > 0$$

$t^{As}$  usually larger, but not when pnictogen height large!

# Kinetic frustration



Effective low energy hoppings



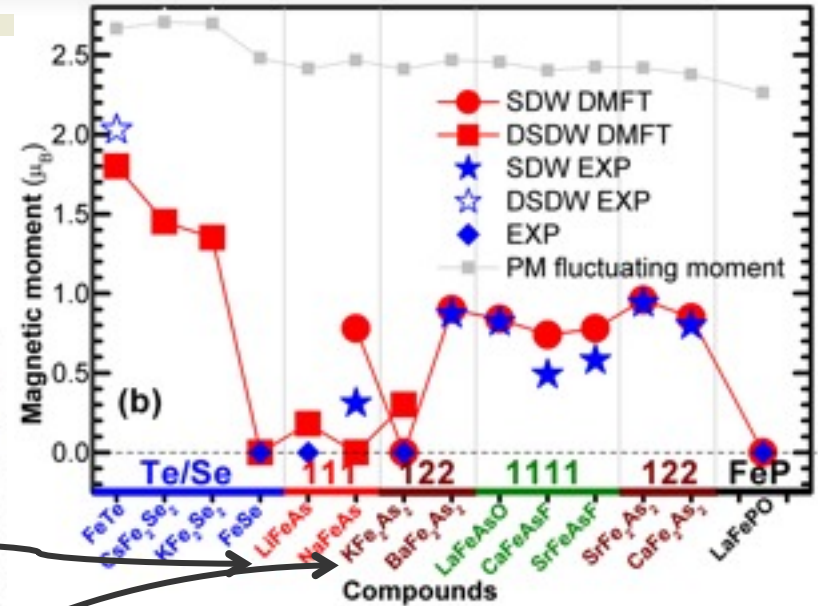
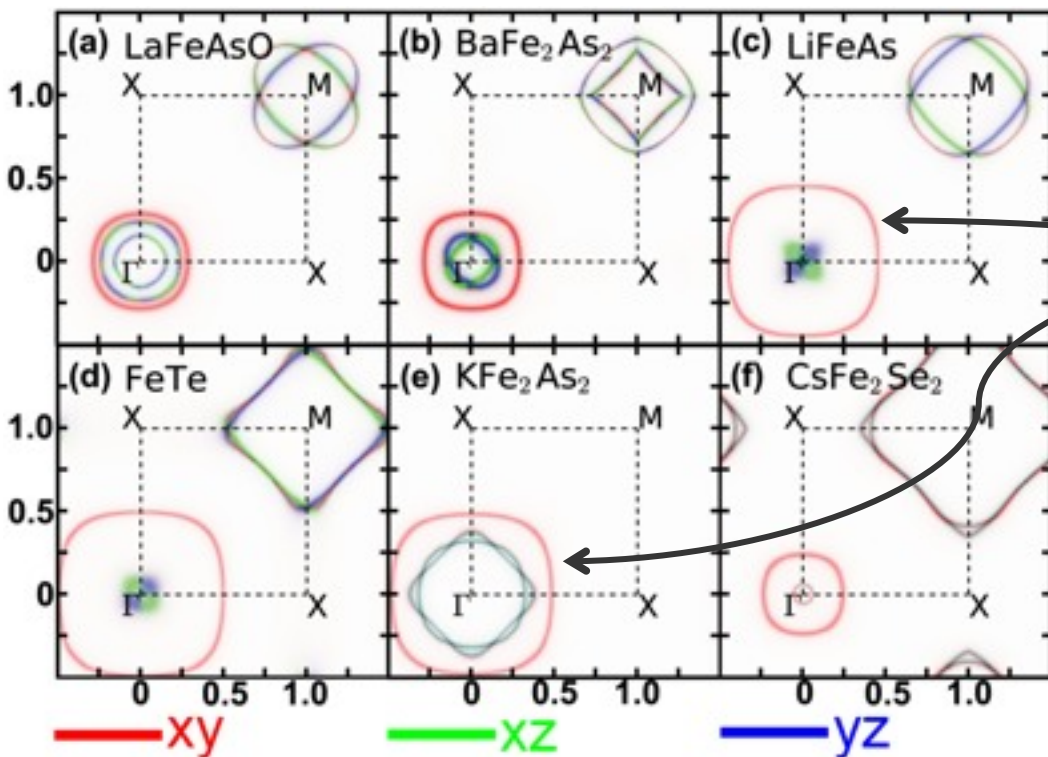
$$t_{xy,xy}^{direct} < 0$$

$$t_{xy,xy}^{As} > 0$$

$t^{As}$  usually larger, but not when pnictogen height large!

Destructive interference leads to kinetic frustration!

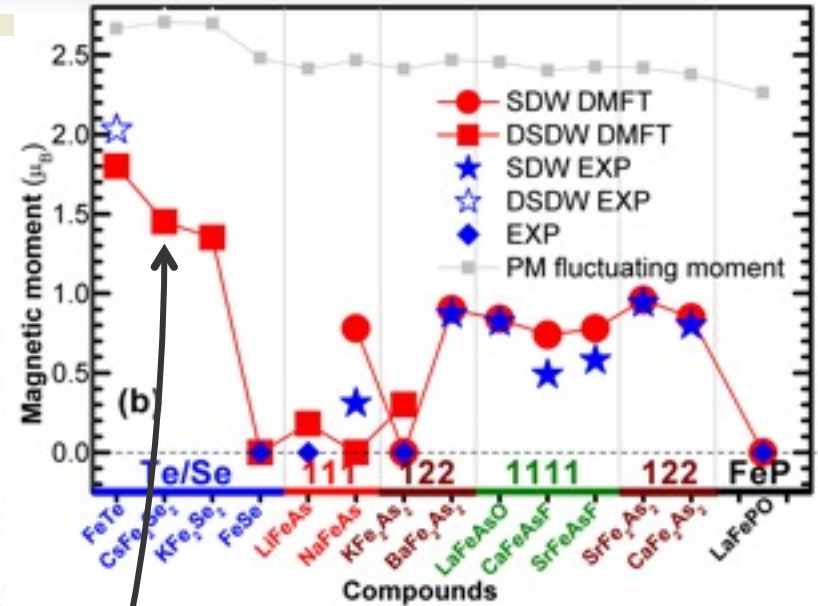
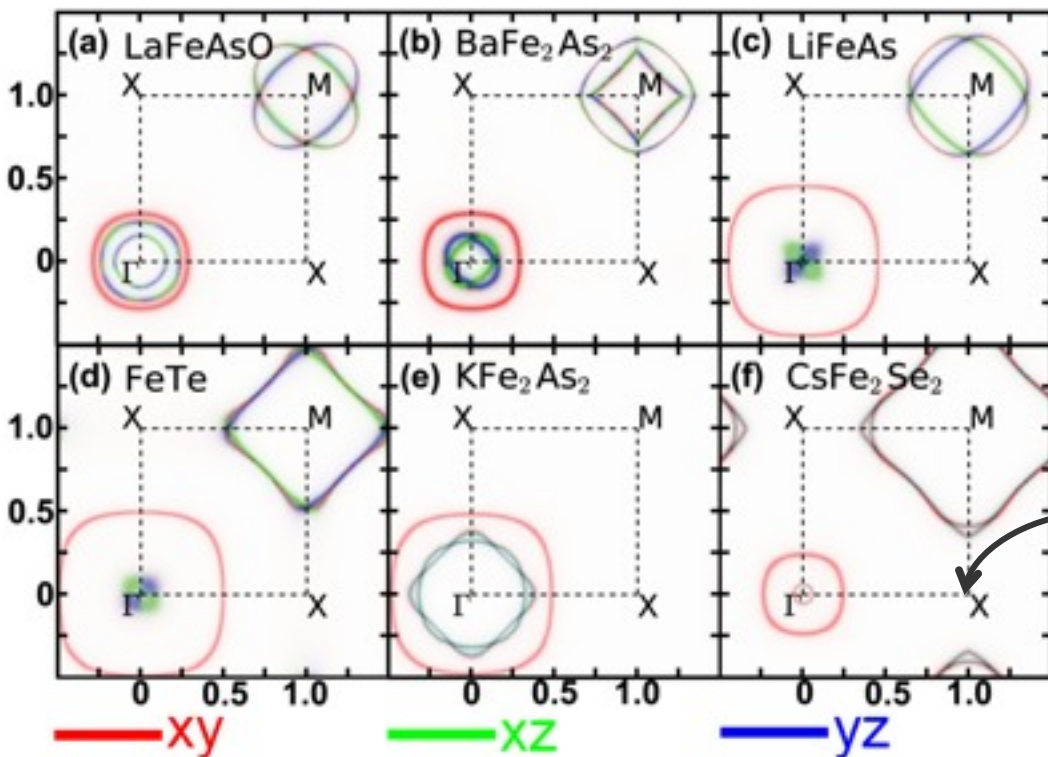
# Fermi surface



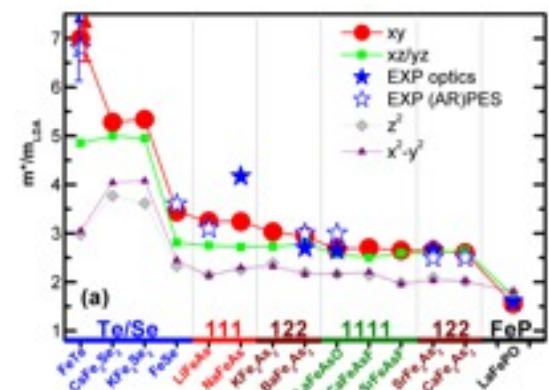
Fermi surface horrible for ordering!



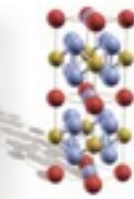
# Fermi surface



No need for nesting in very Correlated compound CsFe<sub>2</sub>Se<sub>2</sub>!



# Optics by DFT+DMFT ( $\text{BaFe}_2\text{As}_2$ )



Z. Yin, KH, G Kotliar, Nature Physics (2011).

Good agreement with experiment!

Correct plasma  $\omega_p$ :

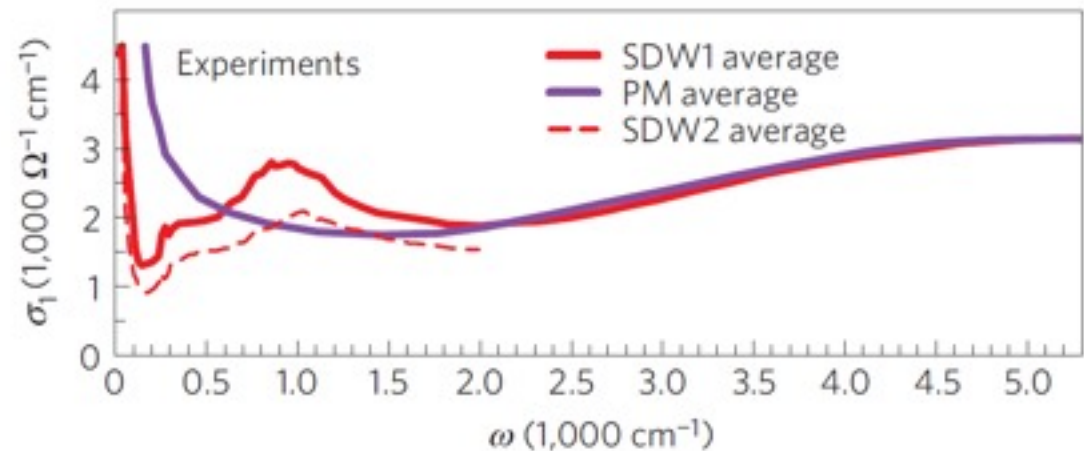
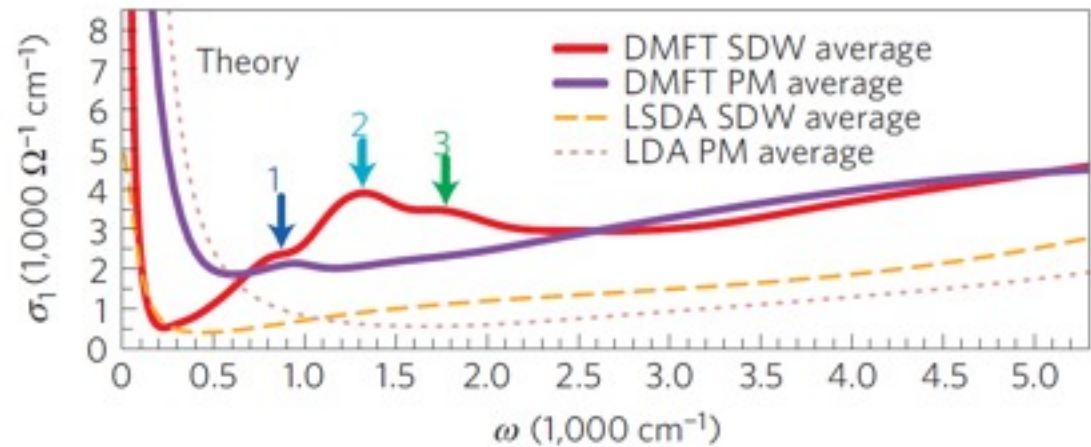
DMFT  $\sim 1.6\text{eV}$

Exp  $\sim 1.6\text{eV}$

LDA  $\sim 2.6\text{eV}$

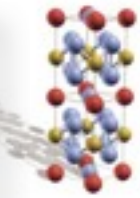
3 peak structure beyond SDW gap

Good agreement at high energy



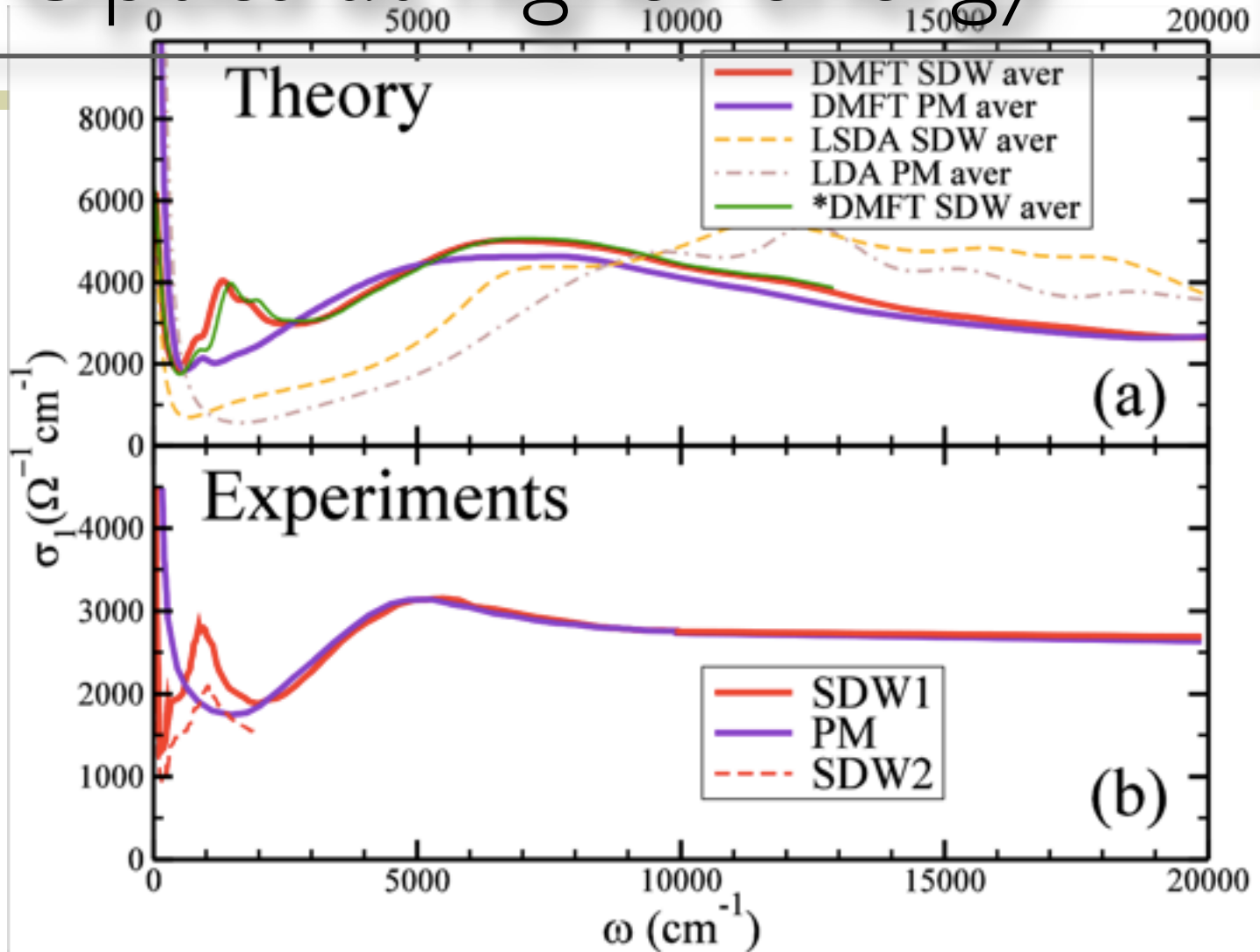
Experiment: W. Z. Hu, et al, PRL 101, 257005 (2008).  
Nakajima, M. et al. Phys. Rev. B 81, 104528 (2010).

# Optics at higher energy

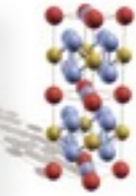


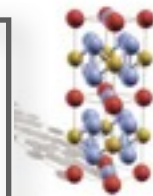


# Optics at higher energy

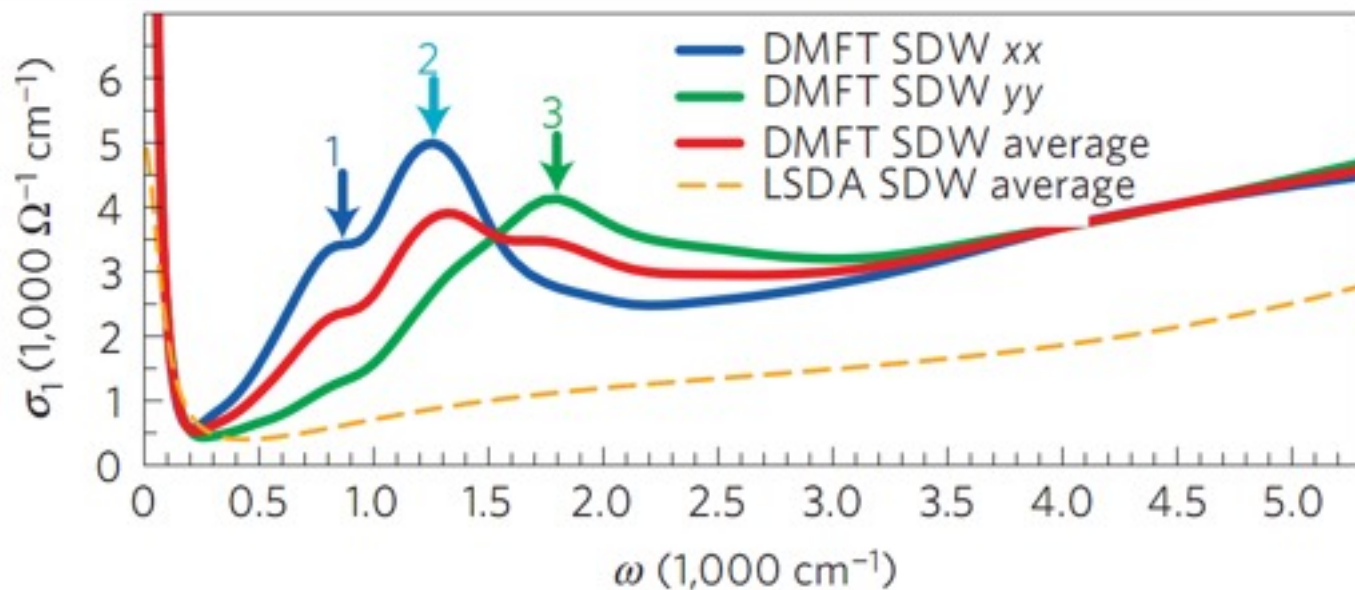
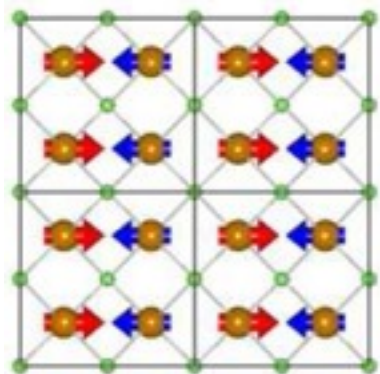


Very good agreement between LDA+DMFT and experiment  
In the entire frequency range.

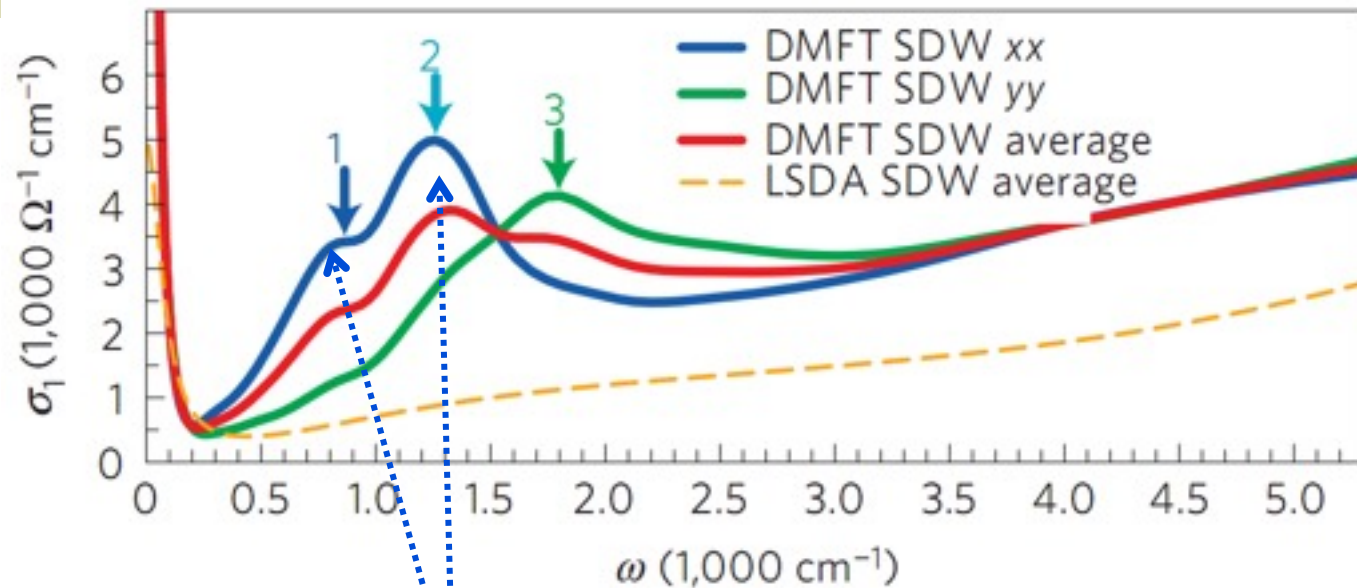
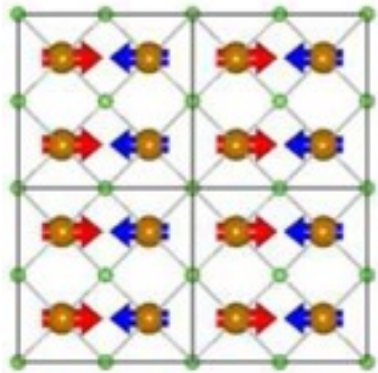
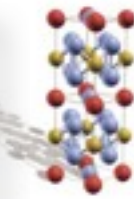




# Optical anisotropy predicted

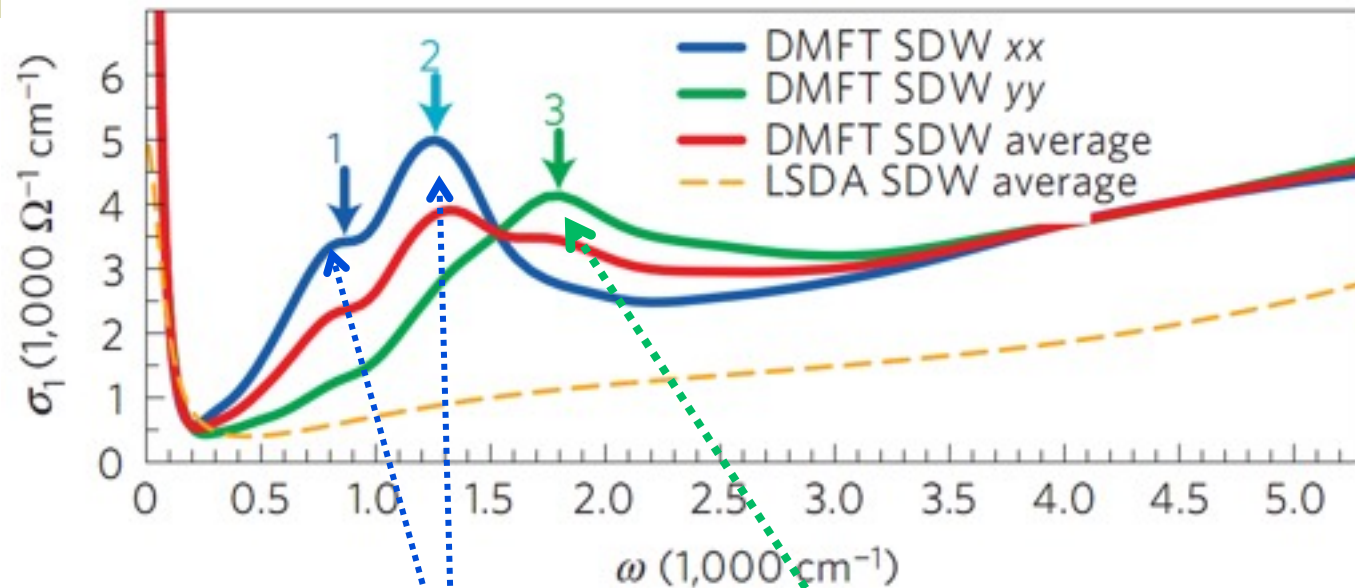
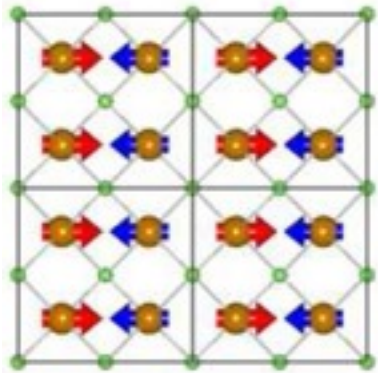
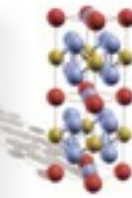


# Optical anisotropy predicted



First two excitations  
only in AFM x-direction

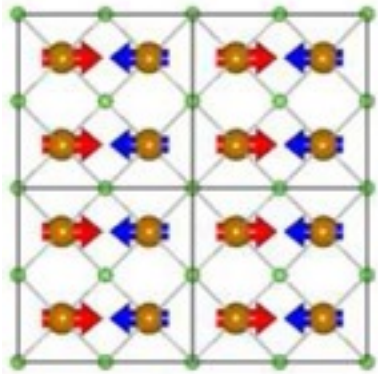
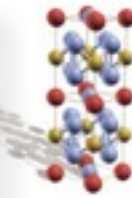
# Optical anisotropy predicted



First two excitations  
only in AFM x-direction

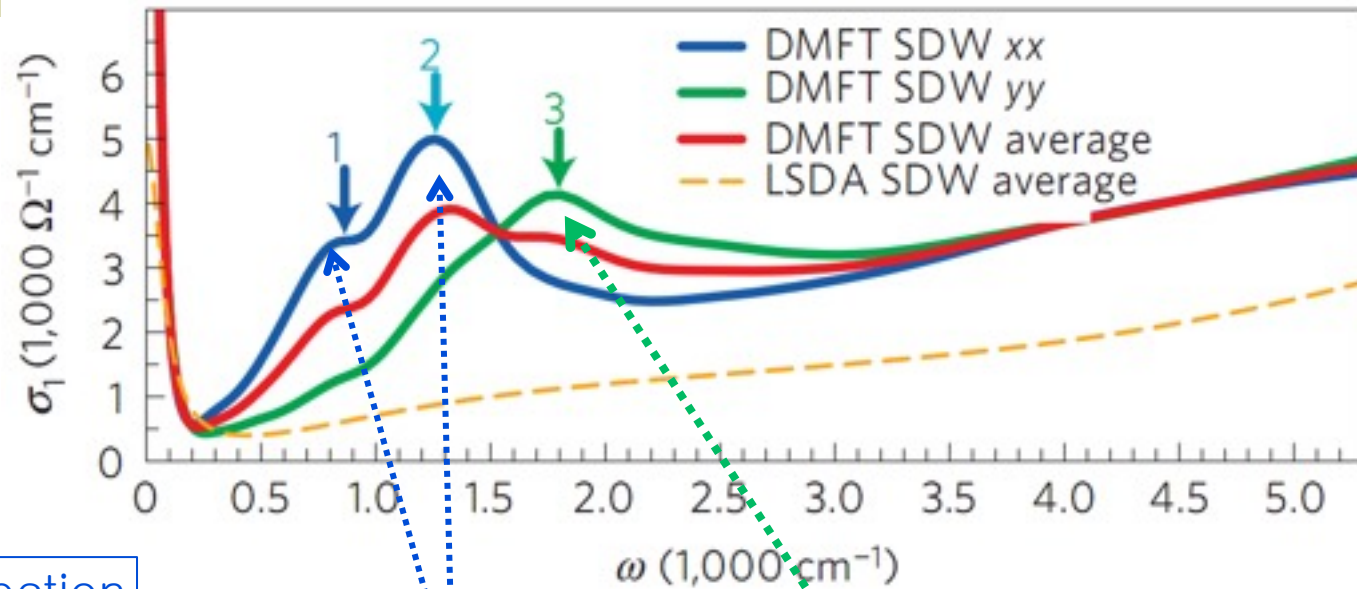
Larger SDW gap in  
FM y-direction

# Optical anisotropy predicted



highway in AFM (x) direction

Pauli blocking  
hinders  
electron hopping  
in FM(y) direction



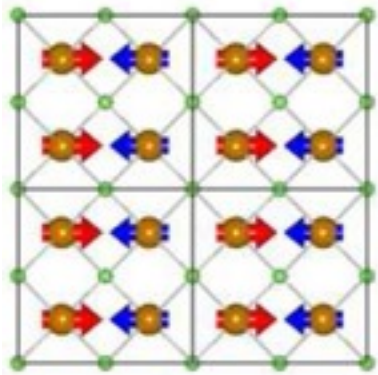
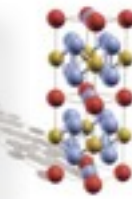
First two excitations  
only in AFM x-direction

Larger SDW gap in  
FM y-direction

Z. P. Yin, KH, G. Kotliar, Nature Physics 2011.

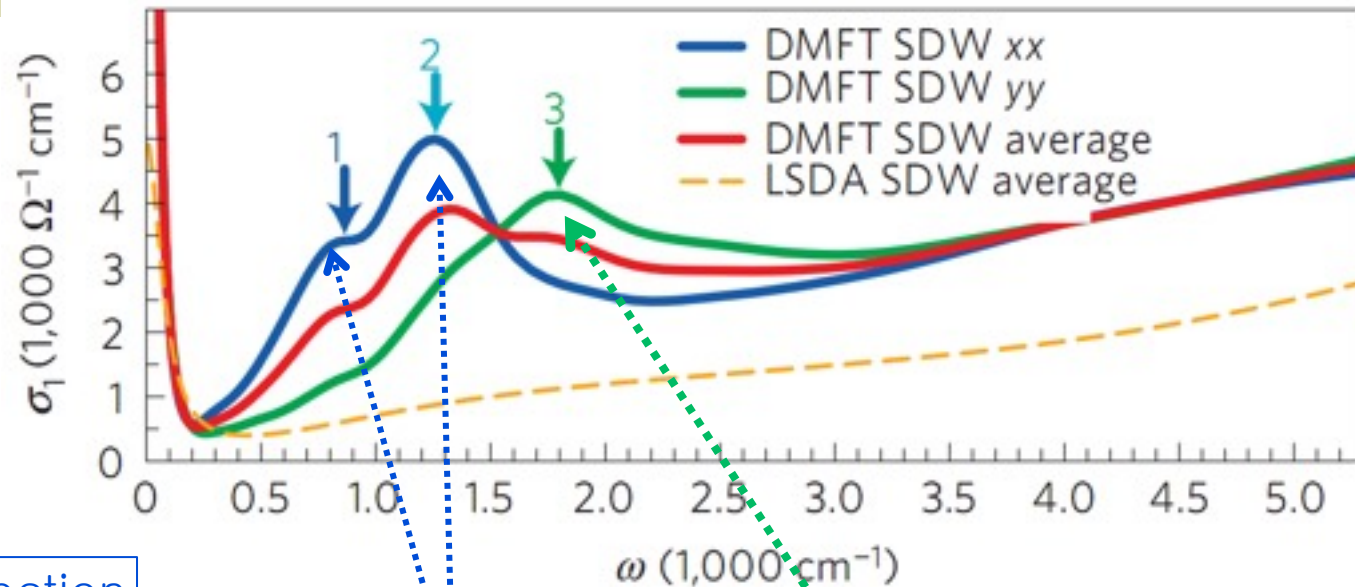


# Optical anisotropy predicted



highway in AFM (x) direction

Pauli blocking  
hinders  
electron hopping  
in FM(y) direction



First two excitations  
only in AFM x-direction

Larger SDW gap in  
FM y-direction

QP want to decrease their kinetic energy  
by choosing "best path"  $\rightarrow$  orbital  
polarization

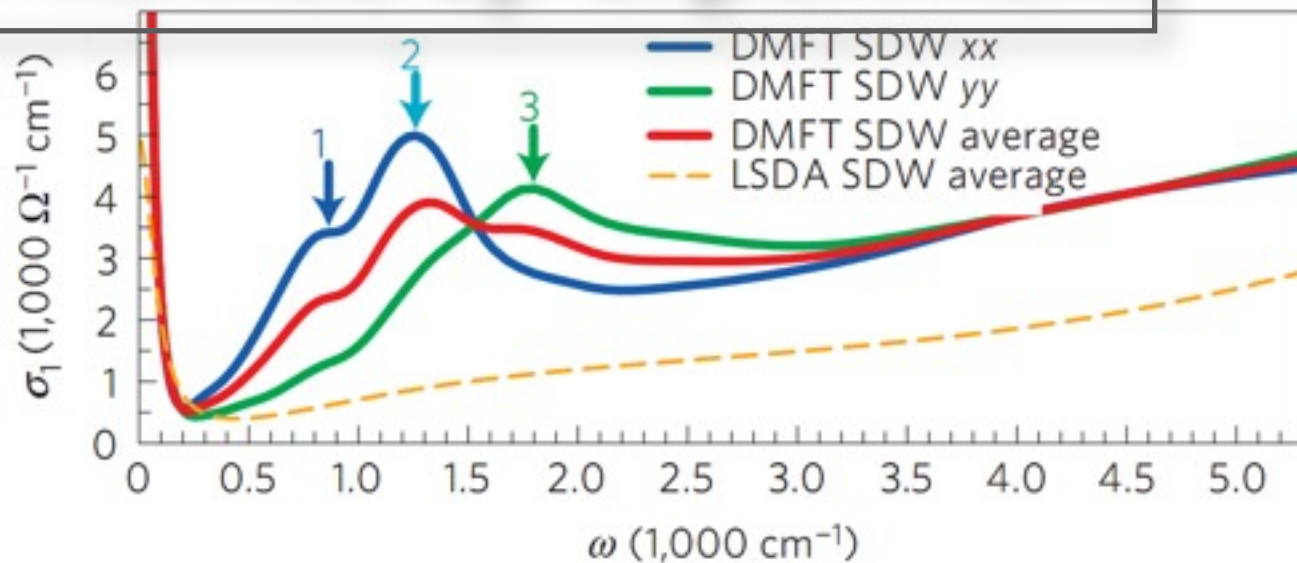
Z. P. Yin, KH, G. Kotliar, Nature Physics 2011.



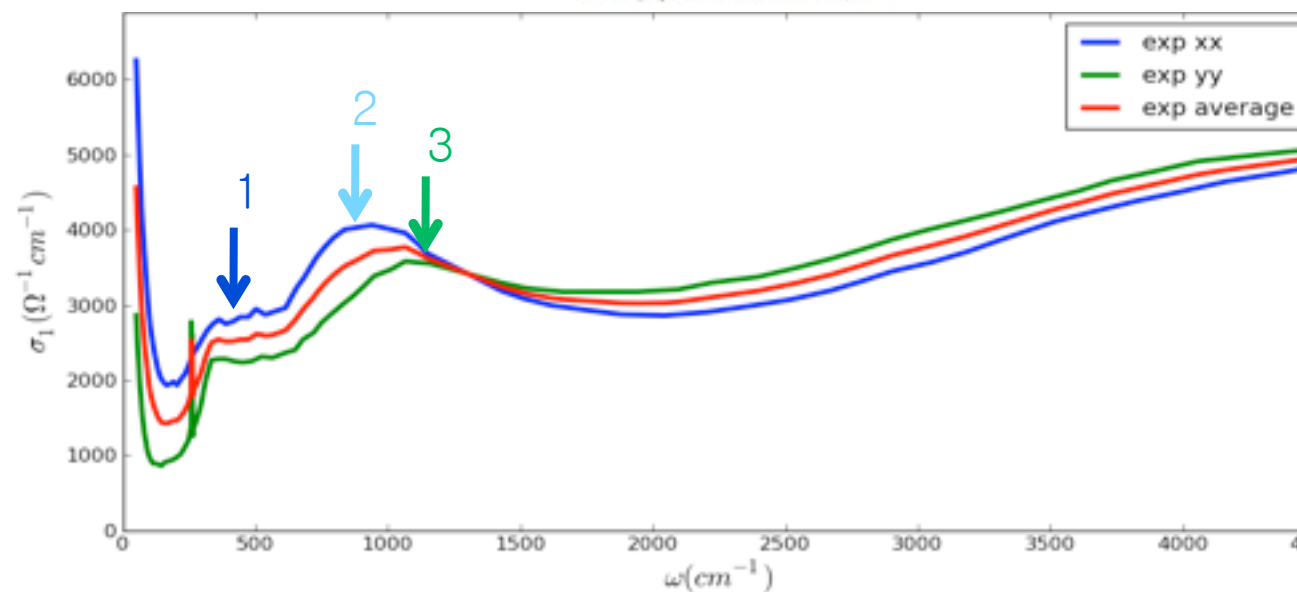
# Prediction verified by experiment



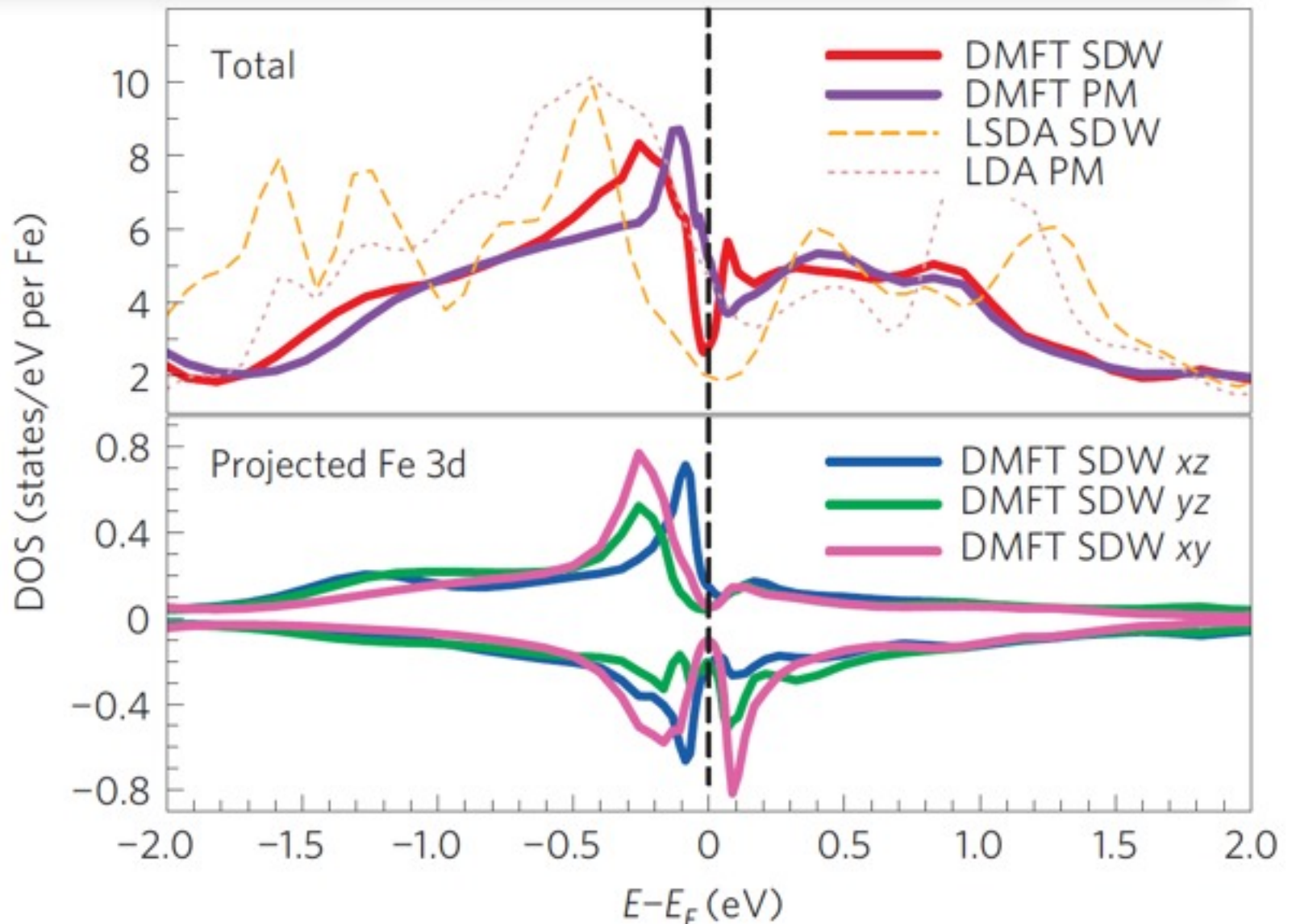
DMFT prediction:  
Nature Physics 7, 294 (2011)



Experiment:  
M. Nakajima, ..., S Uchida,  
PNAS 108, 12238 (2011).



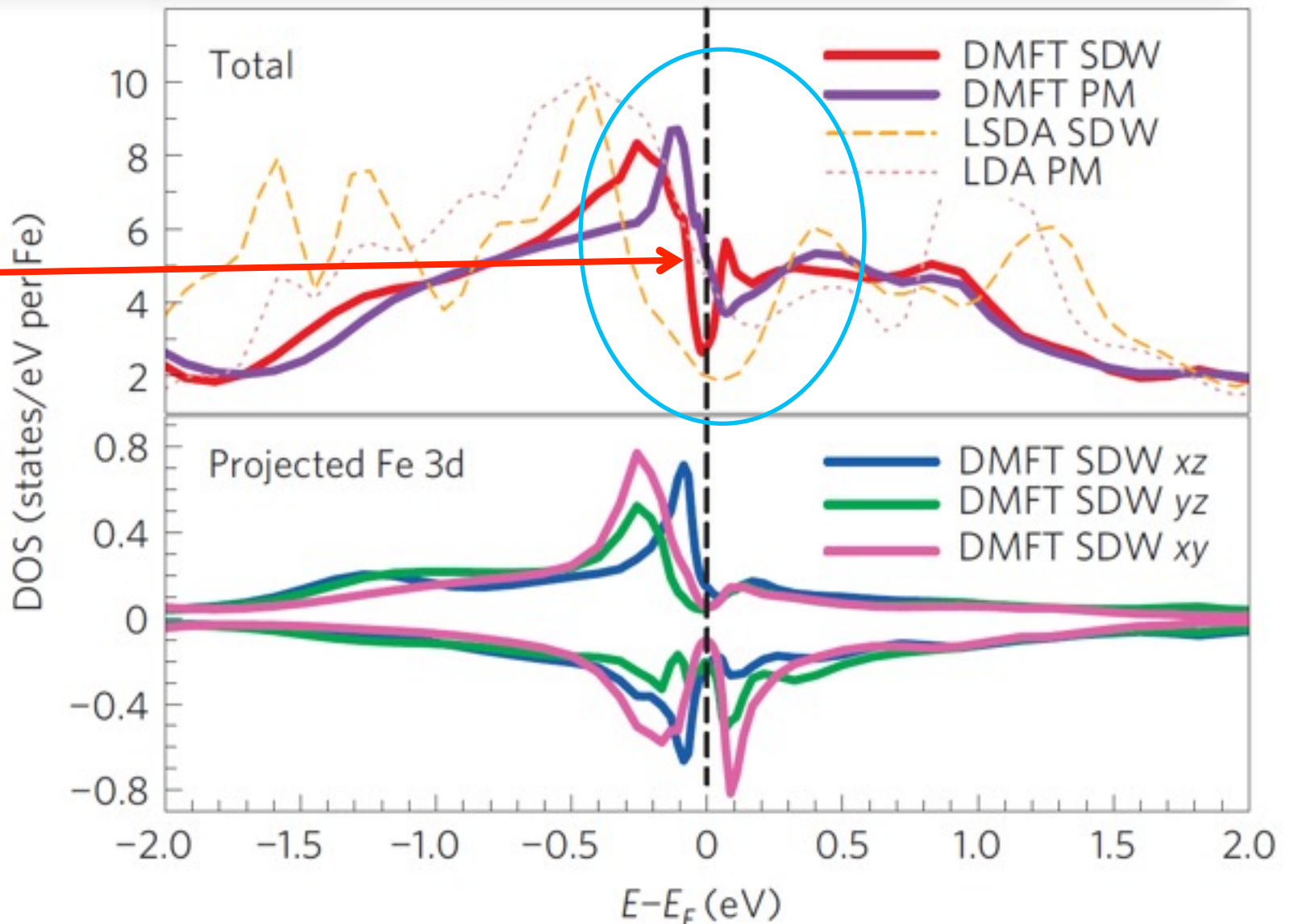
# Density of states



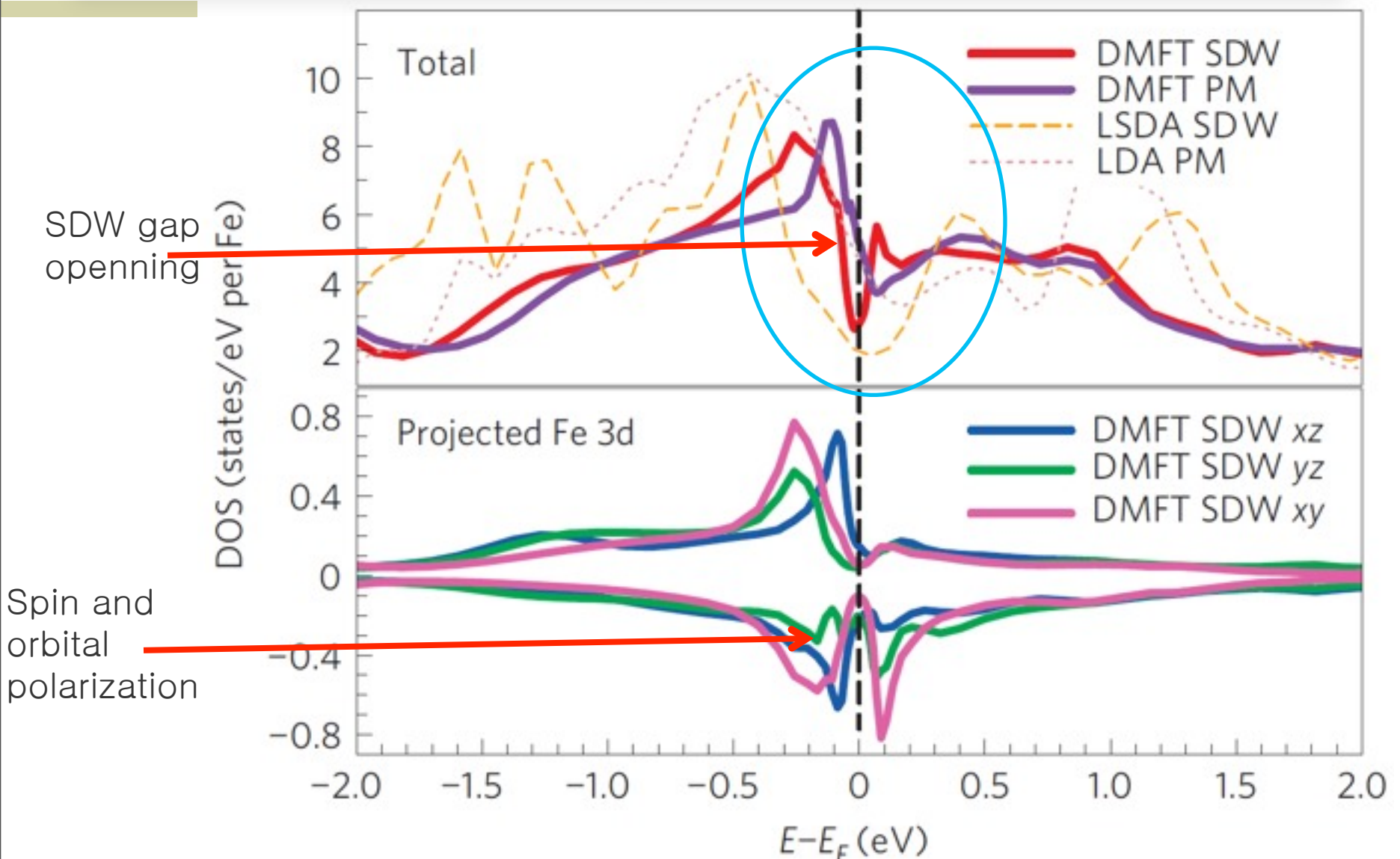
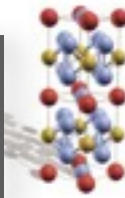
# Density of states



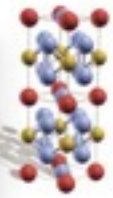
SDW gap  
opening



# Density of states

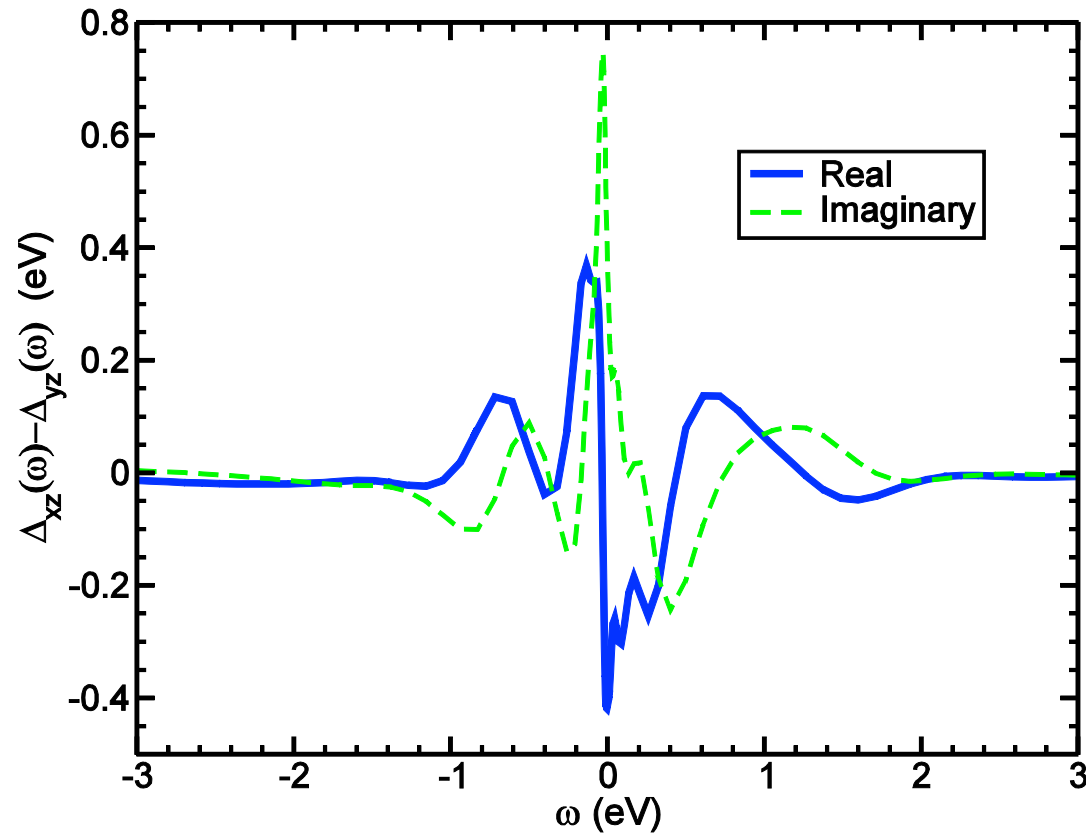
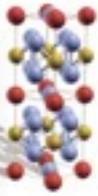


# Orbital polarization-low energy phenomena

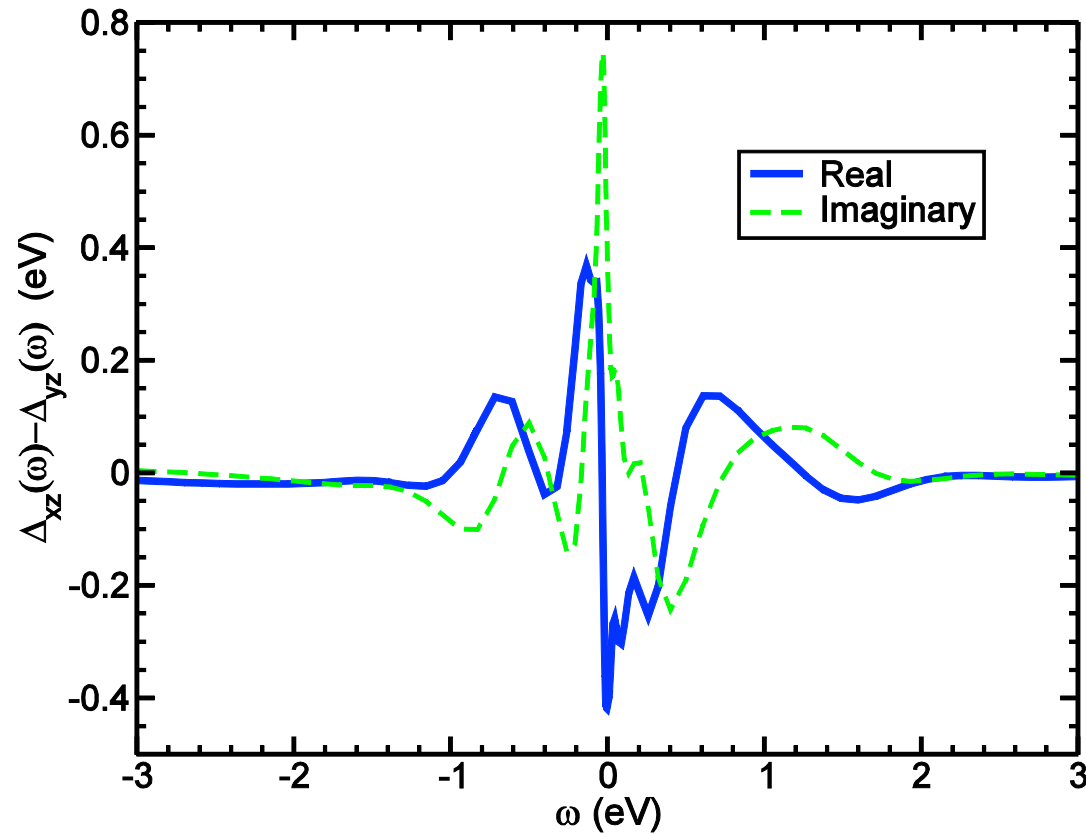
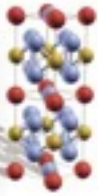




# Orbital polarization-low energy phenomena

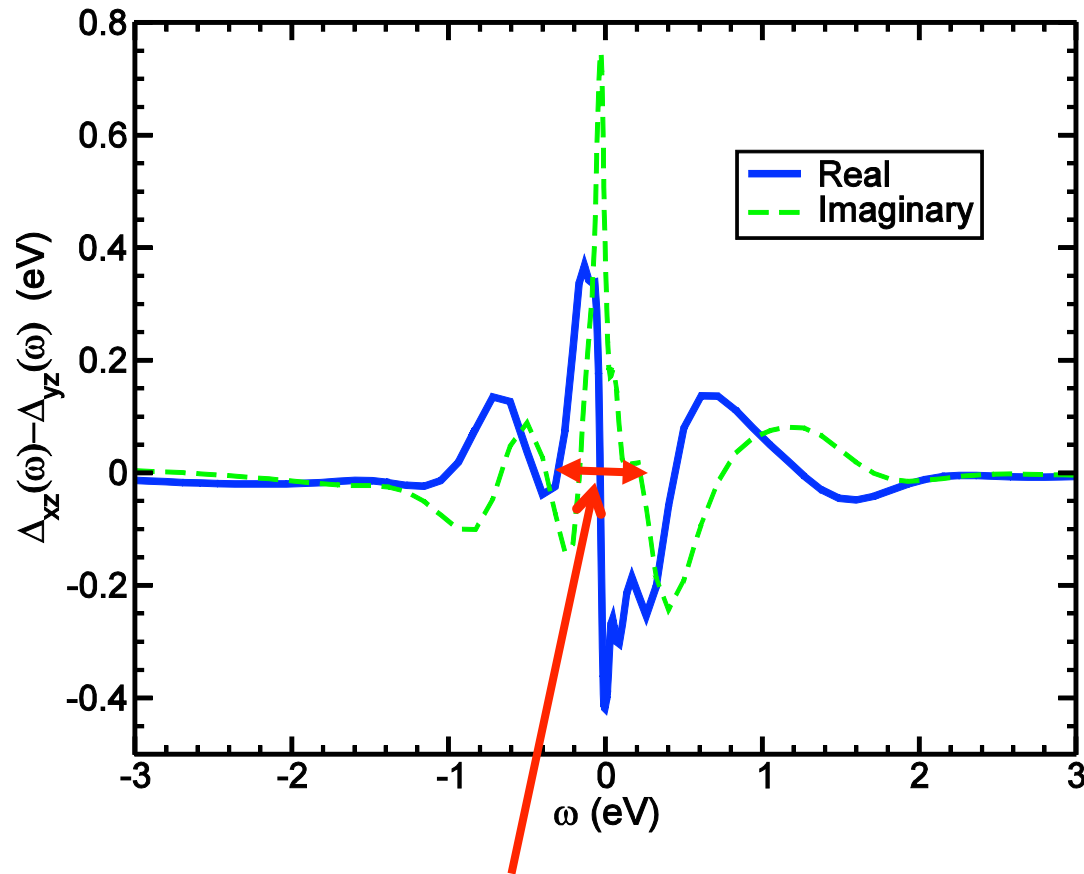
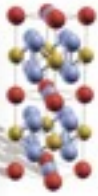


# Orbital polarization-low energy phenomena



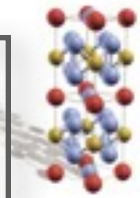
Orbital polarization large at low energy

# Orbital polarization-low energy phenomena

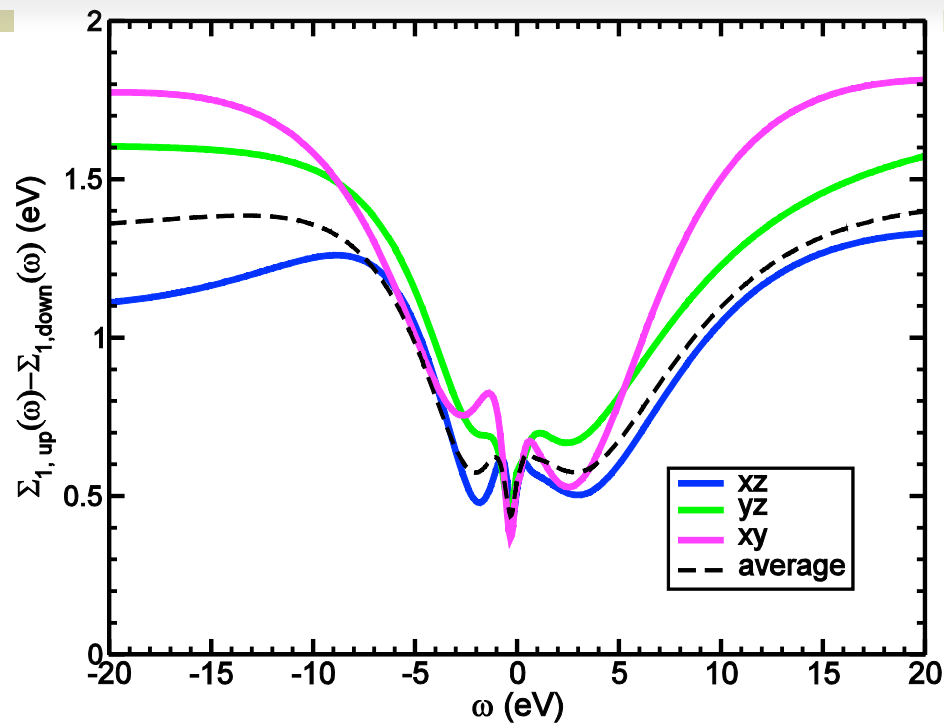
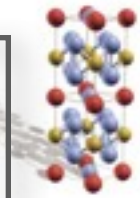


Orbital polarization large at low energy  
(within 300 meV)

# Spin polarization-high energy phenomena

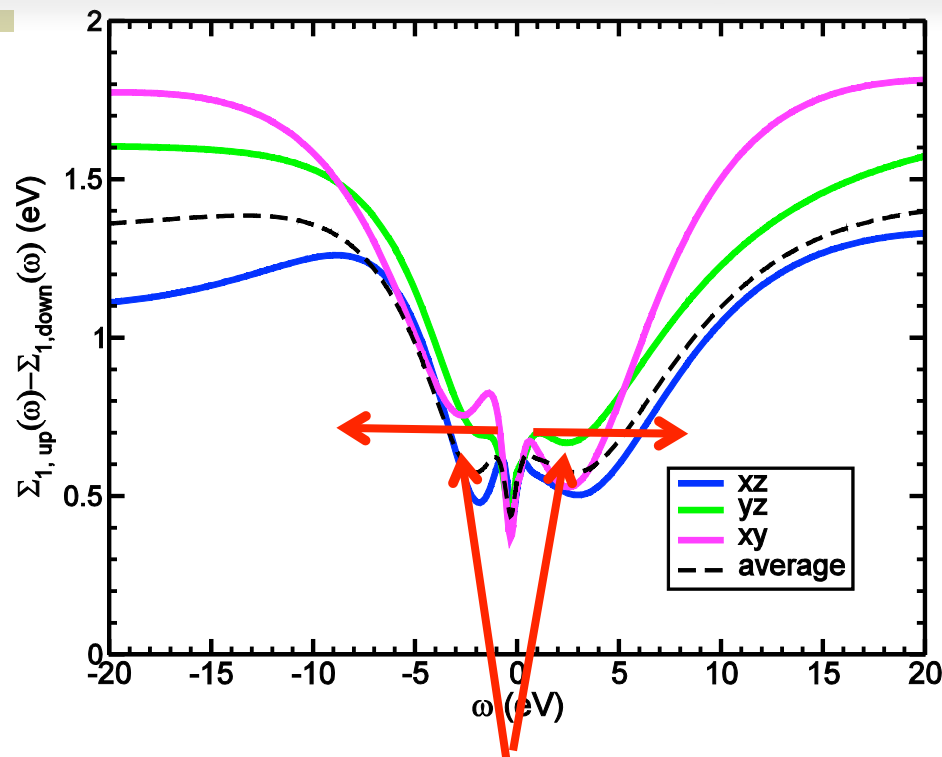
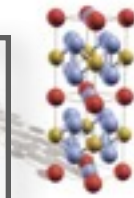


# Spin polarization-high energy phenomena



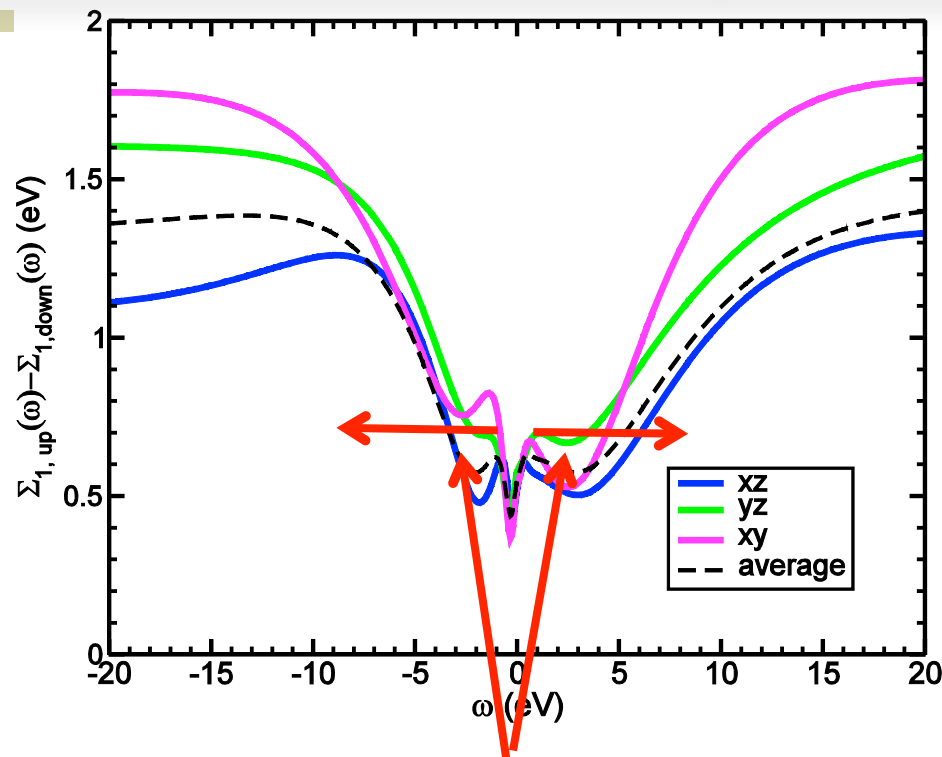
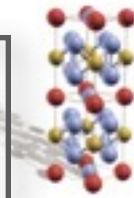


# Spin polarization-high energy phenomena



Spin polarization large at high energy

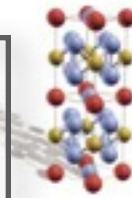
# Spin polarization-high energy phenomena



Spin polarization large at high energy

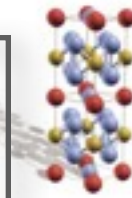
Spin moment lives at high energy with orbital polarization at low energy

# Dynamical structure factor



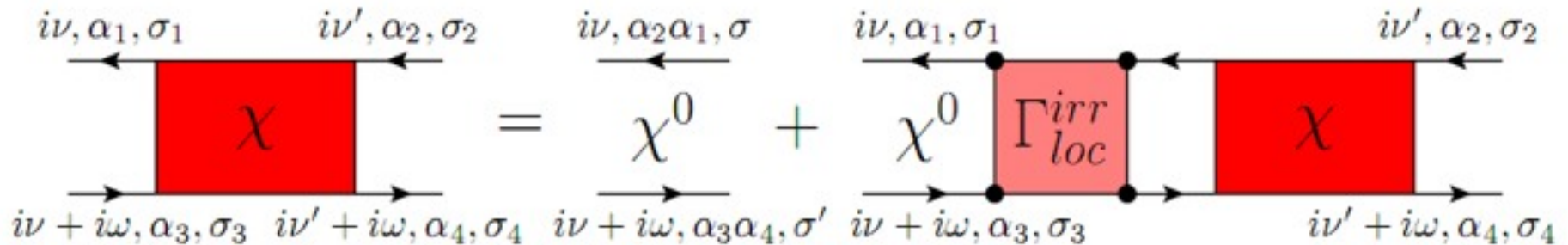
$$S(\mathbf{q}, \omega) = \frac{\chi''(\mathbf{q}, \omega)}{1 - e^{-\hbar\omega/k_B T}}$$

# Dynamical structure factor

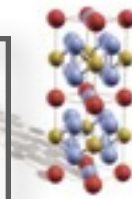


$$S(\mathbf{q}, \omega) = \frac{\chi''(\mathbf{q}, \omega)}{1 - e^{-\hbar\omega/k_B T}}$$

Computed from the two particle response functions  
using the fact that the irreducible vertex is local.

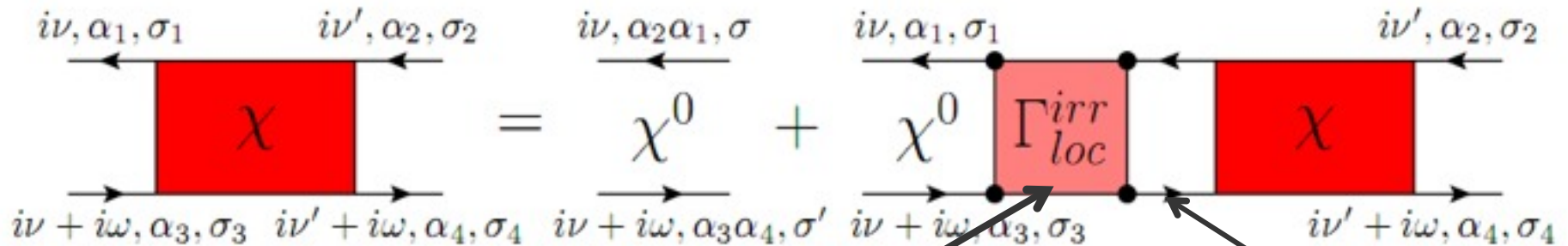


# Dynamical structure factor



$$S(\mathbf{q}, \omega) = \frac{\chi''(\mathbf{q}, \omega)}{1 - e^{-\hbar\omega/k_B T}}$$

Computed from the two particle response functions using the fact that the irreducible vertex is local.



The two particle irreducible vertex function of the impurity

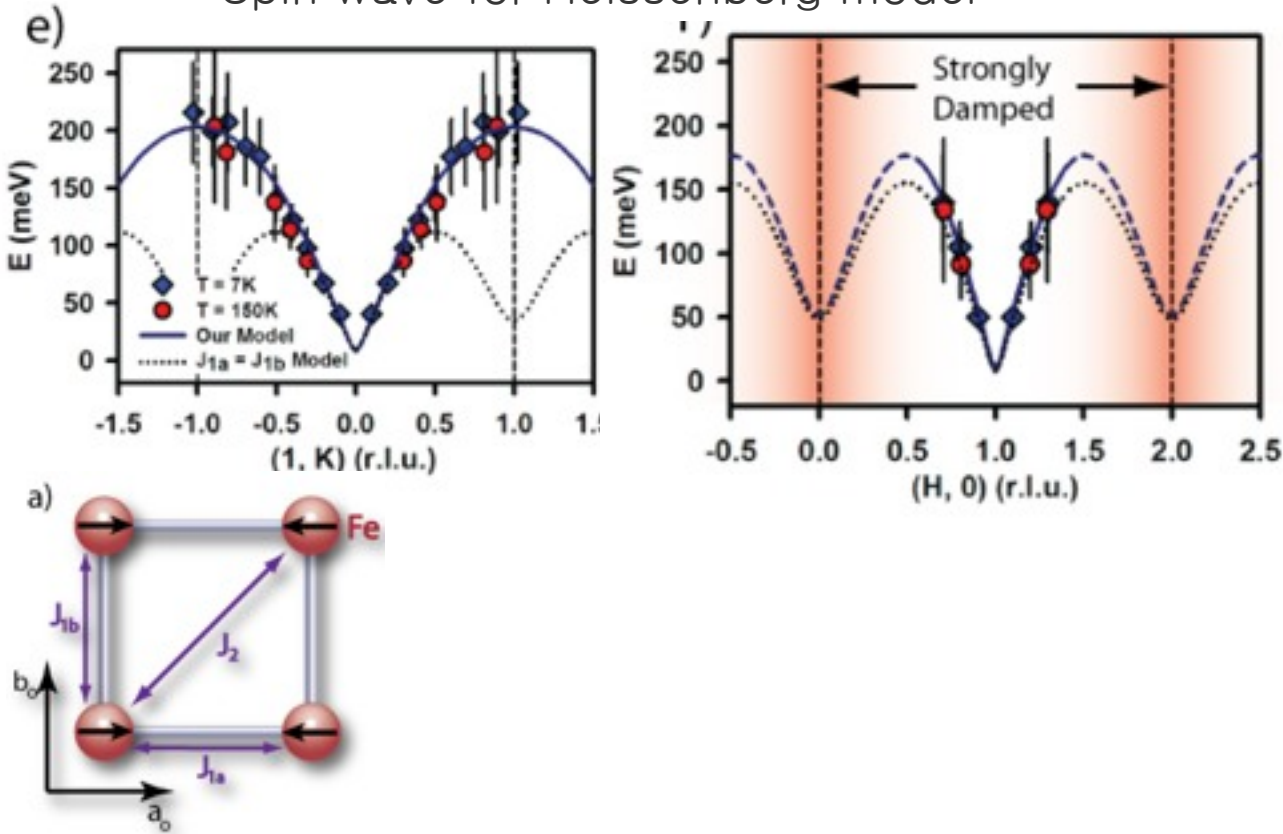
The LDA+DMFT self-consistent lattice Green's function



# Dynamical structure factor



Spin wave for Heisenberg model

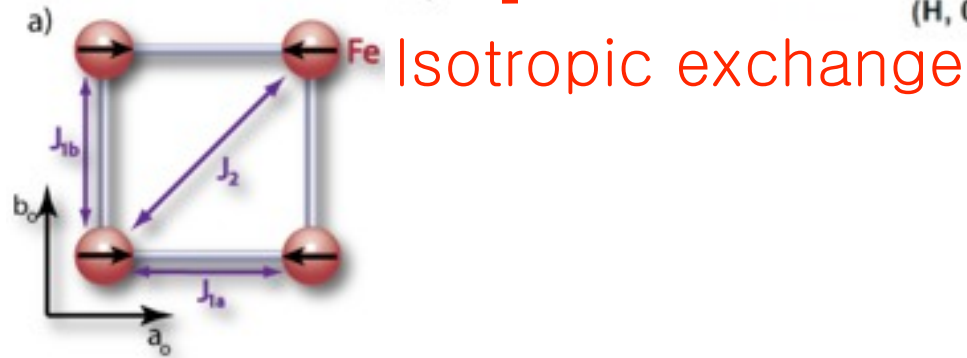
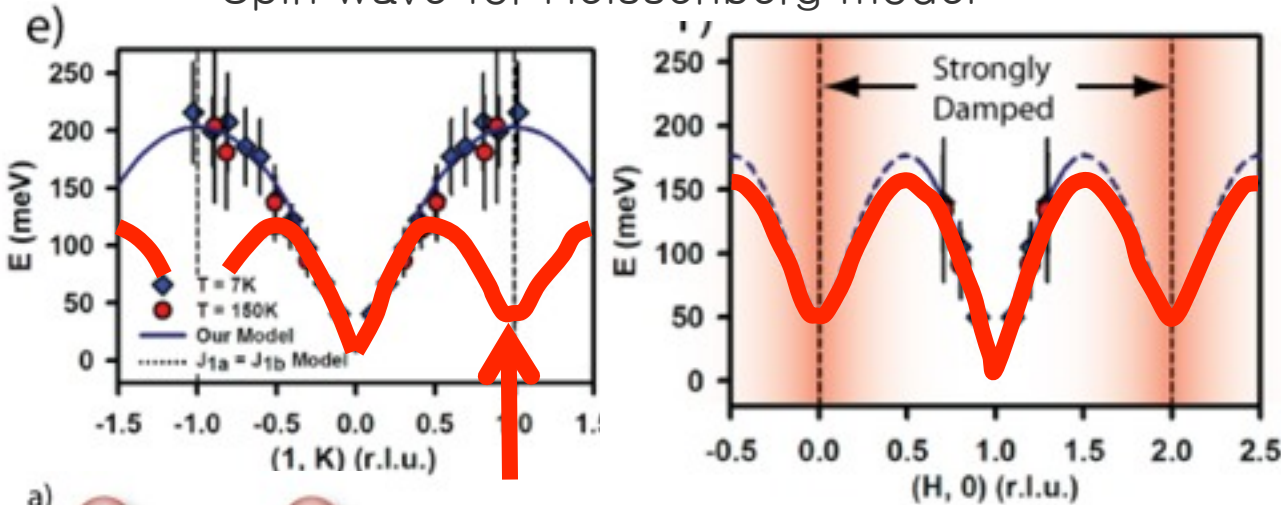


Leland W. Harriger, Pengcheng Dai et al., arXiv:1011.3771

# Dynamical structure factor



Spin wave for Heisenberg model

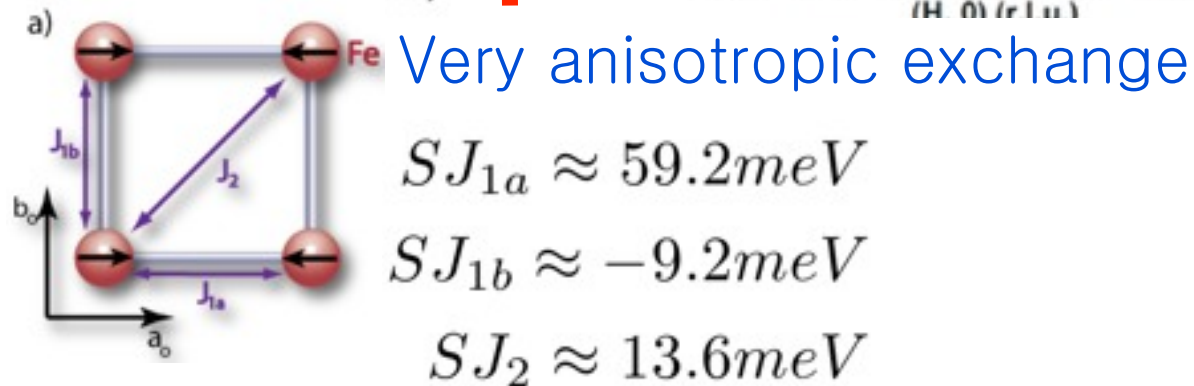
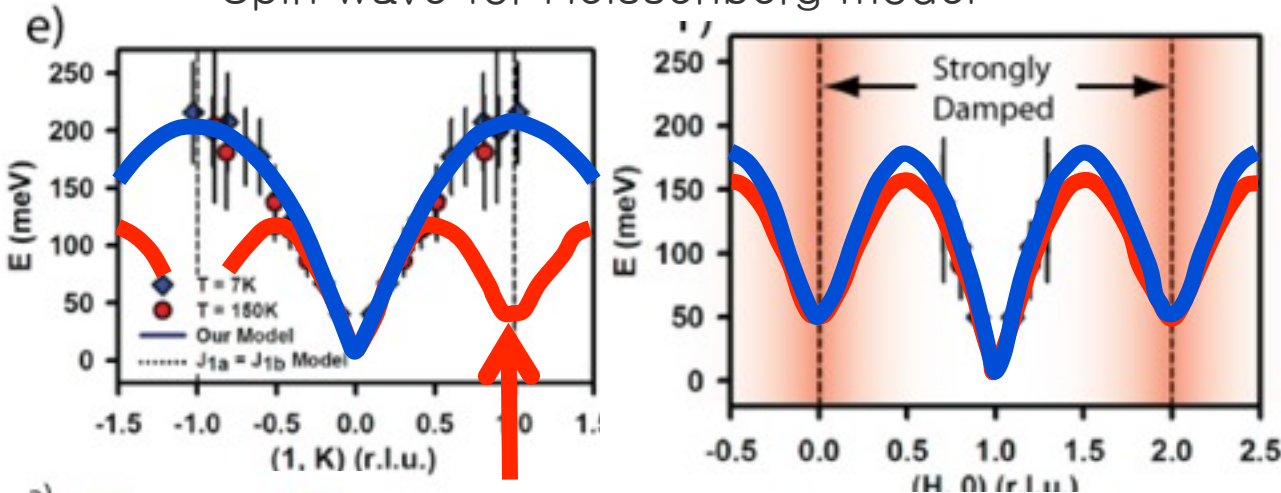


Leland W. Harriger, Pengcheng Dai et al., arXiv:1011.3771

# Dynamical structure factor

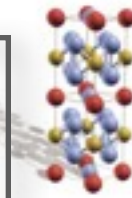


Spin wave for Heisenberg model



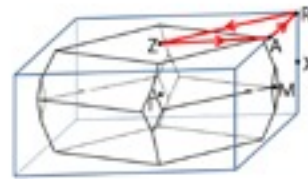
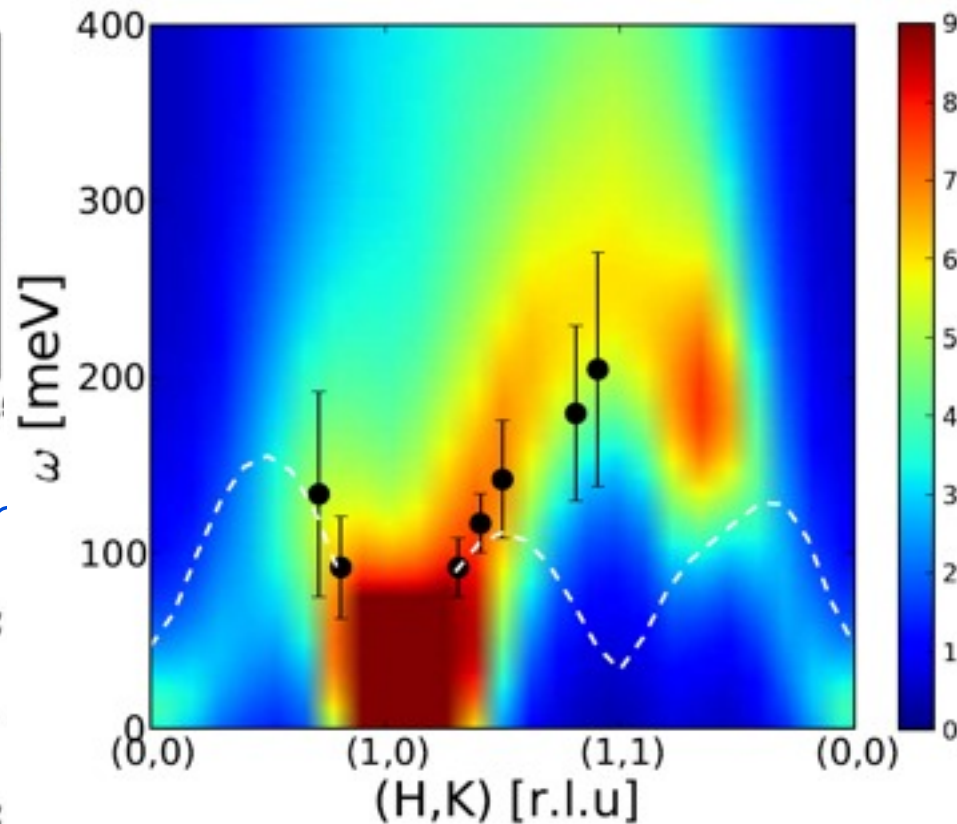
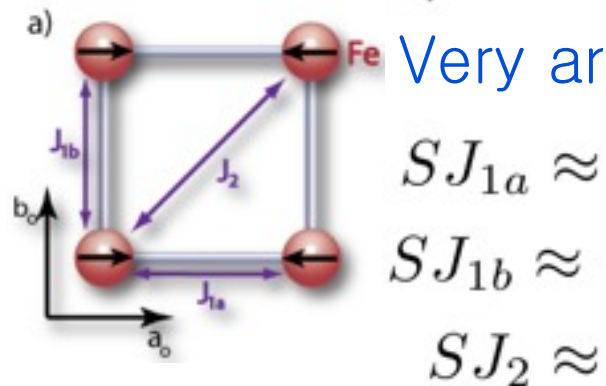
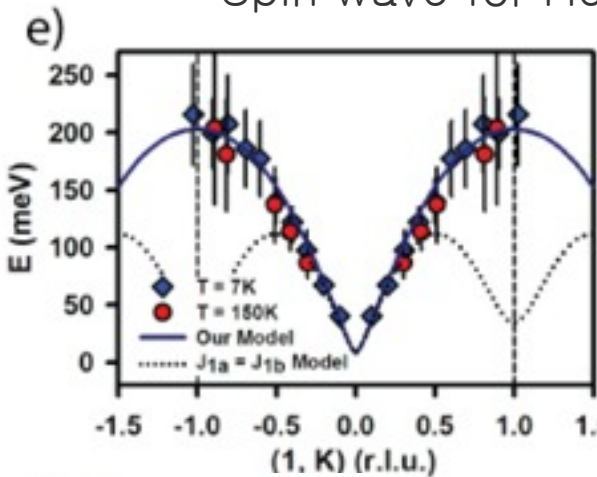
Leland W. Harriger, Pengcheng Dai et al., arXiv:1011.3771

# Dynamical structure factor



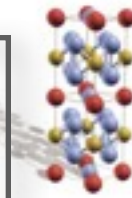
Spin wave for Heisenberg model

DMFT



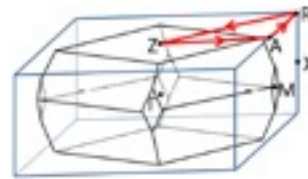
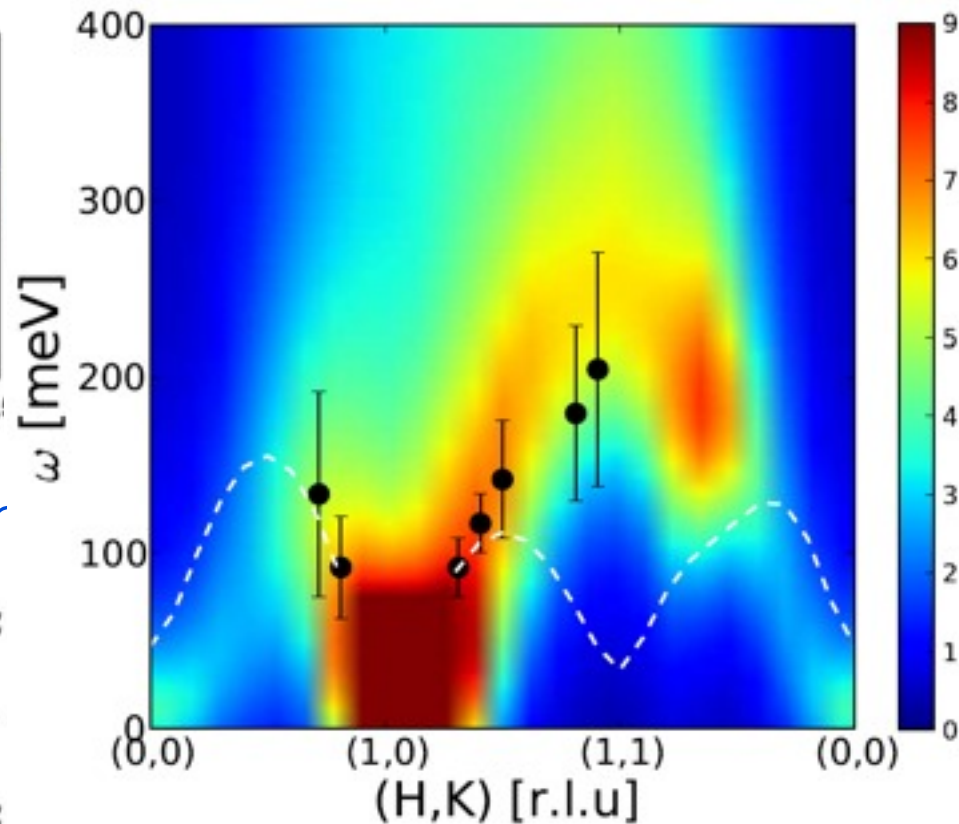
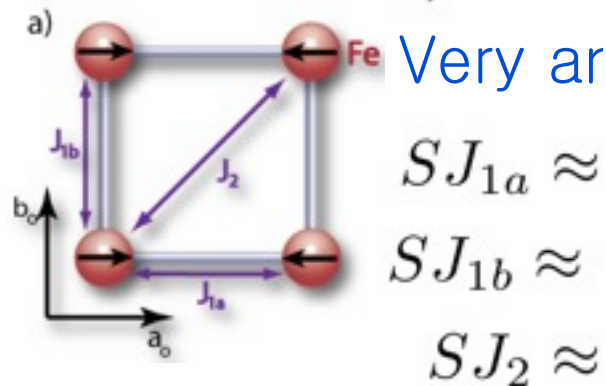
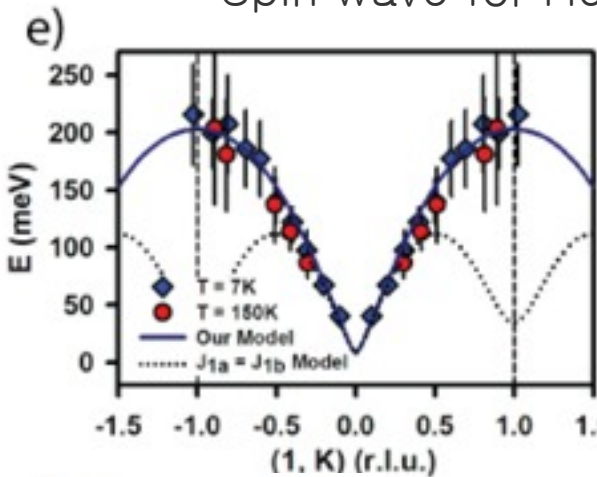
Leland W. Harriger, Pengcheng Dai et al., arXiv:1011.3771

# Dynamical structure factor



Spin wave for Heisenberg model

DMFT

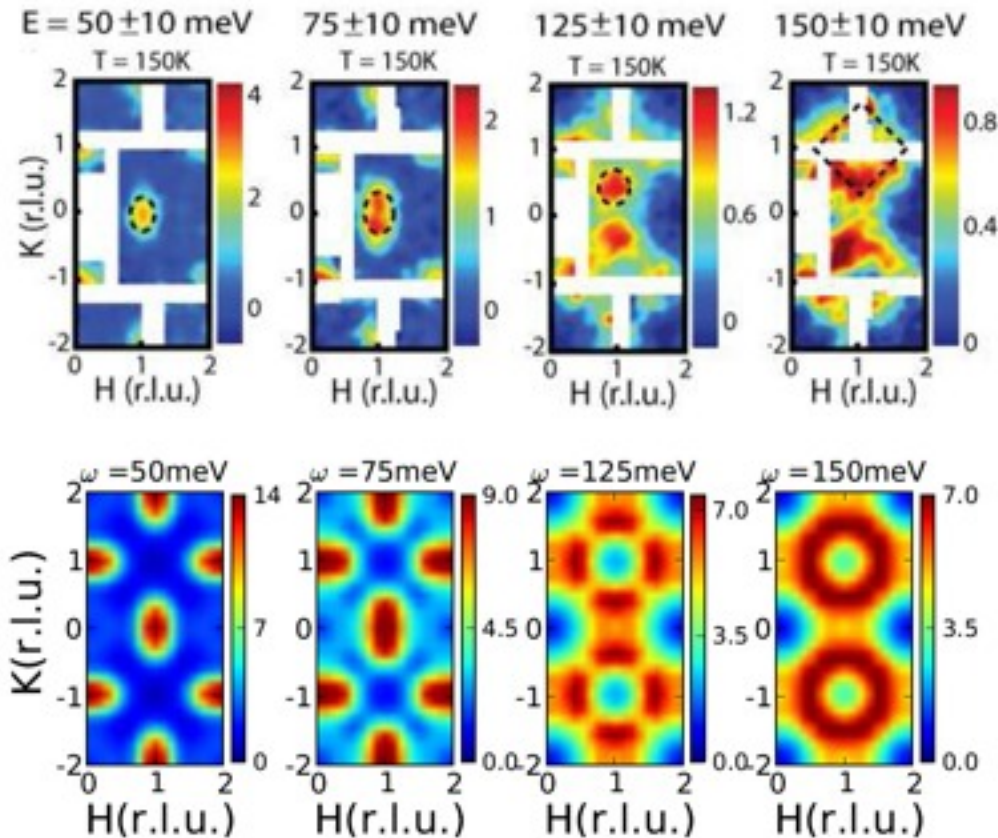
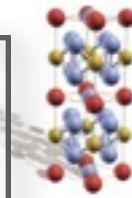


Leland W. Harriger, Pengcheng Dai et al., arXiv:1011.3771

No anisotropy needed (above  $T_S$ ) to explain neutrons



# Dynamical structure factor

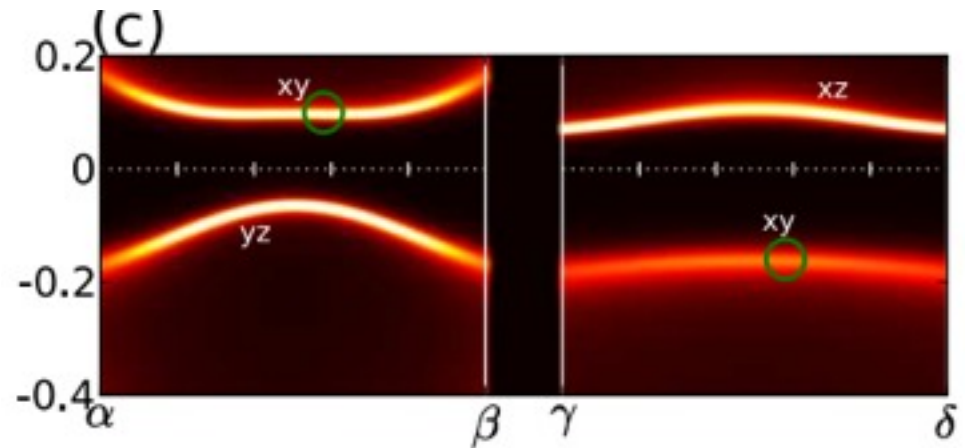
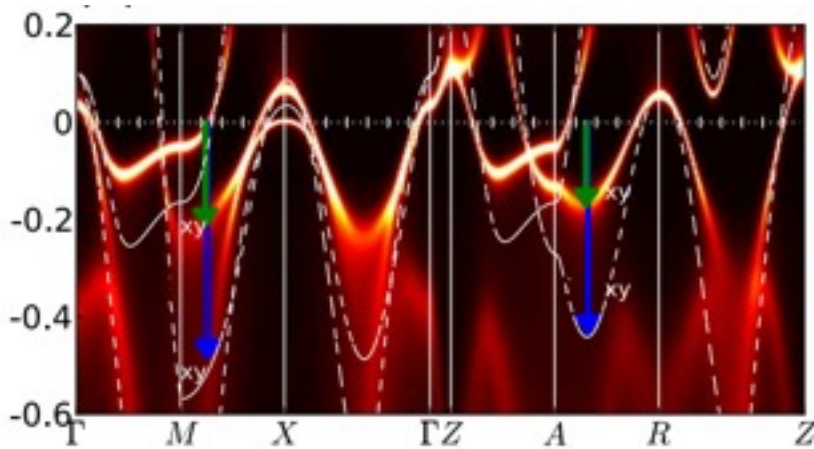
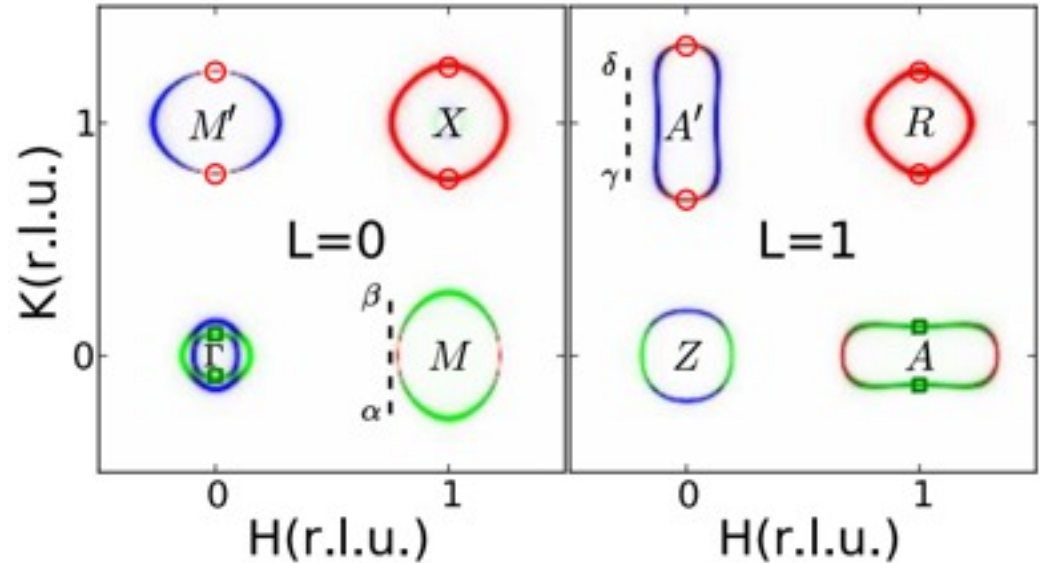
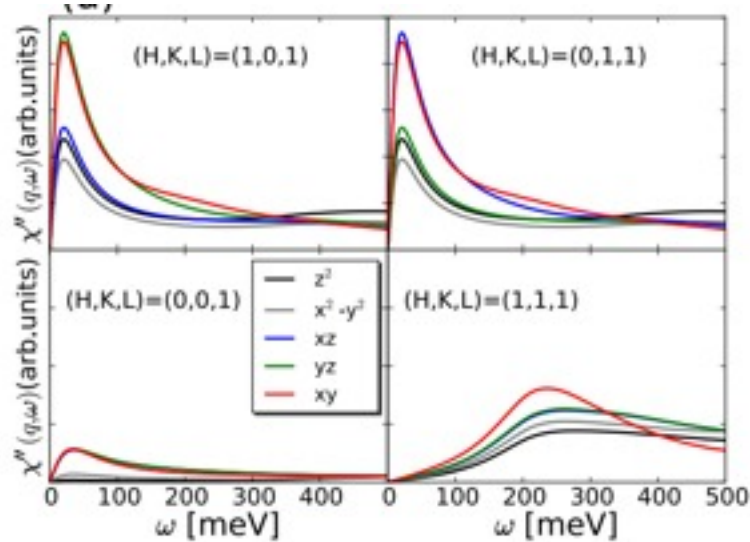
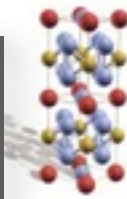


NEUTRONS EXP:  
Leland W. Harriger,  
Pengcheng Dai et al., arXiv:1011.3771

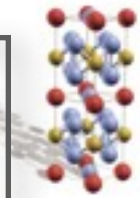
LDA+DMFT

J. T. Park, D. S. Inosov, A. Yaresko, S. Graser, et al.,  
Phys. Rev. B 82, 134503 (Oct 2010).

# Origin of peaks

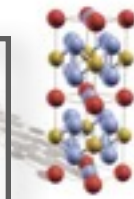


# Large fluctuating moment



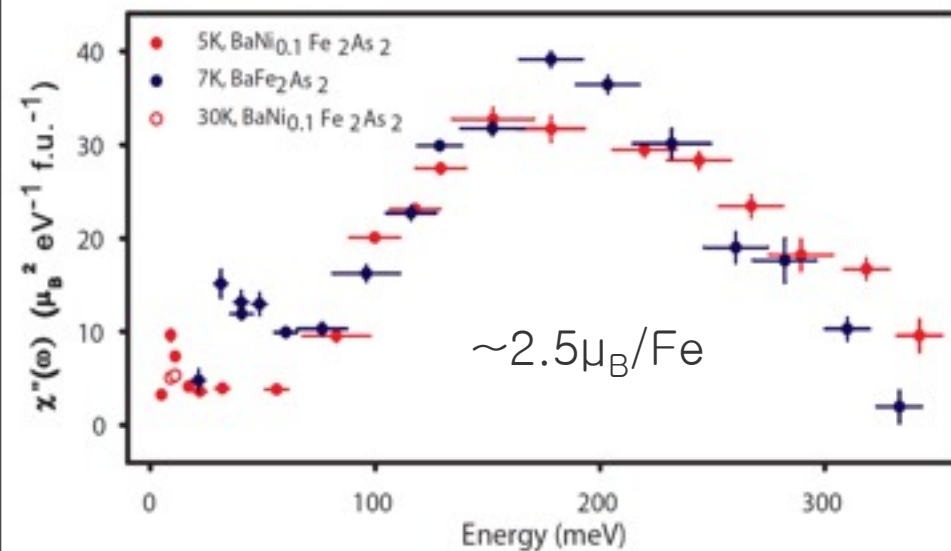
Fluctuating moment by neutrons:  $\langle \mu^2 \rangle = \int \frac{d\omega}{\pi} n(\omega) \chi''(\omega)$

# Large fluctuating moment

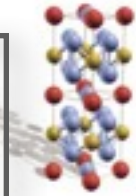


Fluctuating moment by neutrons:  $\langle \mu^2 \rangle = \int \frac{d\omega}{\pi} n(\omega) \chi''(\omega)$

Experiment by Pengcheng Dai

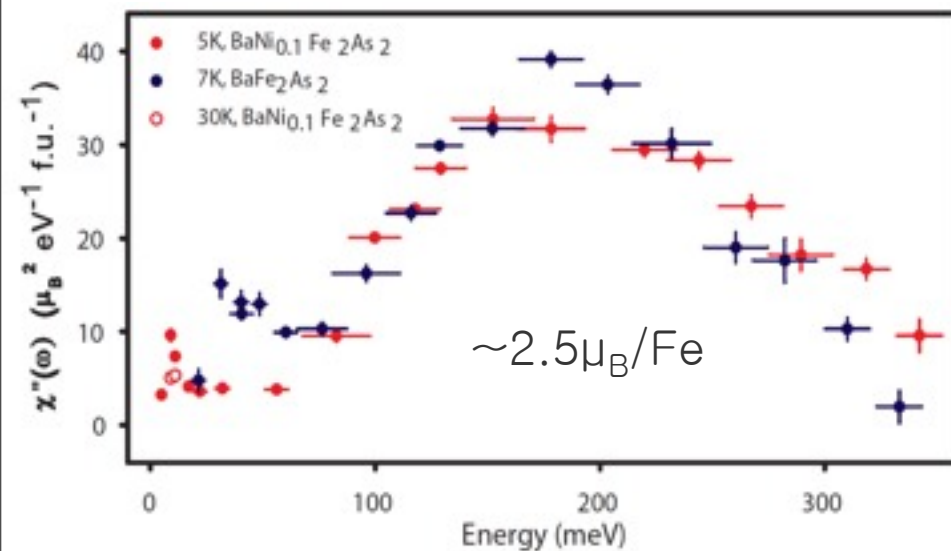


# Large fluctuating moment

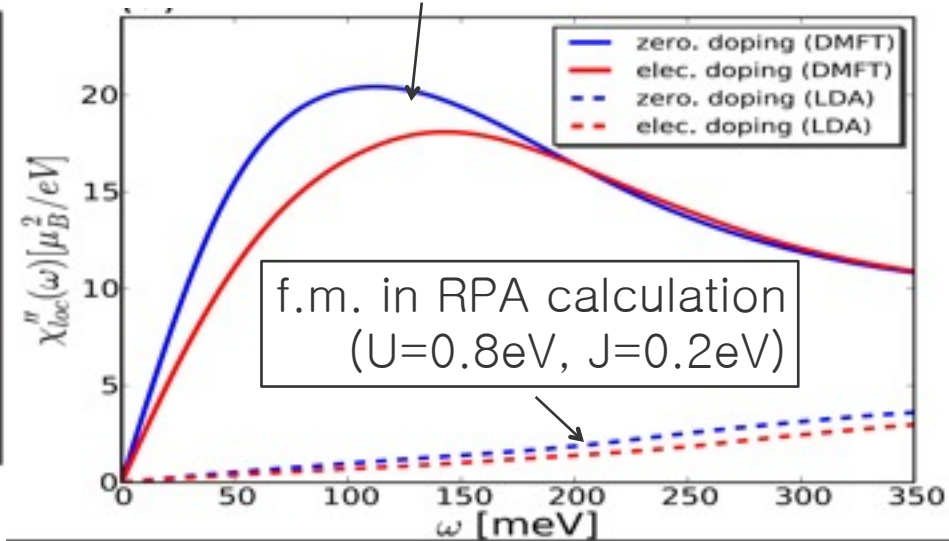


Fluctuating moment by neutrons:  $\langle \mu^2 \rangle = \int \frac{d\omega}{\pi} n(\omega) \chi''(\omega)$

Experiment by Pengcheng Dai

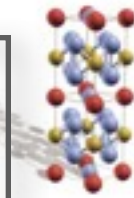


f.m. in DMFT



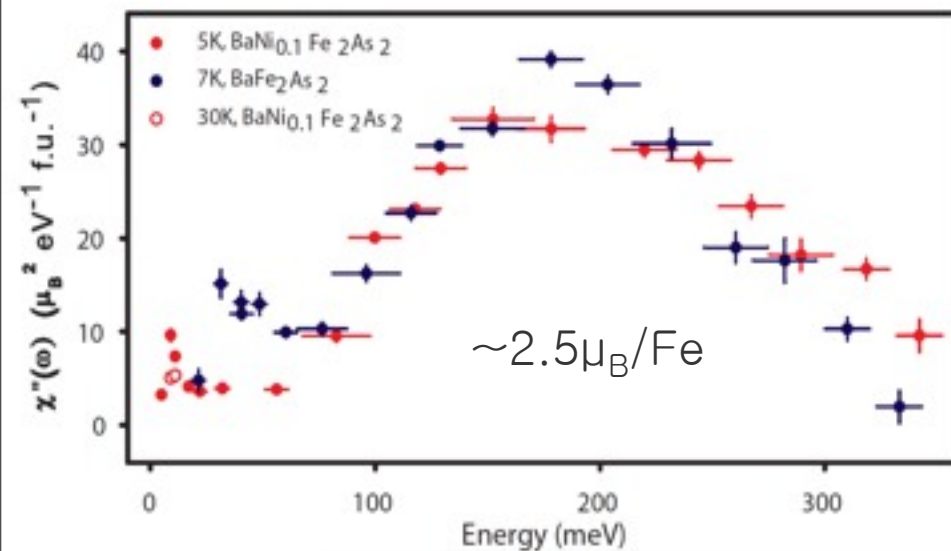


# Large fluctuating moment

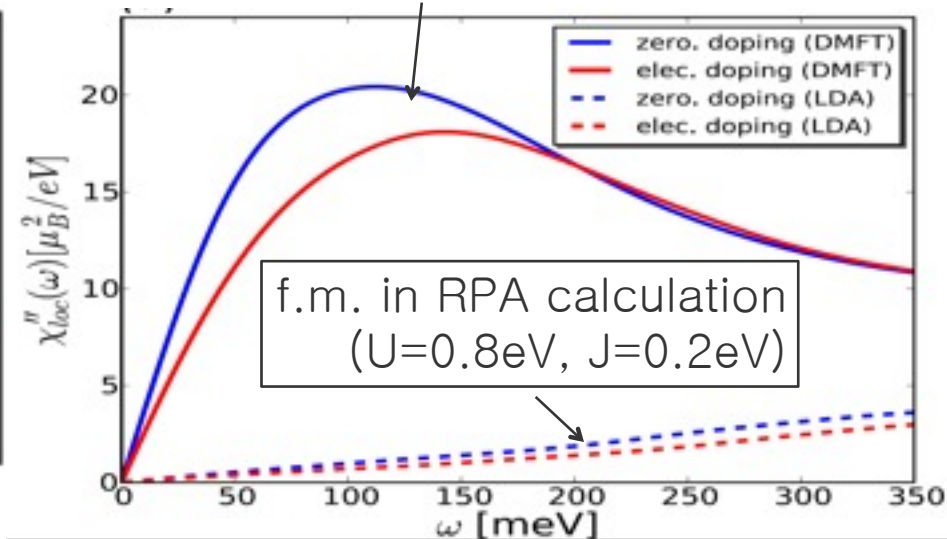


Fluctuating moment by neutrons:  $\langle \mu^2 \rangle = \int \frac{d\omega}{\pi} n(\omega) \chi''(\omega)$

Experiment by Pengcheng Dai



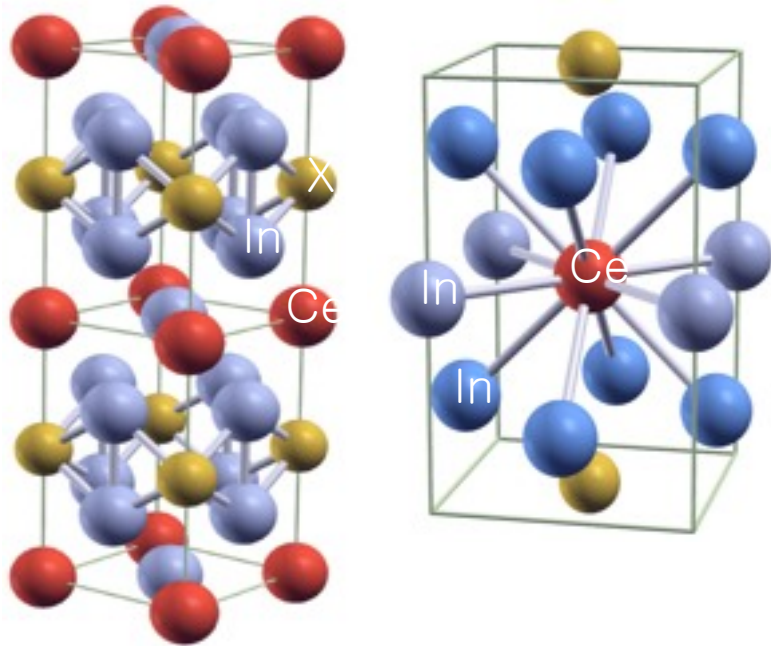
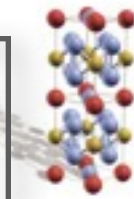
f.m. in DMFT



Large fluctuating moment can not be explained by a purely itinerant model.

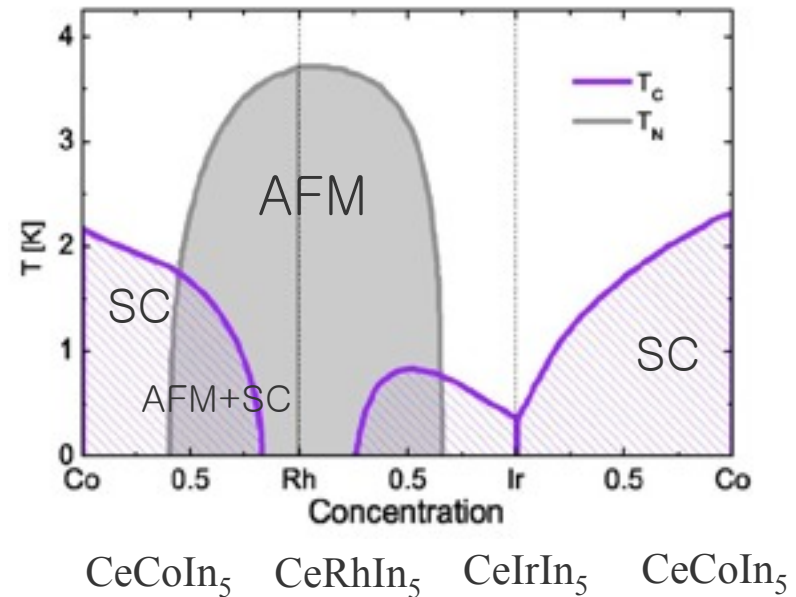
The DMFT account for a dual nature of iron d electrons: itinerant and localized nature.

# Heavy fermion materials (I I 5)



Ce atom in cage of 12 In atoms

## CeXIn<sub>5</sub>

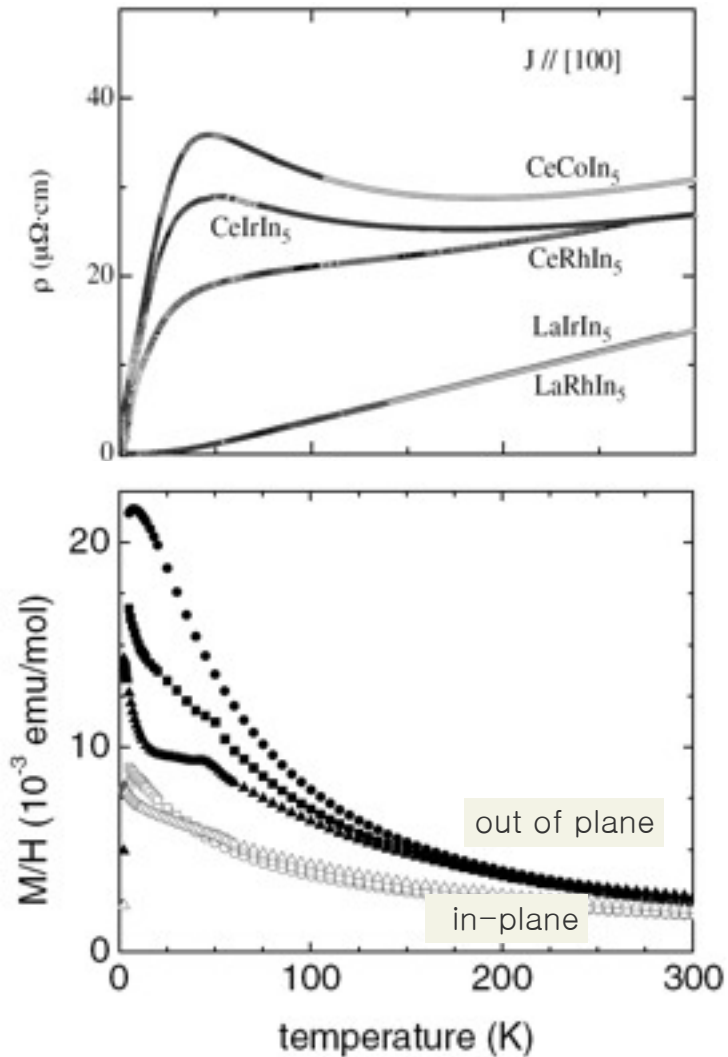


Properties can be tuned (substitution, pressure, magnetic field) between

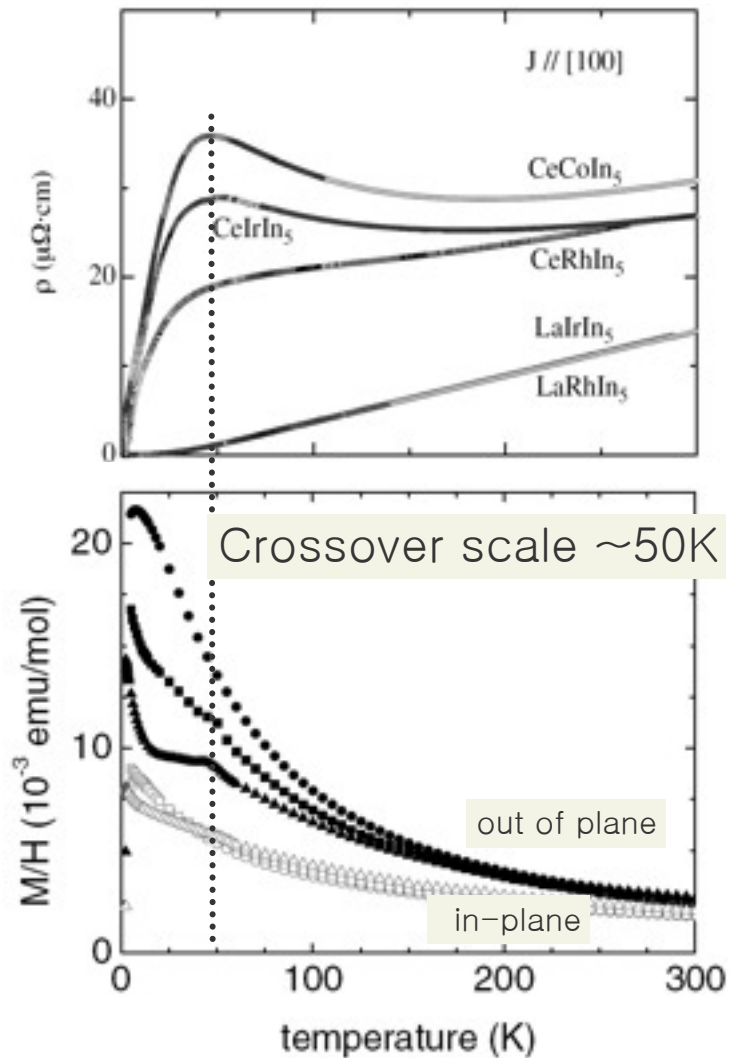
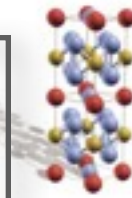
- antiferromagnetism
- superconductivity
- quantum critical point

	CeCoIn <sub>5</sub>	CeRhIn <sub>5</sub>	CeIrIn <sub>5</sub>	PuCoG <sub>5</sub>
$T_c$ [K]	SC 2.3K	N 3.8 K	SC 0.4K	18.3K
$T_{\text{crossover}}$	~50K	~50K	~50K	~370K
$C_v/T$ [mJ/molK <sup>2</sup> ]	300	400	750	100

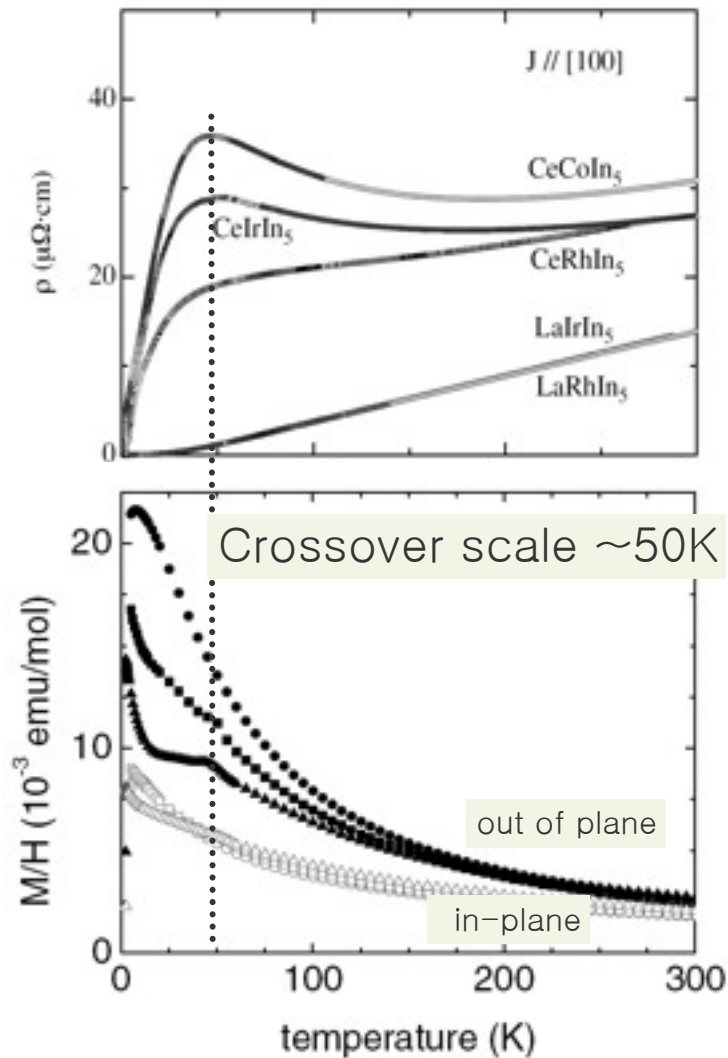
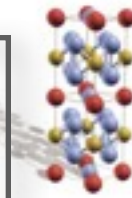
# Coherence crossover in exp.



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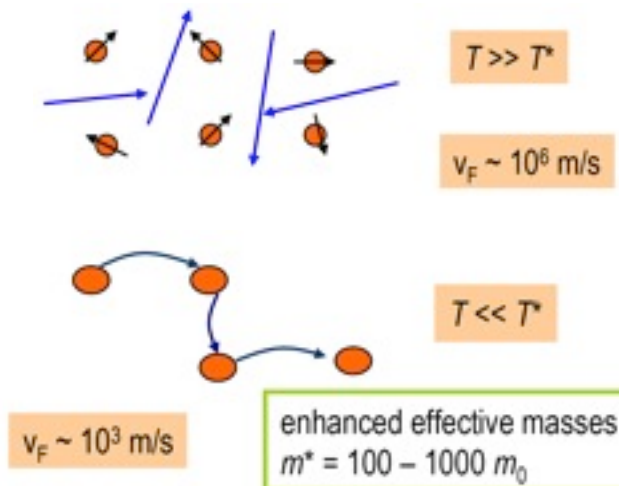
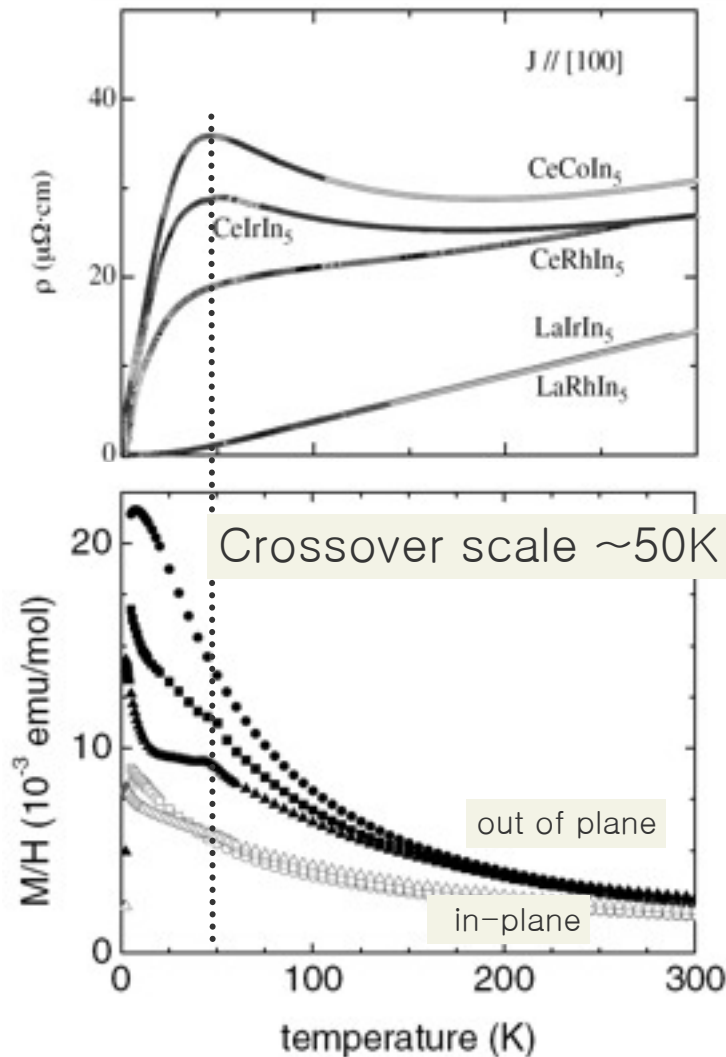
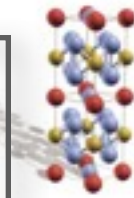
$$T \gg T^*$$

$$v_F \sim 10^6 \text{ m/s}$$

- High temperature Ce-4f local moments



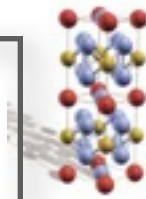
# Coherence crossover in exp.



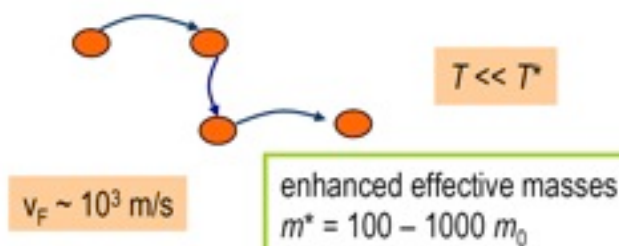
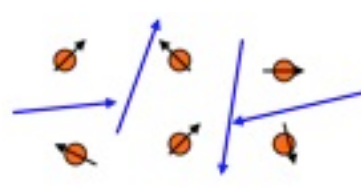
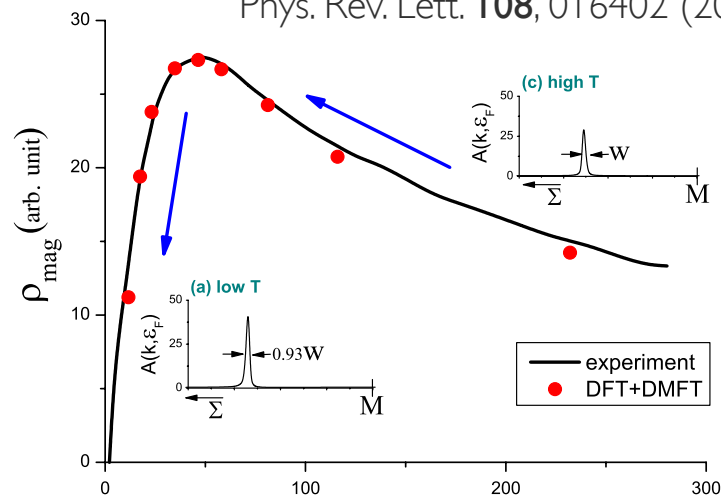
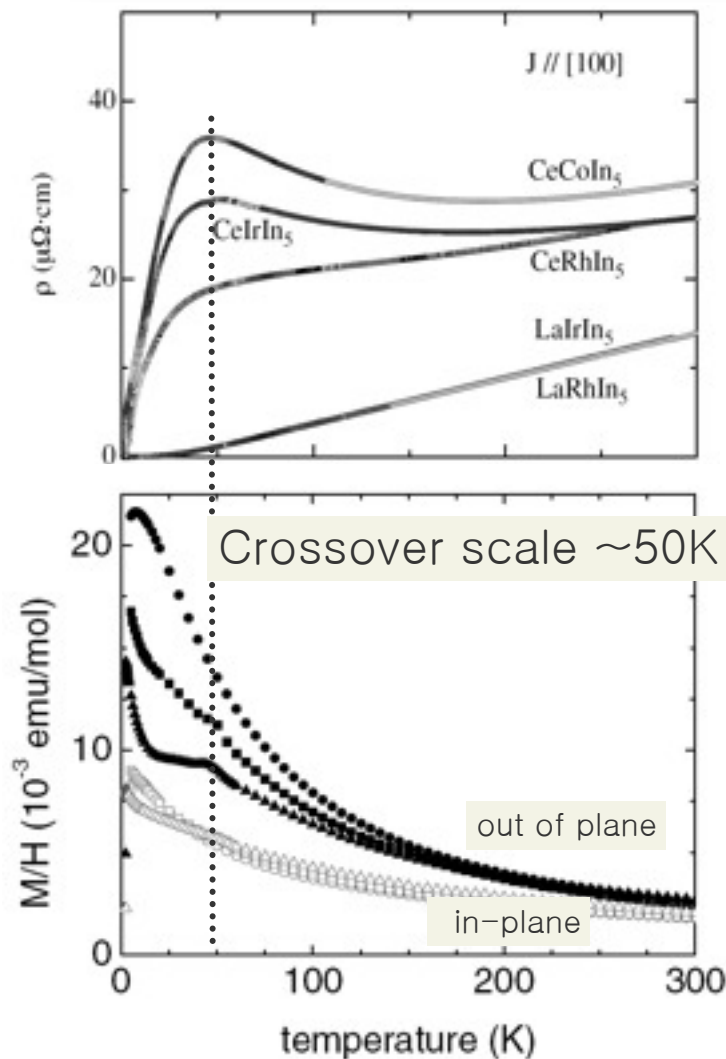
- High temperature  
Ce-4f local  
moments

- Low temperature –  
Itinerant heavy bands

# Coherence crossover in exp.



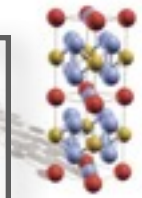
H.C. Choi, B.I. Min, J.H. Shim, K. Haule, G. Kotliar,  
Phys. Rev. Lett. **108**, 016402 (2012).



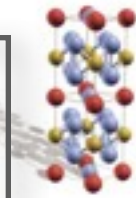
- High temperature  
Ce-4f local  
moments

- Low temperature –  
Itinerant heavy bands

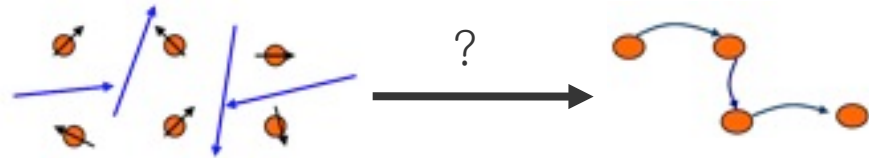
# Issues for the specific system



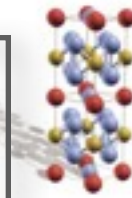
# Issues for the specific system



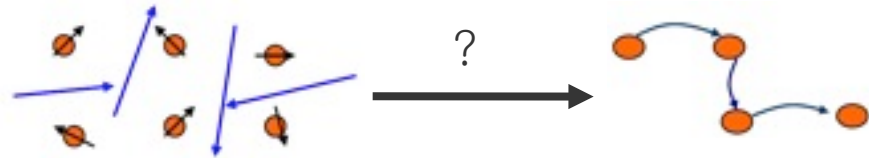
- How does the crossover from localized moments to itinerant q.p. happen?



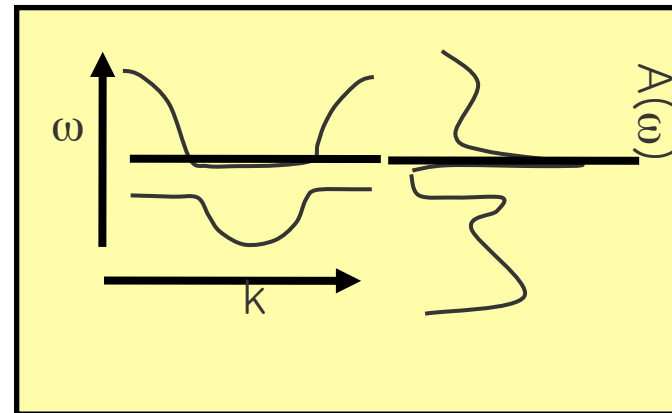
# Issues for the specific system



- How does the crossover from localized moments to itinerant q.p. happen?

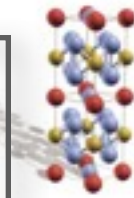


- How does the spectral weight redistribute?

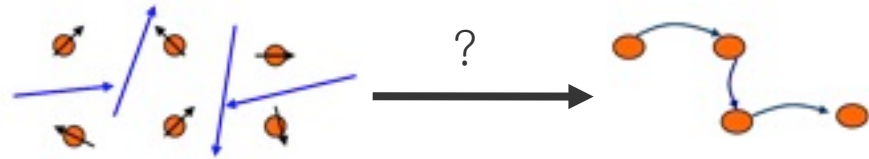




# Issues for the specific system

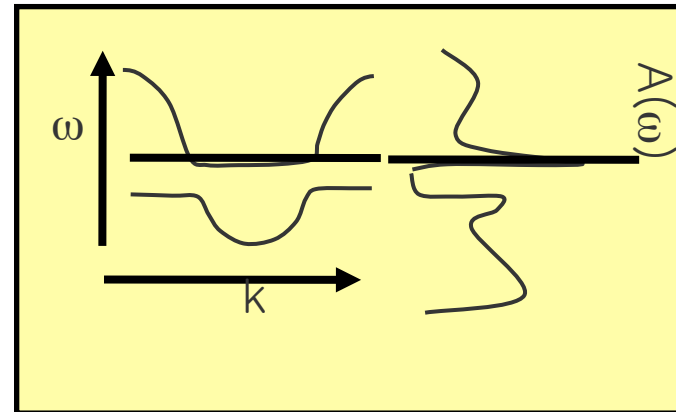


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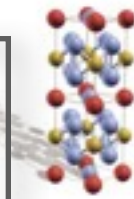


- How does the spectral weight redistribute?

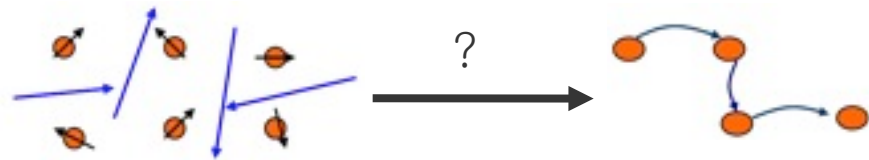
- Where in momentum space q.p. appear?



# Issues for the specific system



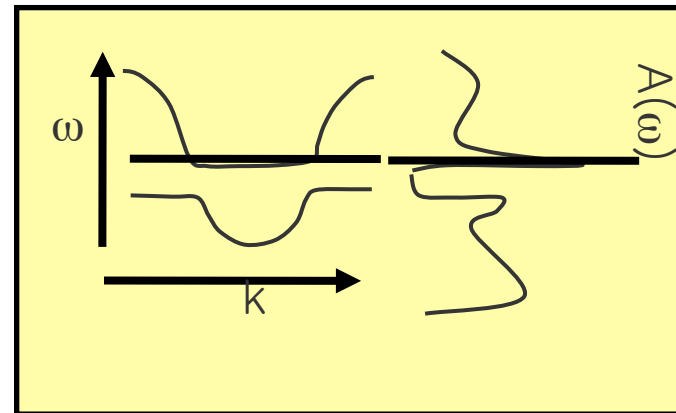
- How does the crossover from localized moments to itinerant q.p. happen?



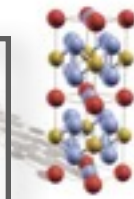
- How does the spectral weight redistribute?

- Where in momentum space q.p. appear?

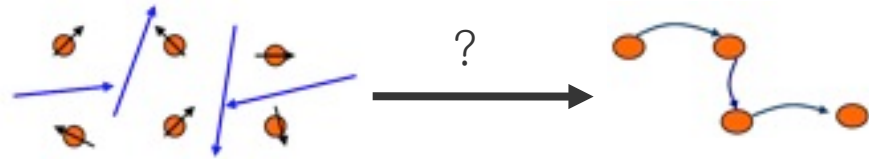
- What is the momentum dispersion of q.p.?



# Issues for the specific system

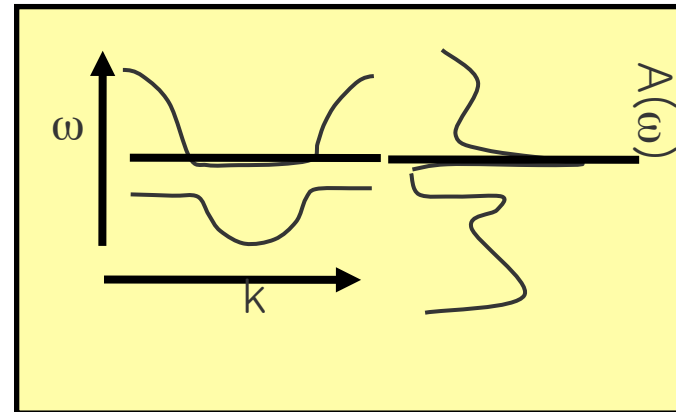


- How does the crossover from localized moments to itinerant q.p. happen?



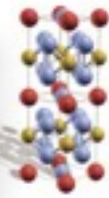
- How does the spectral weight redistribute?

- Where in momentum space q.p. appear?



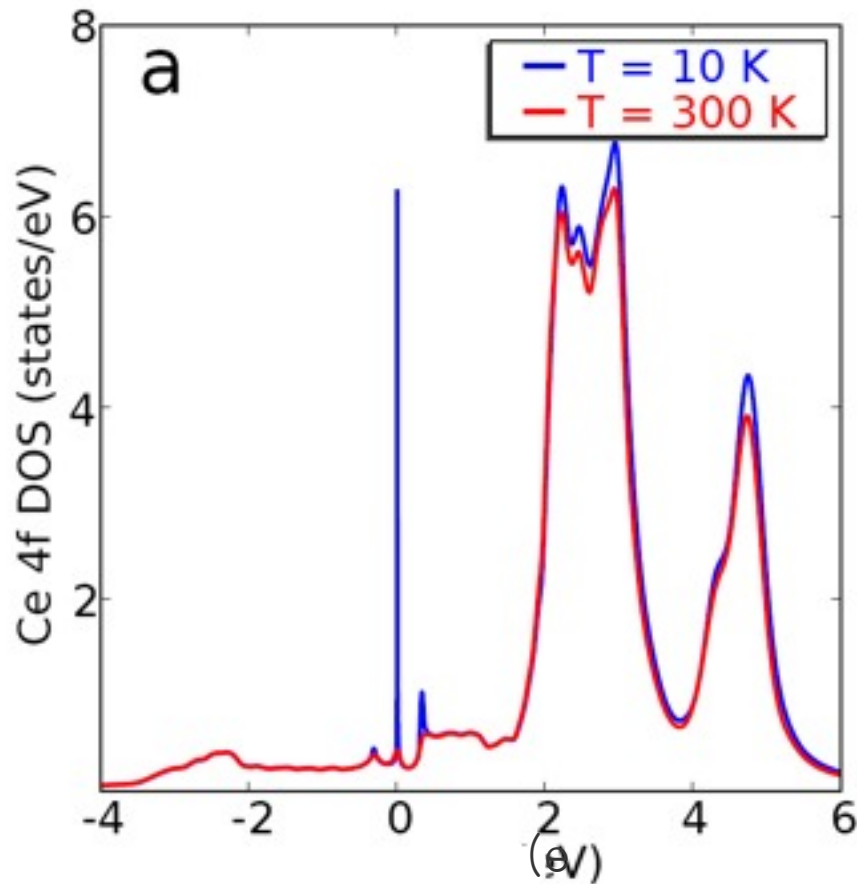
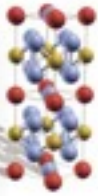
- What is the momentum dispersion of q.p.?
- How does the hybridization gap look like in momentum space?

# Temperature dep. of the local Ce-4f spectra



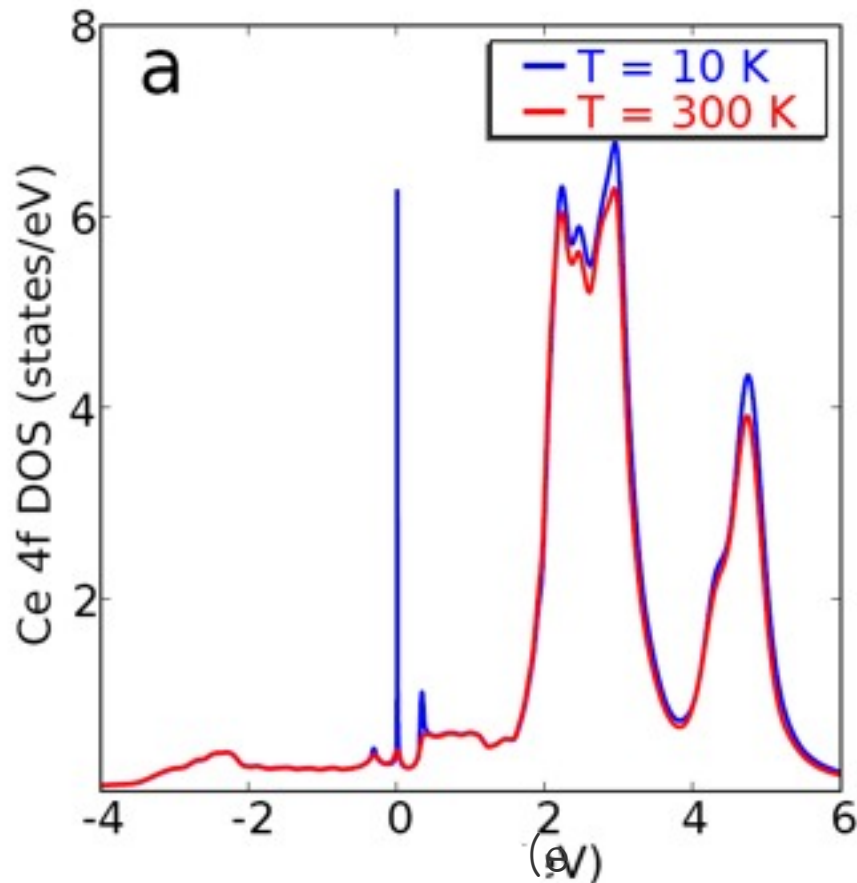
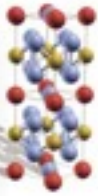
J. H. Shim, KH, and G. Kotliar  
Science 318, 1615 (2007)

# Temperature dep. of the local Ce-4f spectra



J. H. Shim, KH, and G. Kotliar  
Science 318, 1615 (2007)

# Temperature dep. of the local Ce-4f spectra

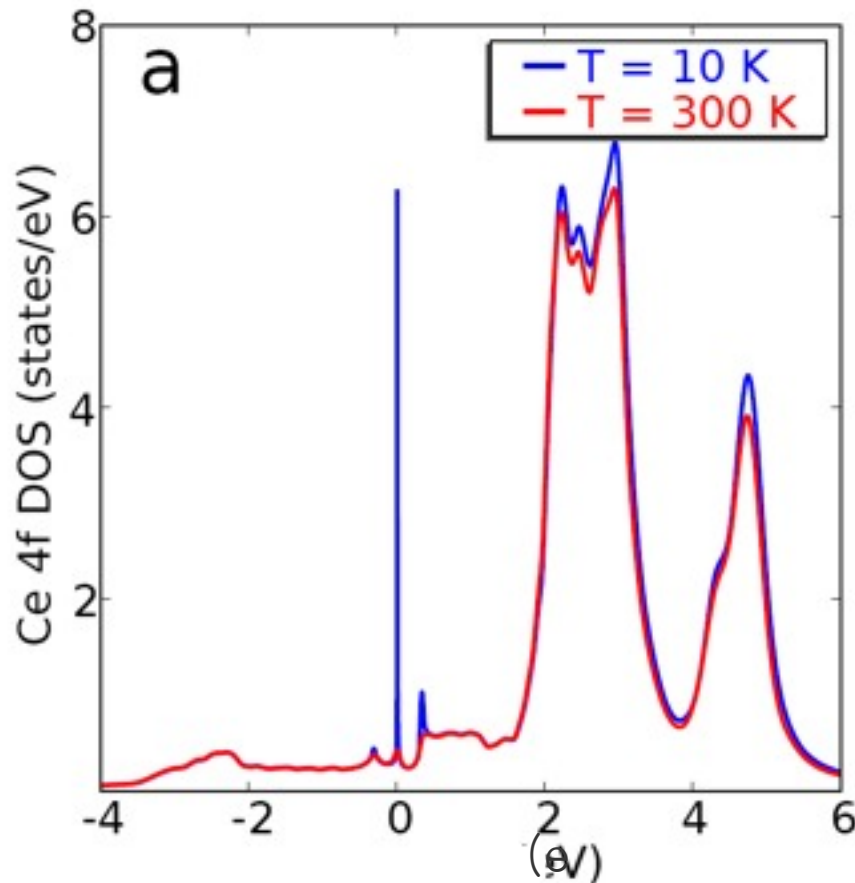
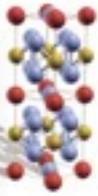


- At 300K, only Hubbard bands

J. H. Shim, KH, and G. Kotliar  
Science 318, 1615 (2007)



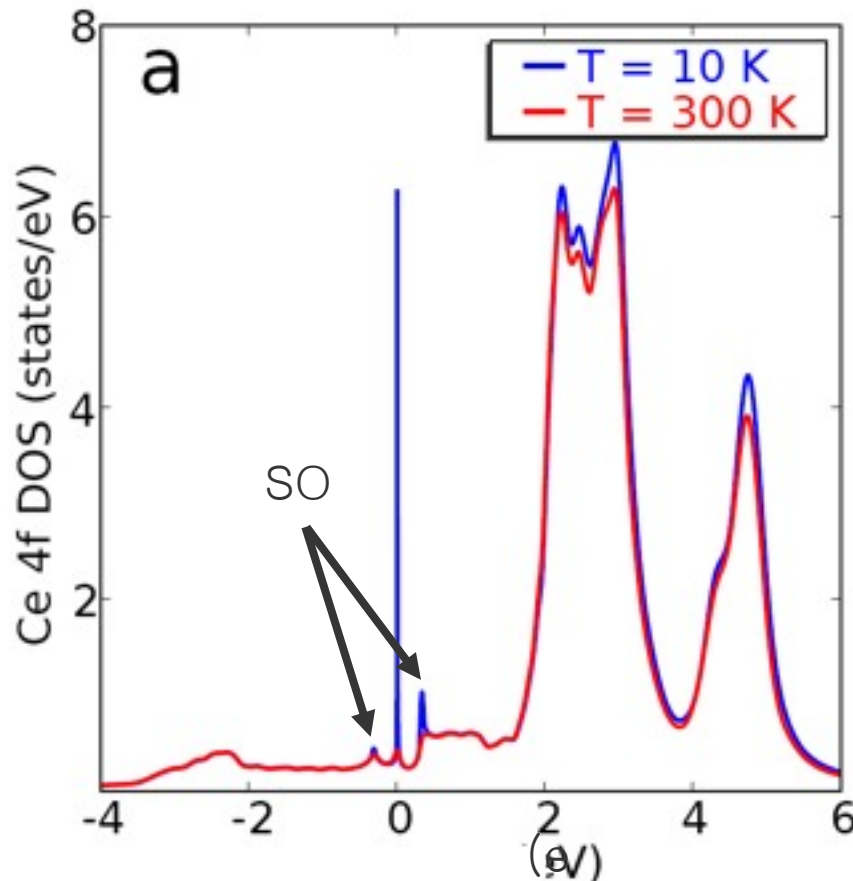
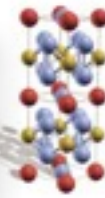
# Temperature dep. of the local Ce-4f spectra



- At 300K, only Hubbard bands
- At low  $T$ , very narrow q.p. peak (width  $\sim 3\text{ meV}$ )

J. H. Shim, KH, and G. Kotliar  
Science 318, 1615 (2007)

# Temperature dep. of the local Ce-4f spectra



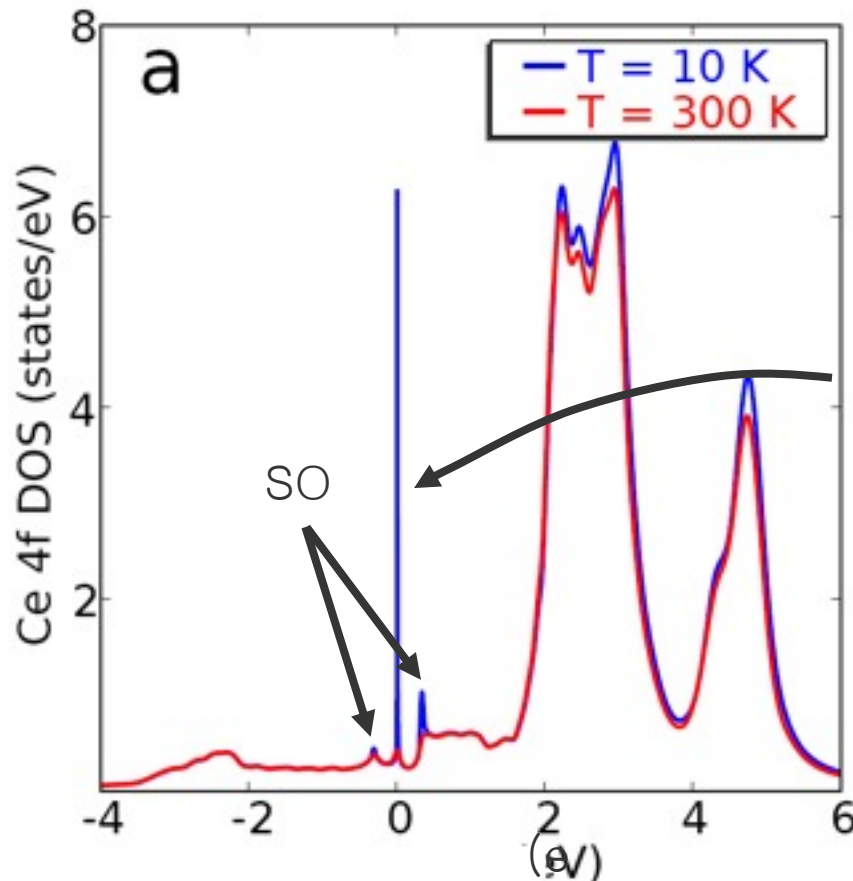
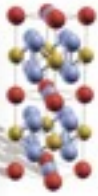
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- SO coupling splits q.p.:  $\pm 0.28\text{eV}$

J. H. Shim, KH, and G. Kotliar  
Science 318, 1615 (2007)

# Temperature dep. of the local Ce-4f spectra



- At 300K, only Hubbard bands

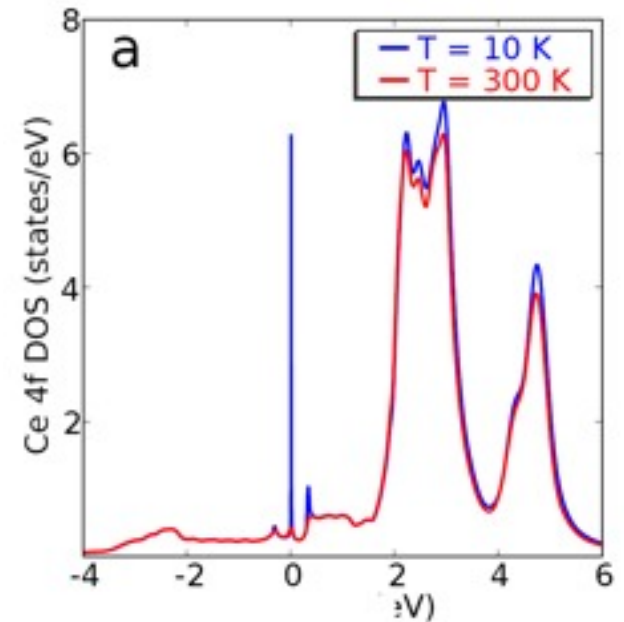
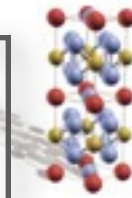
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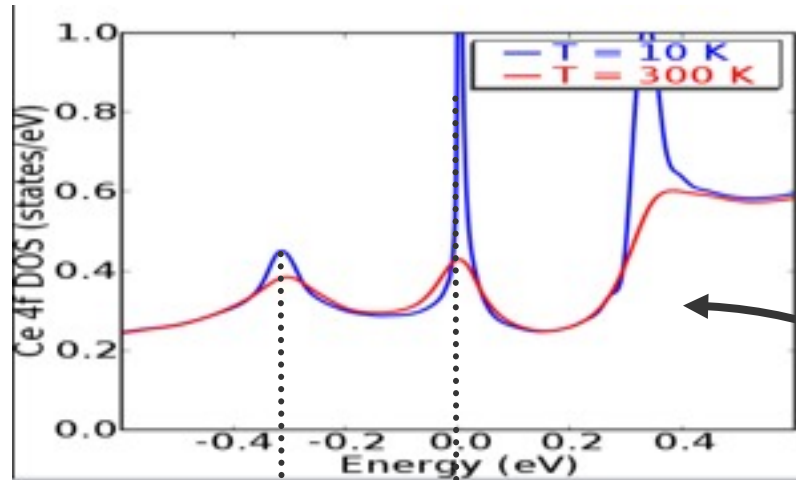
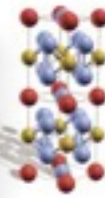
- Redistribution of weight up to very high frequency

J. H. Shim, KH, and G. Kotliar  
Science 318, 1615 (2007)

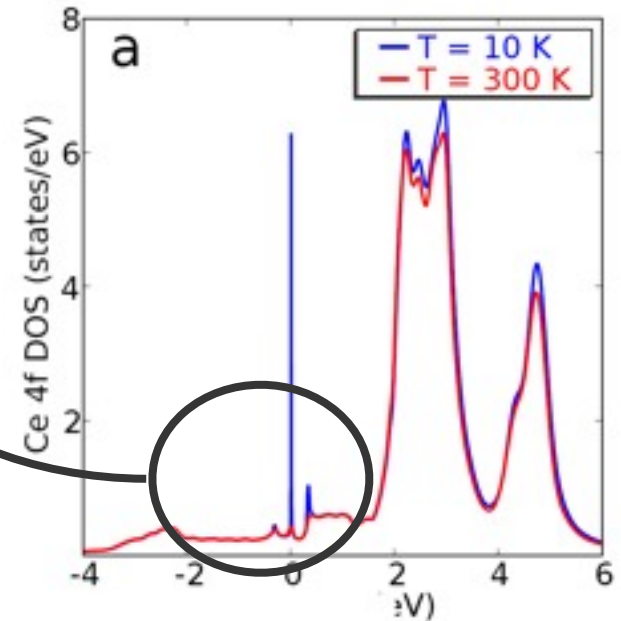
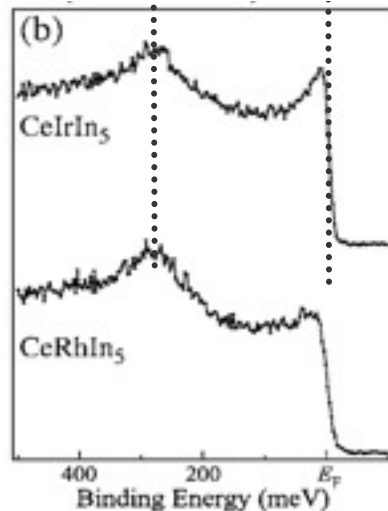
# Angle integrated photoemission vs DMFT



# Angle integrated photoemission vs DMFT

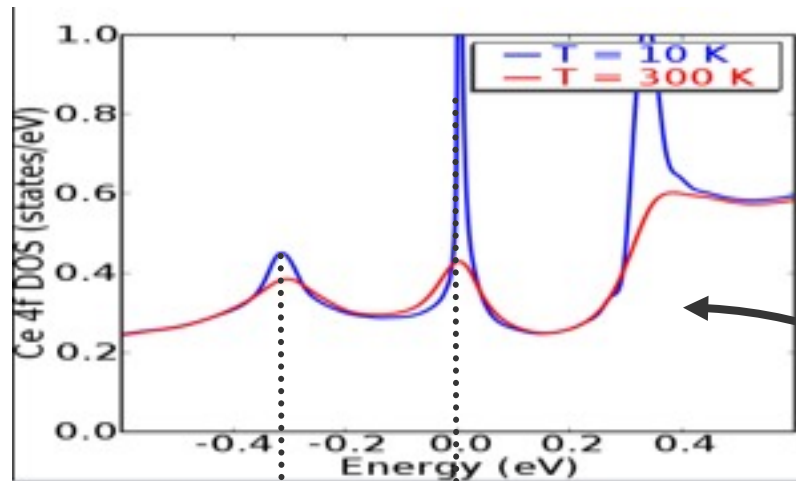
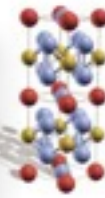


4d-4f on-resonance ( $h\nu=122$  eV)

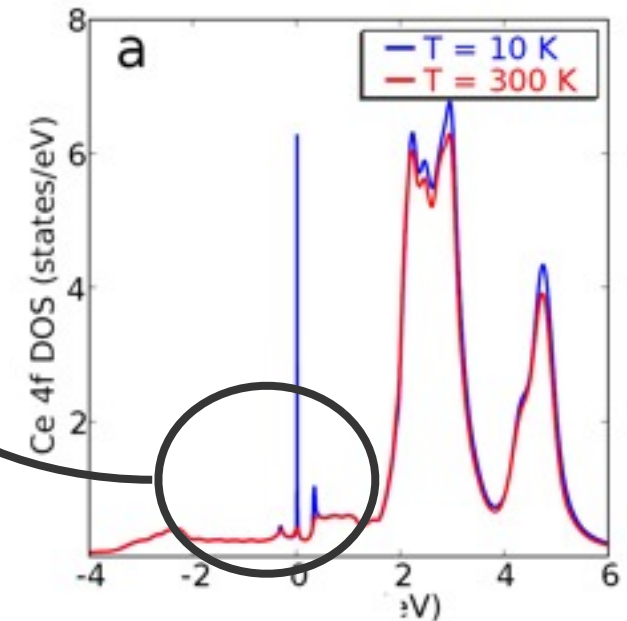
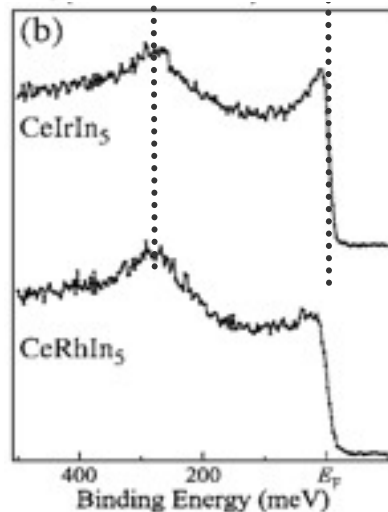


ARPES  
Fujimori, 2006

# Angle integrated photoemission vs DMFT



4d-4f on-resonance ( $h\nu=122$  eV)

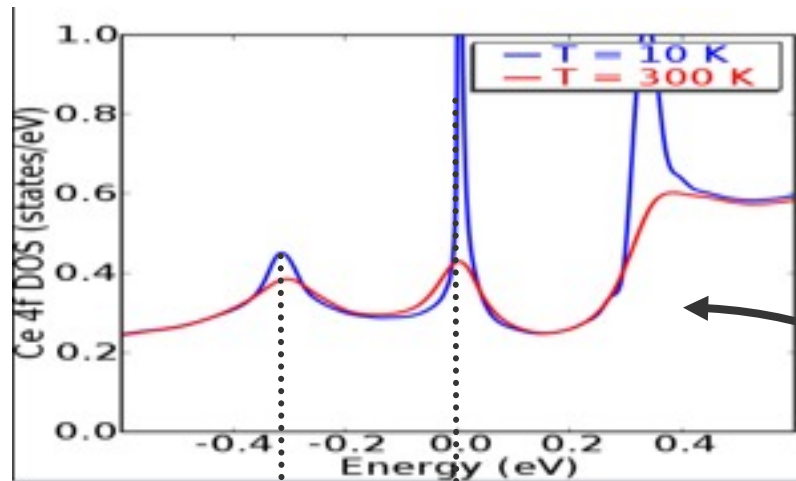
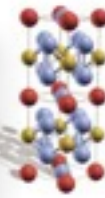


Experimental resolution  $\sim 30$  meV,  
theory predicts 3 meV broad band

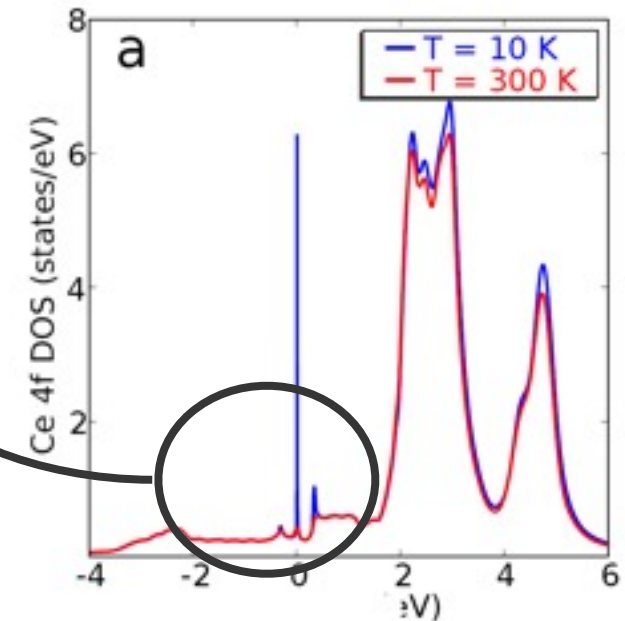
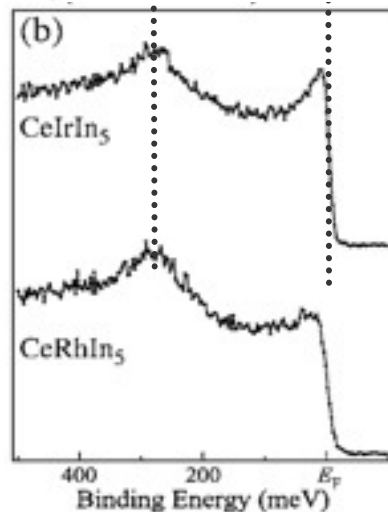
ARPES  
Fujimori, 2006



# Angle integrated photoemission vs DMFT



4d-4f on-resonance ( $h\nu=122$  eV)

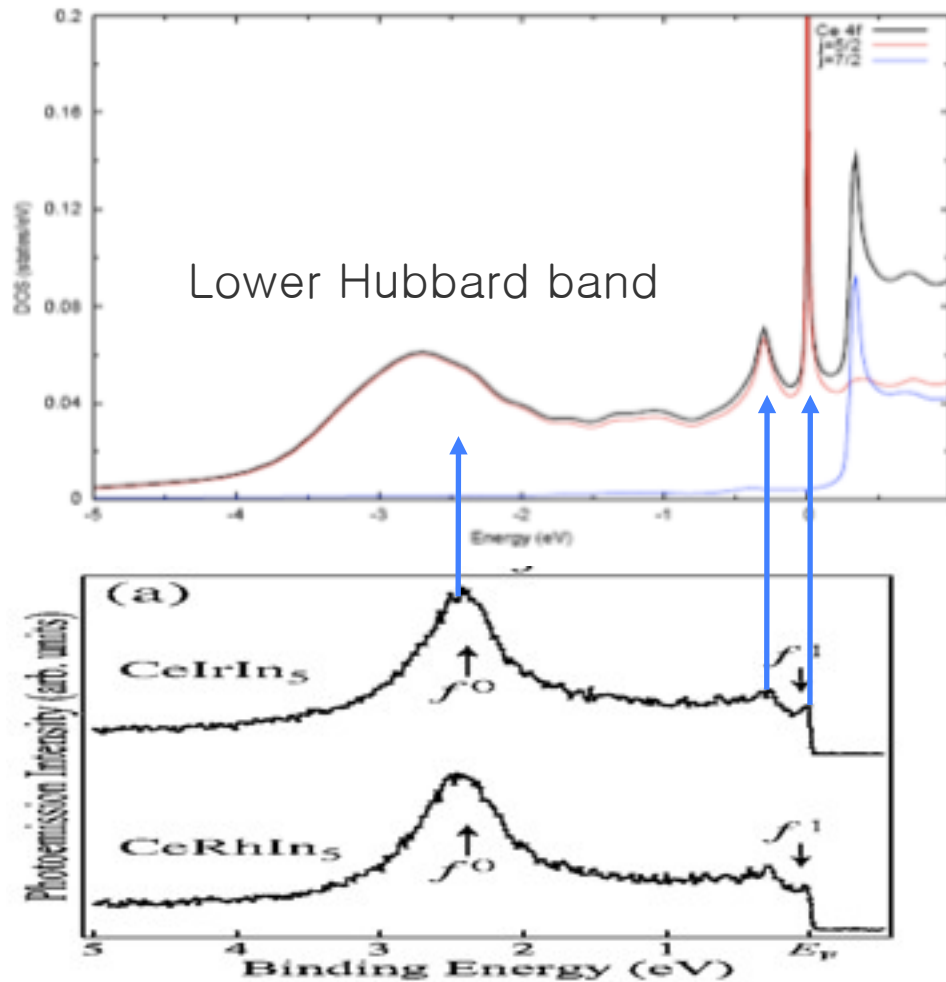


Experimental resolution  $\sim 30$  meV,  
theory predicts 3 meV broad band

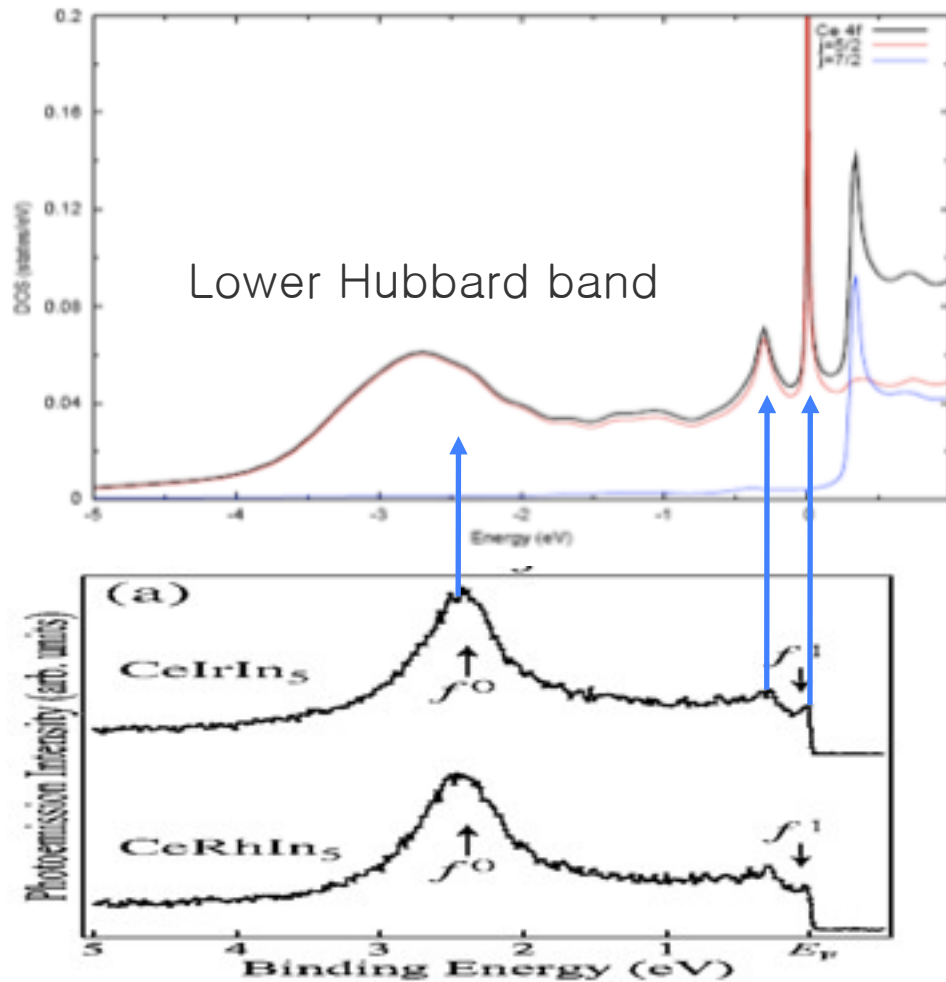
Surface sensitive at 122 eV

ARPES  
Fujimori, 2006

# Angle integrated photoemission vs DMFT

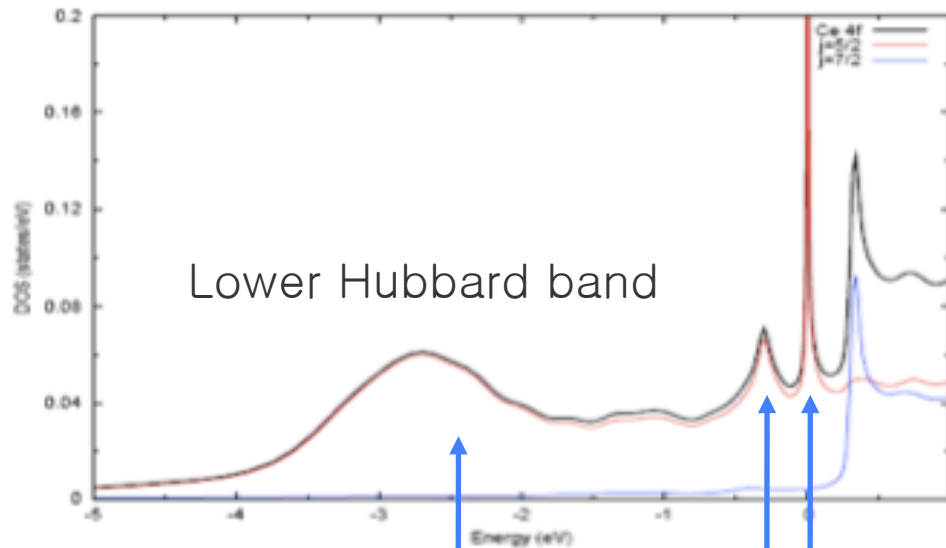
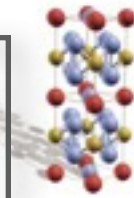


# Angle integrated photoemission vs DMFT



ARPES  
Fujimori, 2006

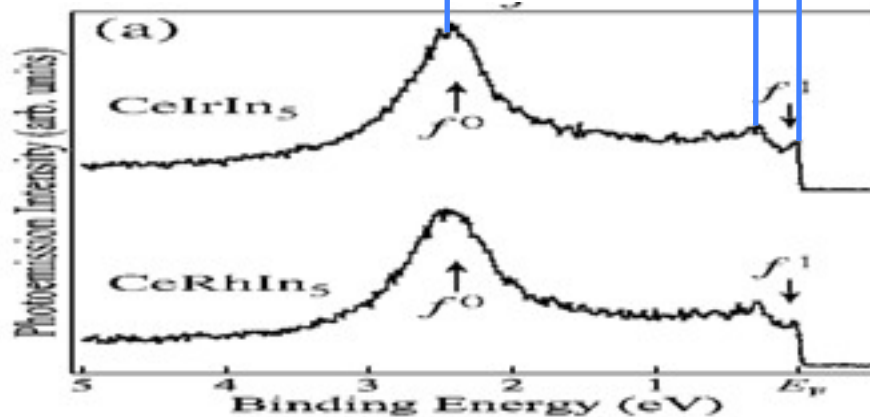
# Angle integrated photoemission vs DMFT



Nice agreement for the

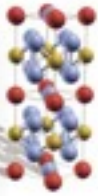
- Hubbard band position
- SO split qp peak

Hard to see narrow resonance in ARPES since very little weight of q.p. is below  $E_f$

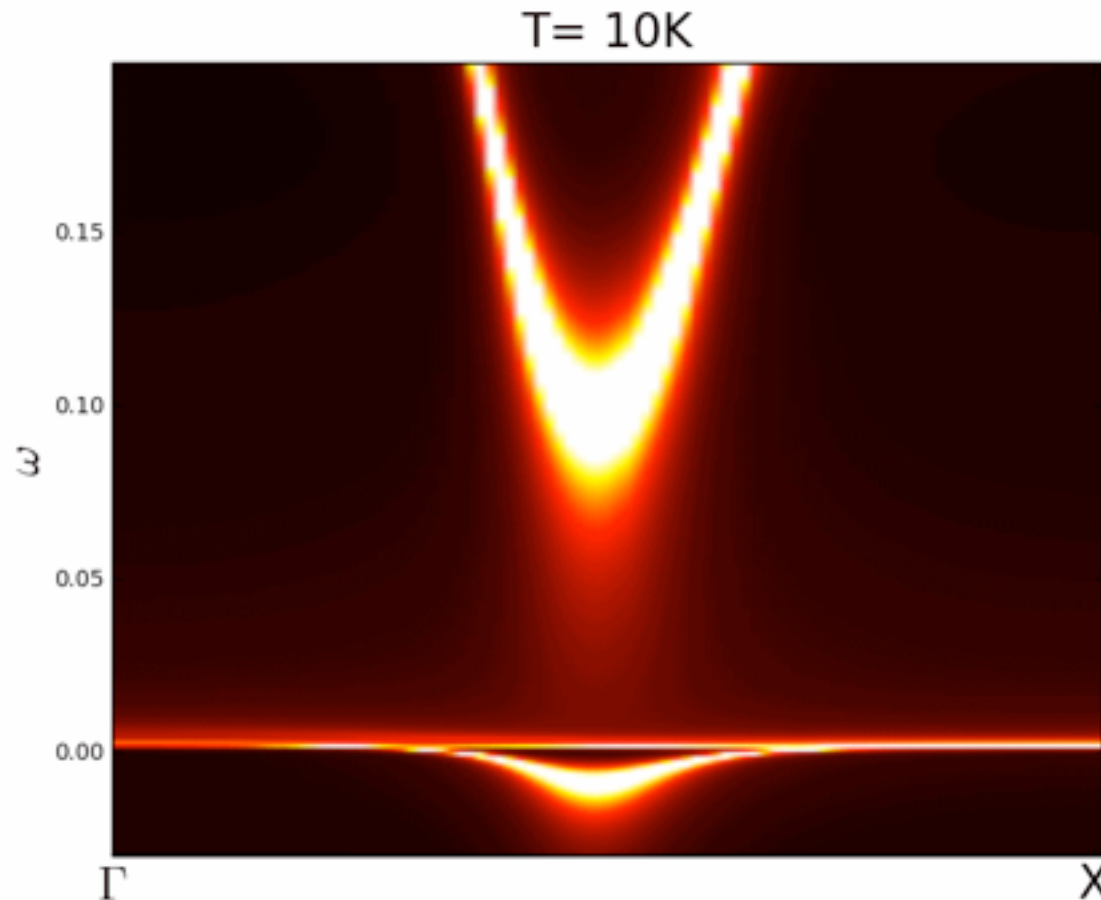


ARPES  
Fujimori, 2006

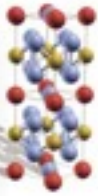
# T-dep momentum resolved photoemission



spectral  
function:  
 $A(k, \omega)$

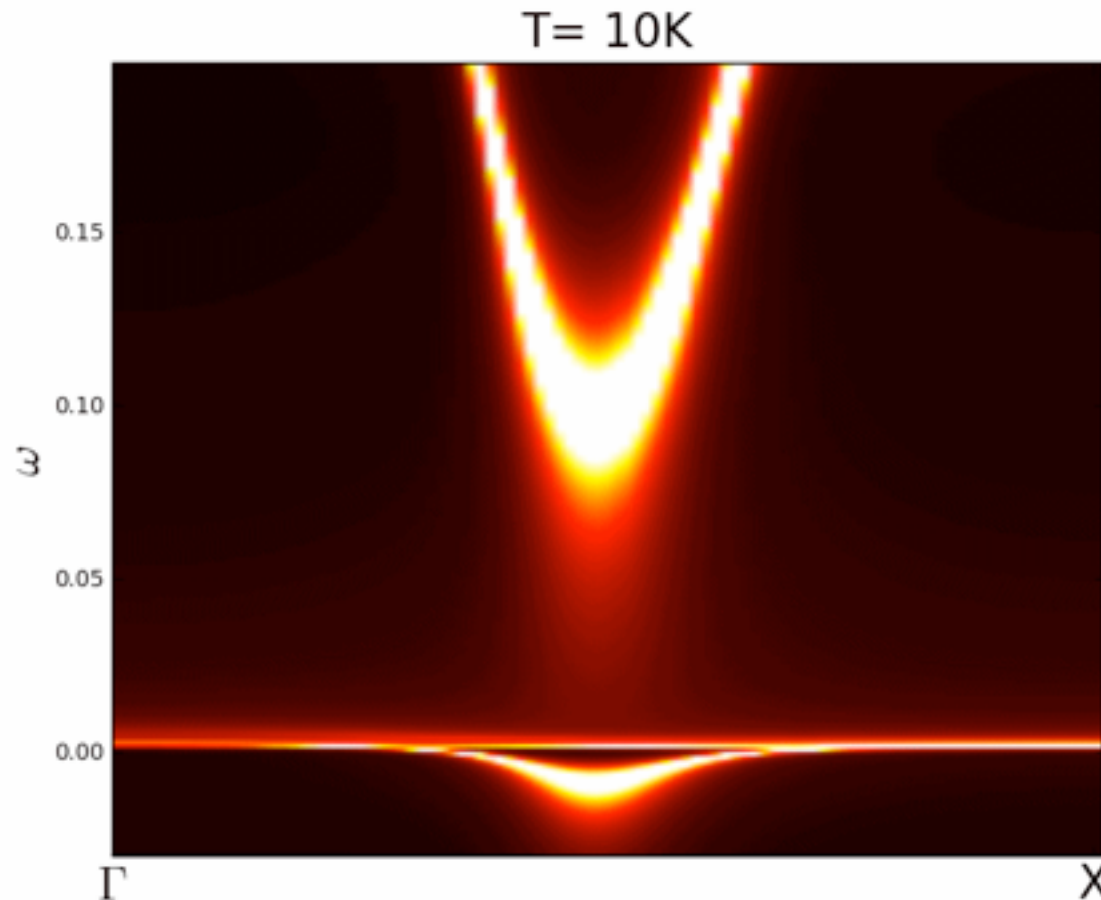


# T-dep momentum resolved photoemission



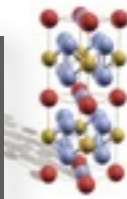
spectral  
function:  
 $A(k, \omega)$

H.C. Choi, B.I. Min, J.H. Shim, K. Haule, G. Kotliar,  
Phys. Rev. Lett. **108**, 016402 (2012).

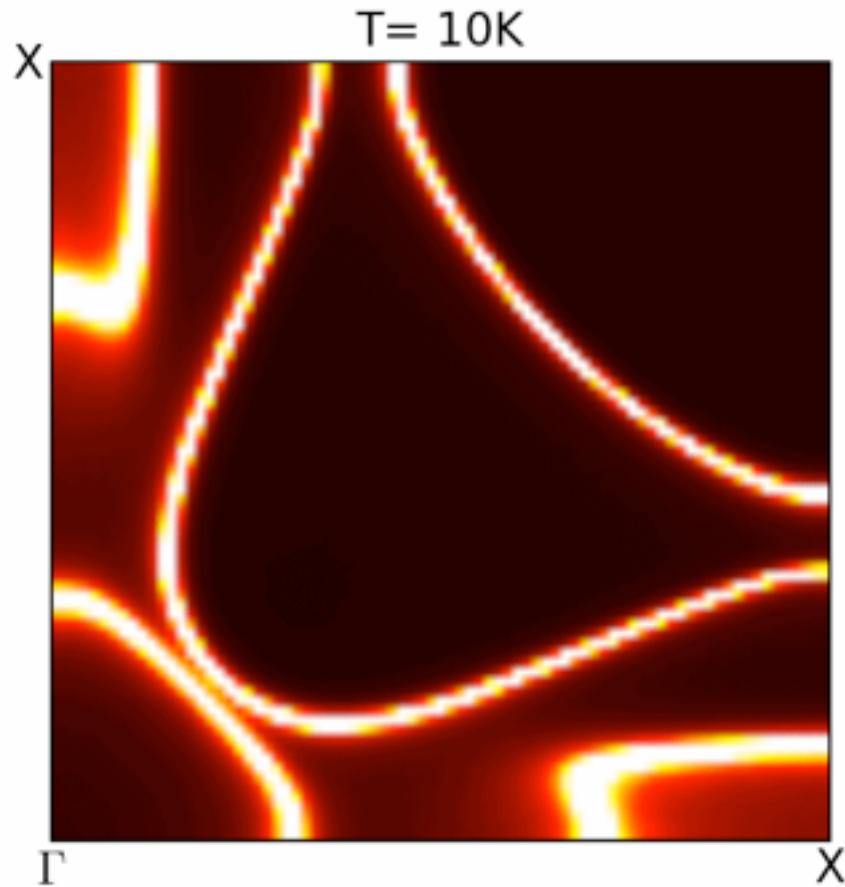




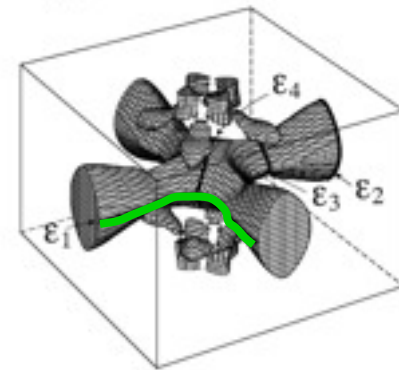
# T-dep Fermi surface-topological change



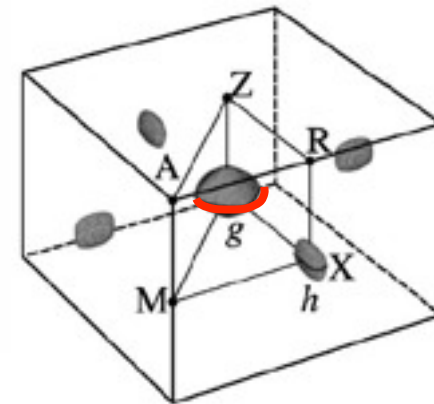
Fermi surface in the  $\Gamma$  plane



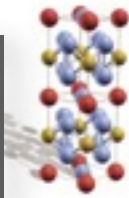
high -T



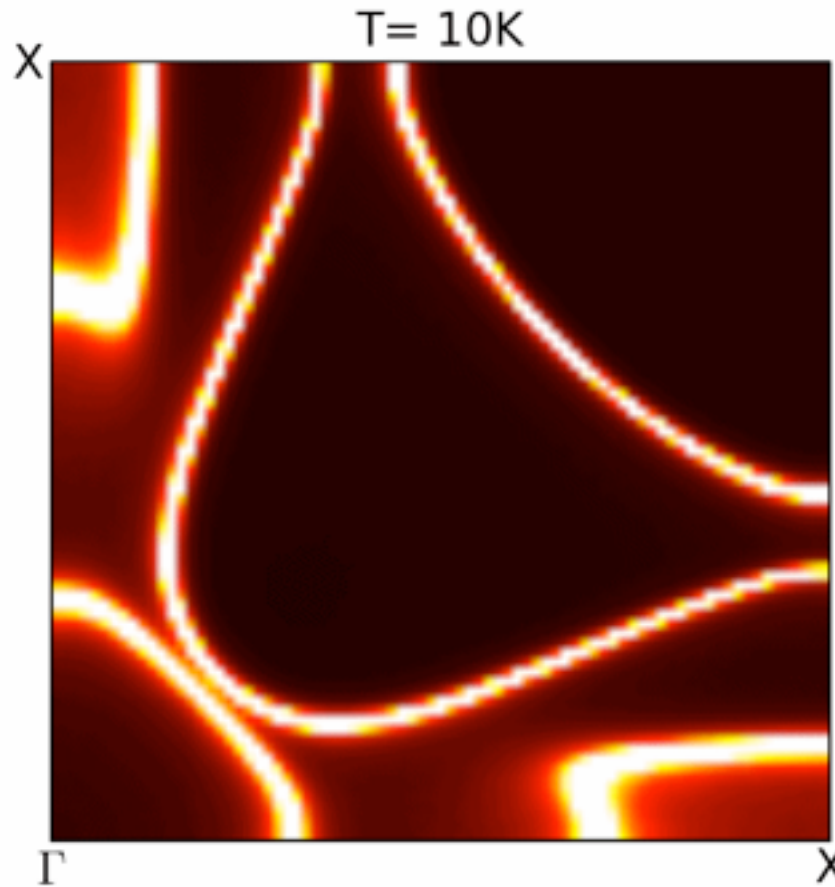
low -T



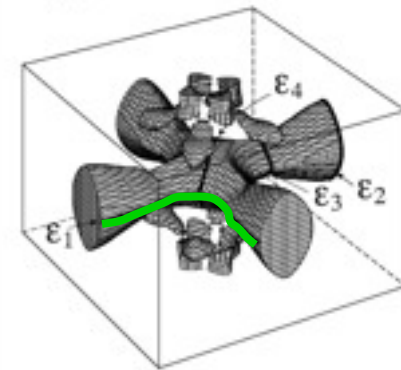
# T-dep Fermi surface-topological change



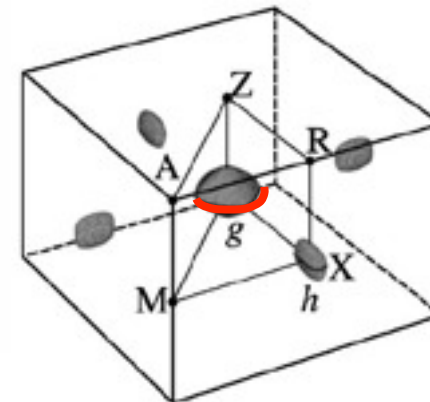
Fermi surface in the  $\Gamma$  plane



high -T

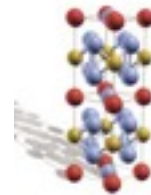


low -T

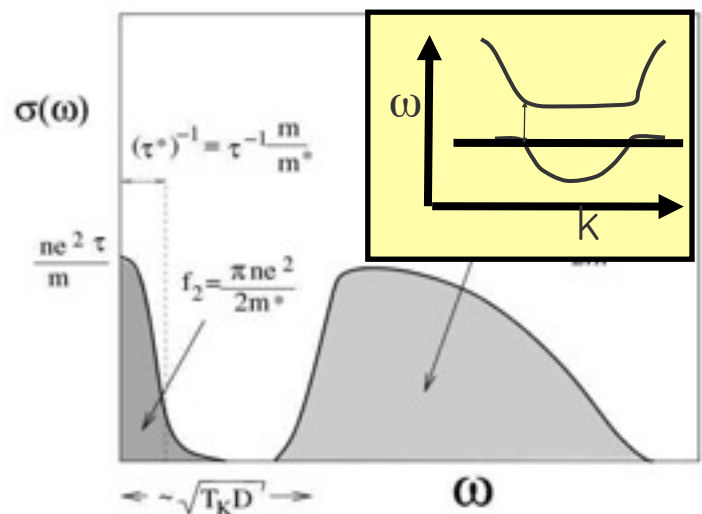


H.C. Choi, B.I. Min, J.H. Shim, K. Haule, G. Kotliar,  
Phys. Rev. Lett. **108**, 016402 (2012).

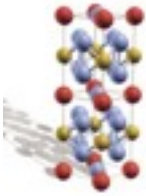
# Optical conductivity



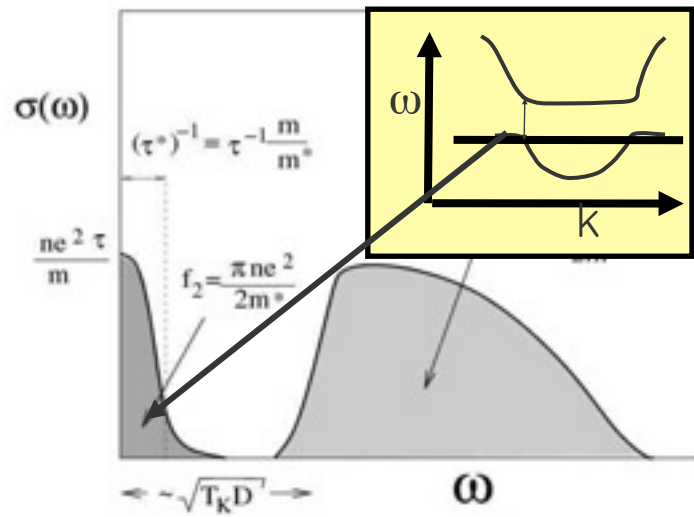
Typical heavy fermion at low T:



# Optical conductivity

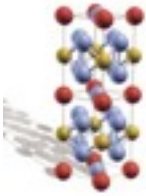


Typical heavy fermion at low T:

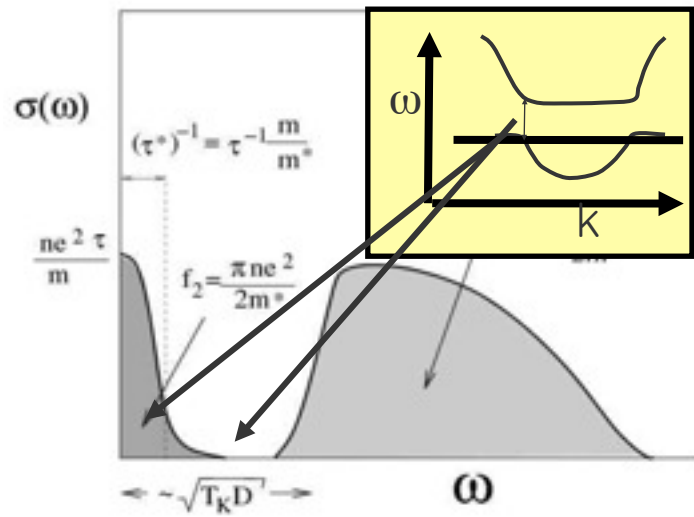


Narrow Drude peak (narrow q.p. band)

# Optical conductivity



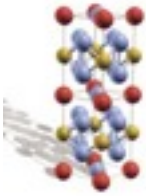
Typical heavy fermion at low T:



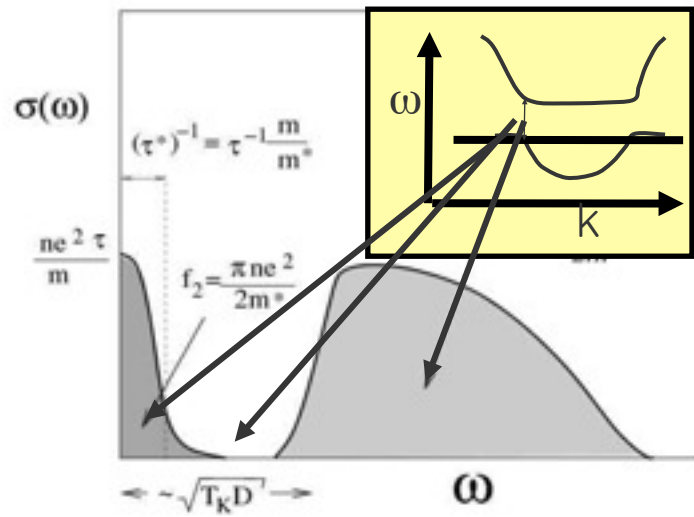
Narrow Drude peak (narrow q.p. band)

Hybridization gap

# Optical conductivity



Typical heavy fermion at low T:



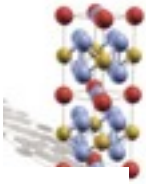
Narrow Drude peak (narrow q.p. band)

Hybridization gap

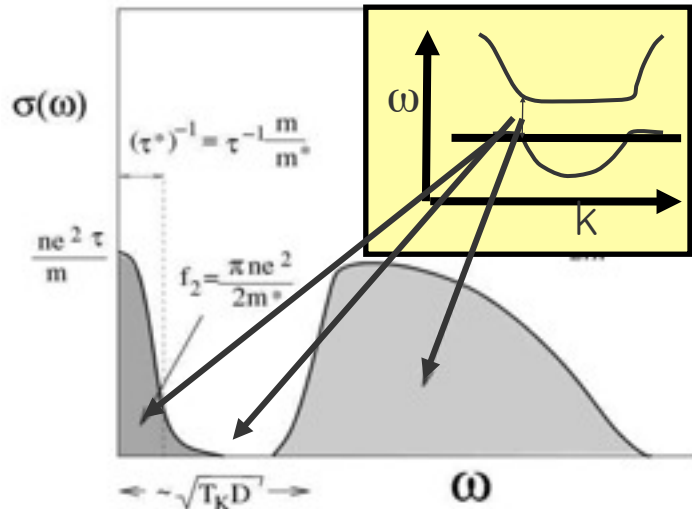
Interband transitions across  
hybridization gap  $\rightarrow$  mid IR peak



# Optical conductivity



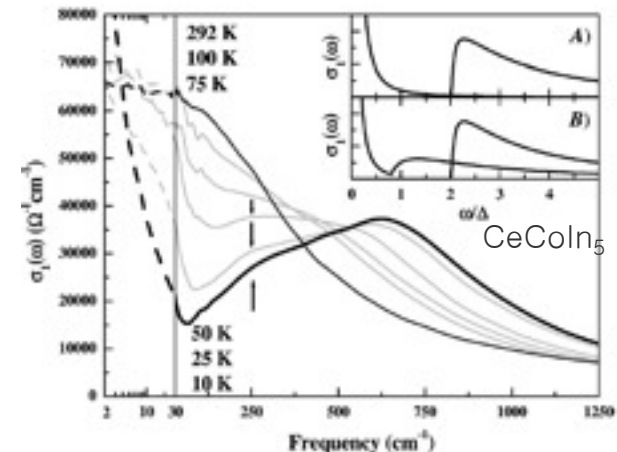
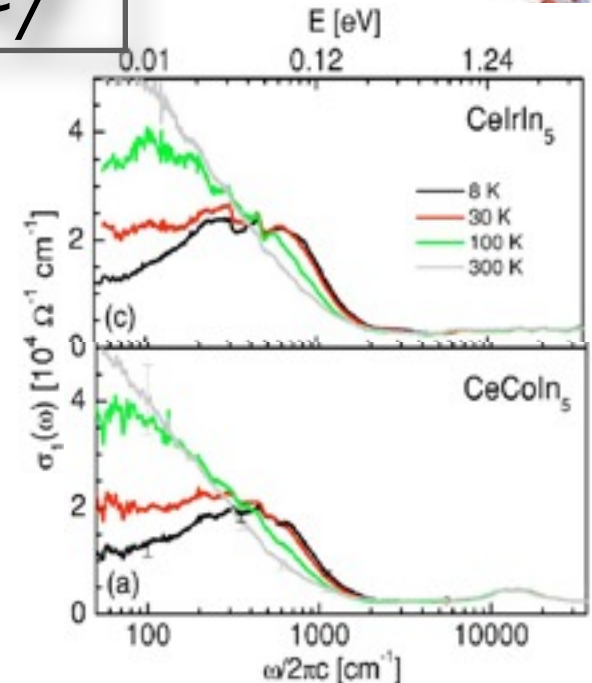
Typical heavy fermion at low T:



Narrow Drude peak (narrow q.p. band)

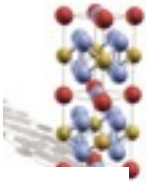
Hybridization gap

Interband transitions across hybridization gap  $\rightarrow$  mid IR peak

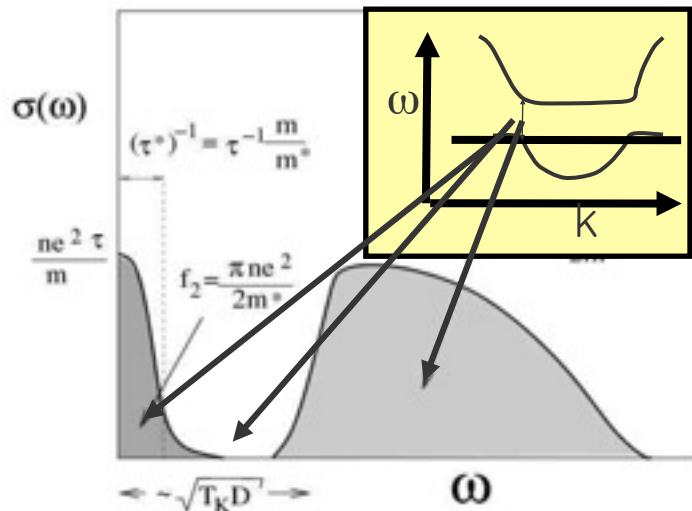


F.P. Mena & D. Van der Marel, 2005 | E.J. Singley & D.N Basov, 2002

# Optical conductivity



Typical heavy fermion at low T:

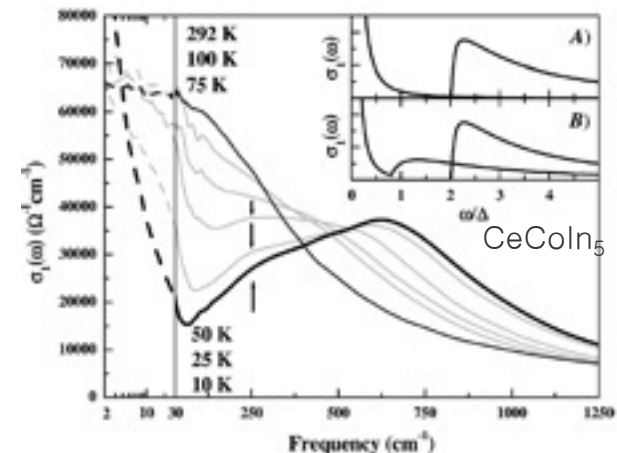
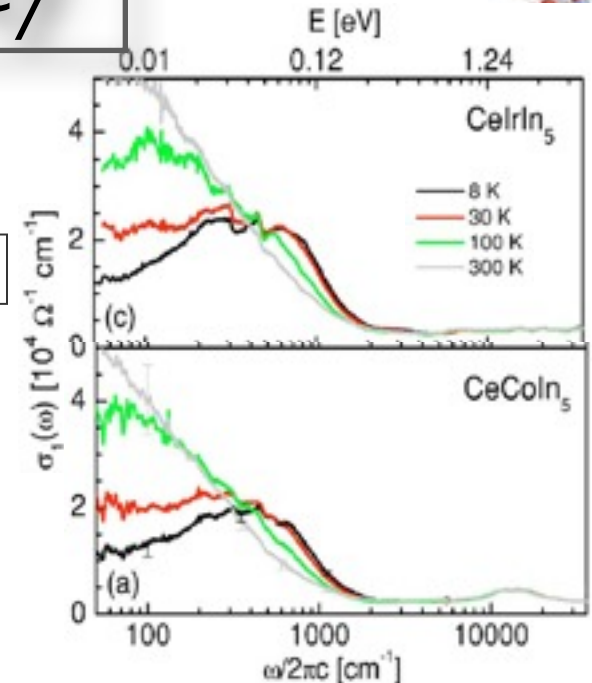


no visible Drude peak

Narrow Drude peak (narrow q.p. band)

Hybridization gap

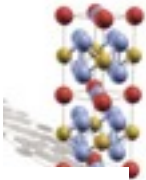
Interband transitions across hybridization gap  $\rightarrow$  mid IR peak



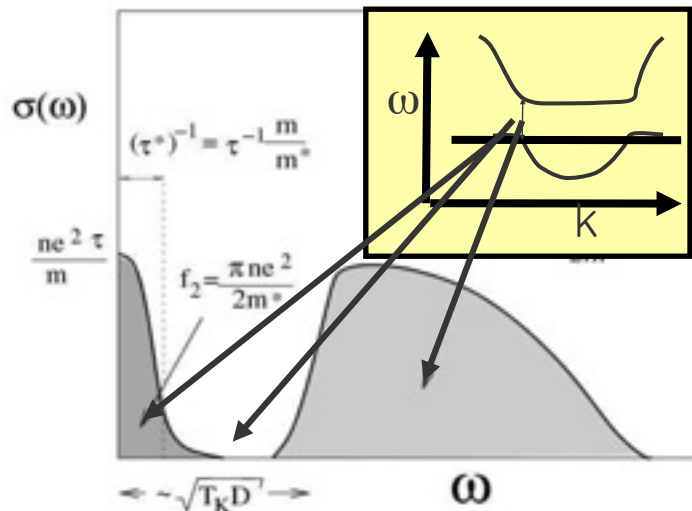
F.P. Mena & D. Van der Marel, 2005

E.J. Singley & D.N. Basov, 2002

# Optical conductivity



Typical heavy fermion at low T:



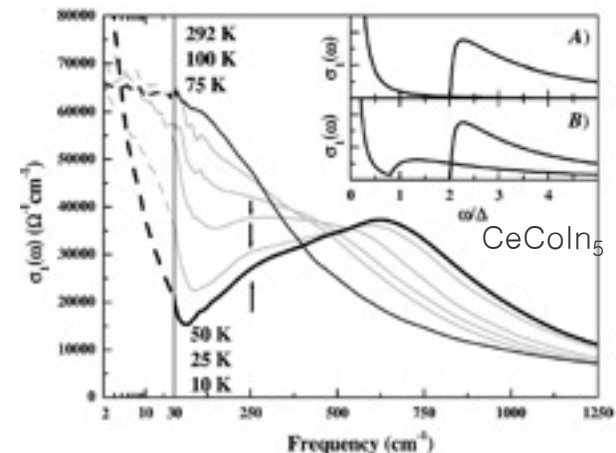
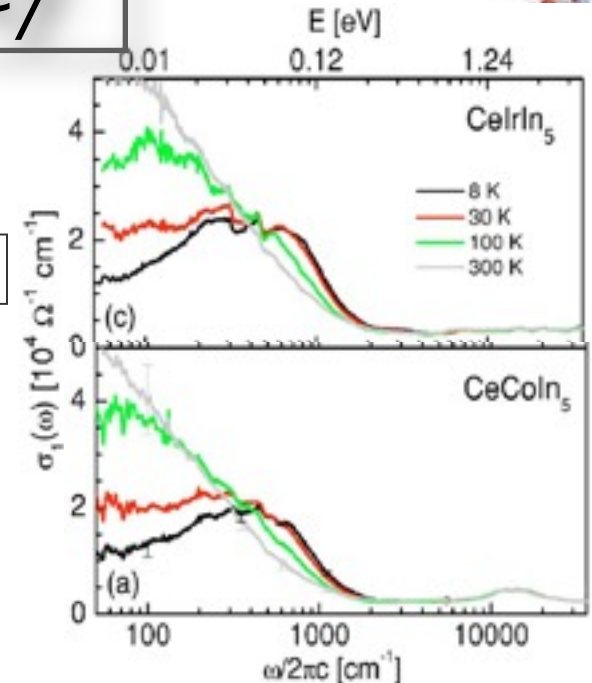
no visible Drude peak

no sharp hybridization gap

Narrow Drude peak (narrow q.p. band)

Hybridization gap

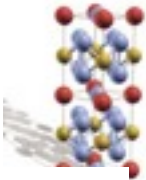
Interband transitions across hybridization gap  $\rightarrow$  mid IR peak



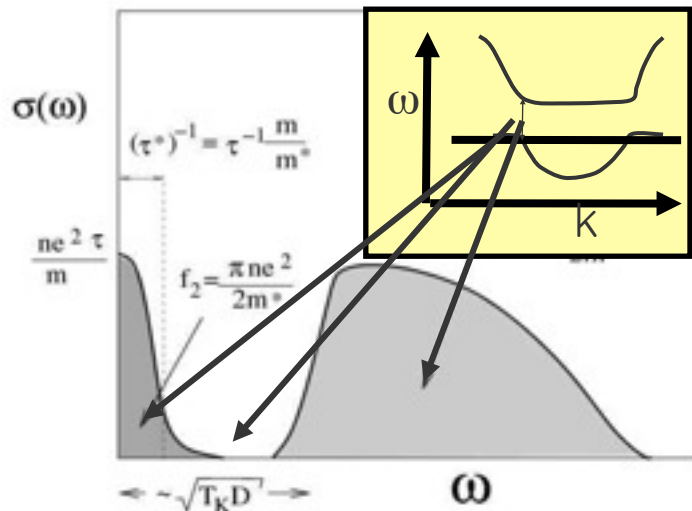
F.P. Mena & D. Van der Marel, 2005

E.J. Singley & D.N. Basov, 2002

# Optical conductivity



Typical heavy fermion at low T:



no visible Drude peak

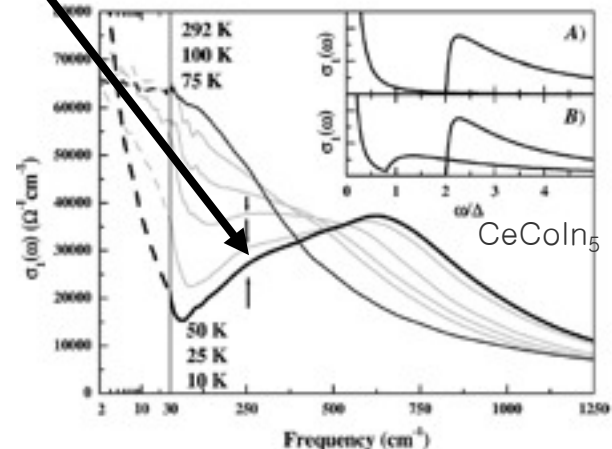
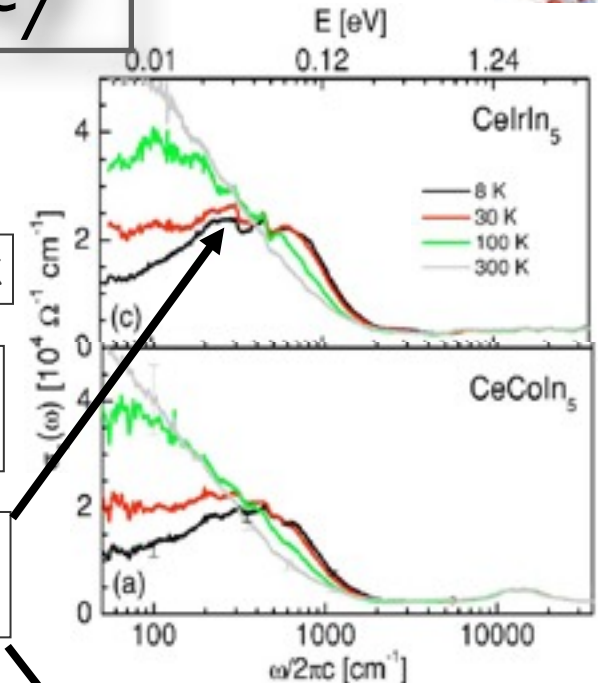
no sharp hybridization gap

first mid-IR peak at  $250 \text{ cm}^{-1}$

Narrow Drude peak (narrow q.p. band)

Hybridization gap

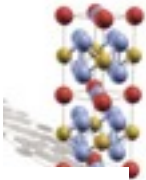
Interband transitions across hybridization gap  $\rightarrow$  mid IR peak



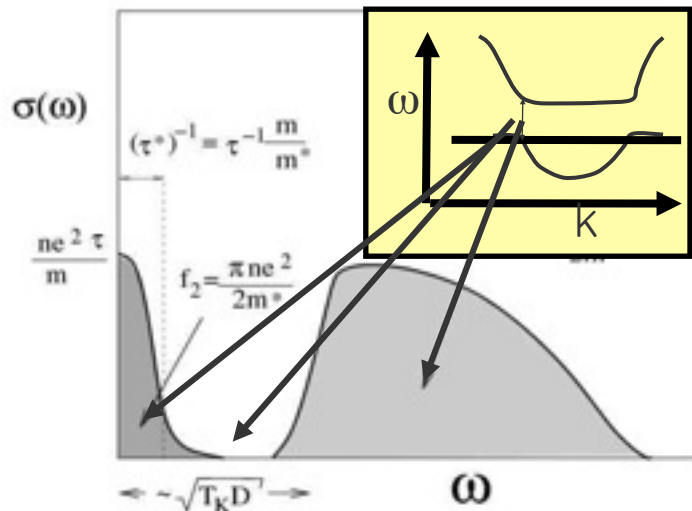
F.P. Mena & D. Van der Marel, 2005

E.J. Singley & D.N. Basov, 2002

# Optical conductivity



Typical heavy fermion at low T:



no visible Drude peak

no sharp hybridization gap

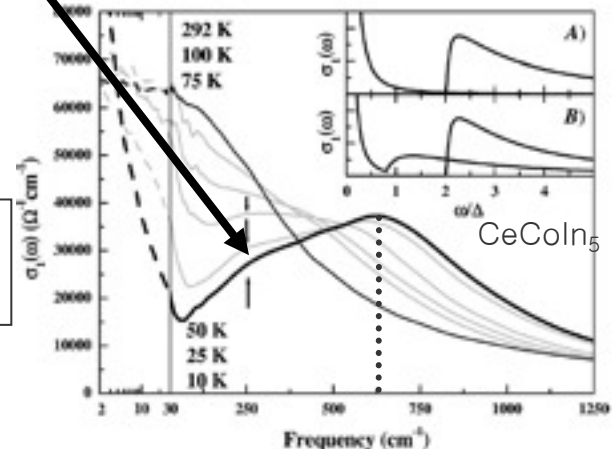
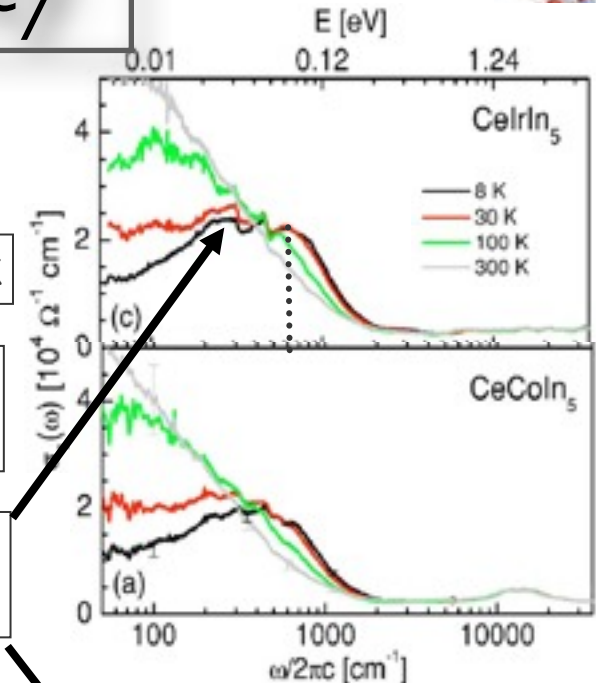
first mid-IR peak at  $250 \text{ cm}^{-1}$

Narrow Drude peak (narrow q.p. band)

Hybridization gap

Interband transitions across hybridization gap  $\rightarrow$  mid IR peak

second mid IR peak at  $600 \text{ cm}^{-1}$

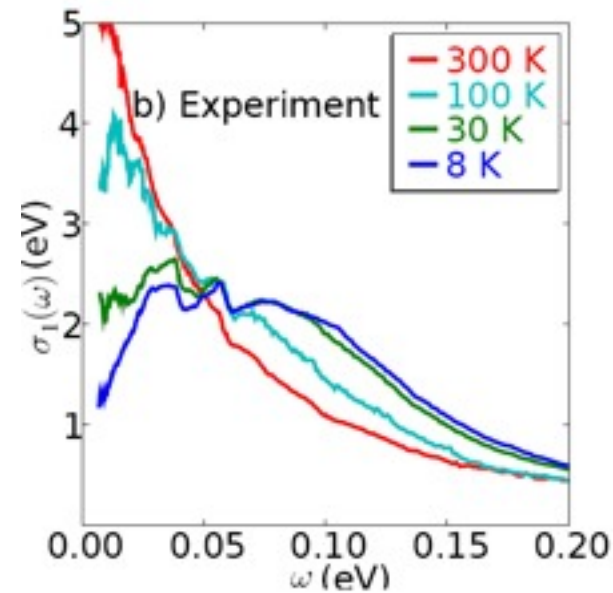
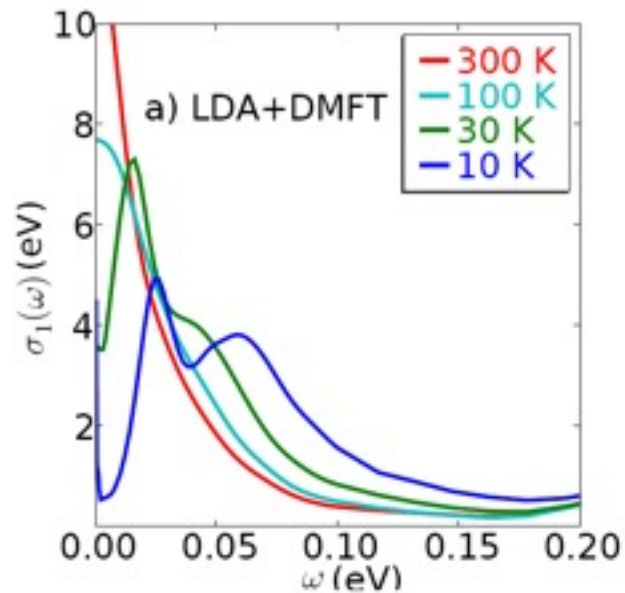
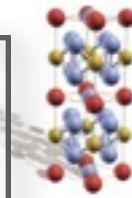


F.P. Mena & D. Van der Marel, 2005

E.J. Singley & D.N. Basov, 2002

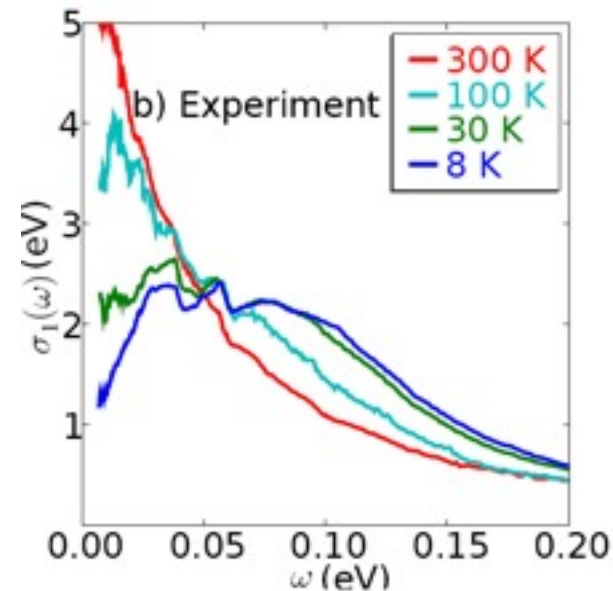
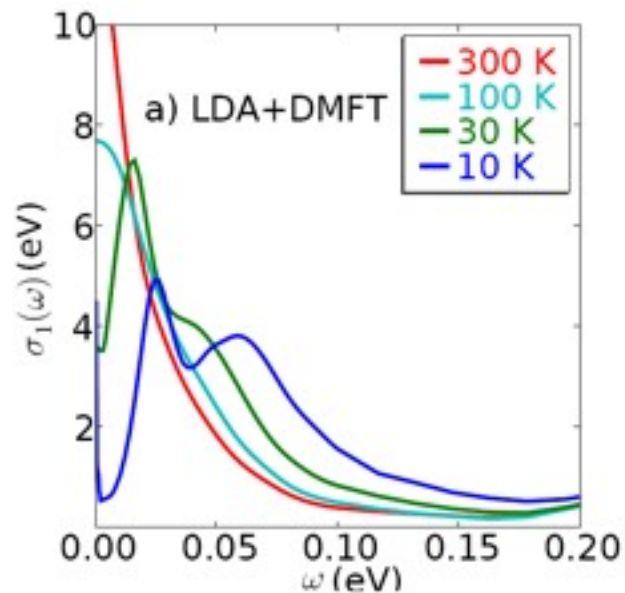
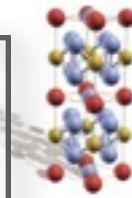


# Optical conductivity in LDA+DMFT



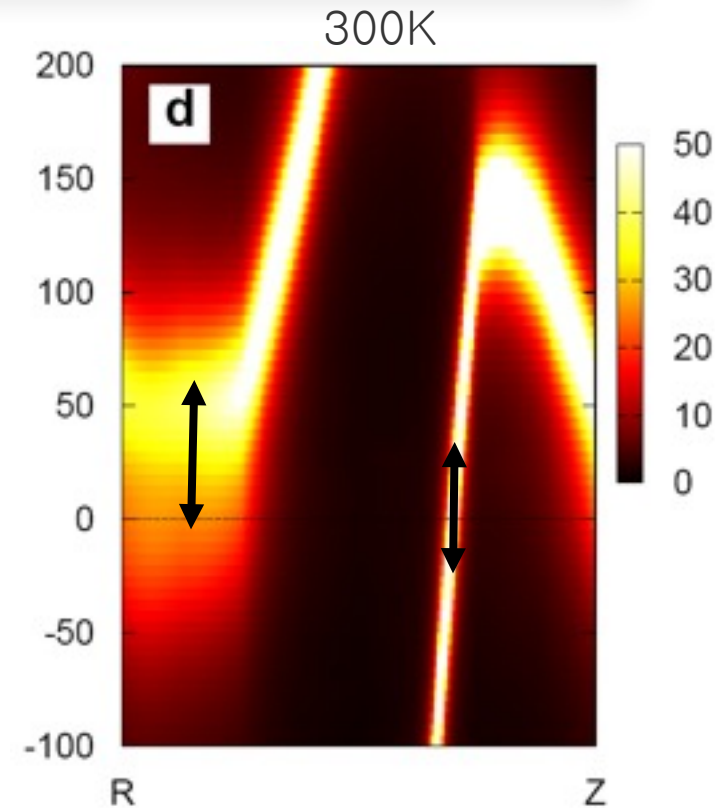
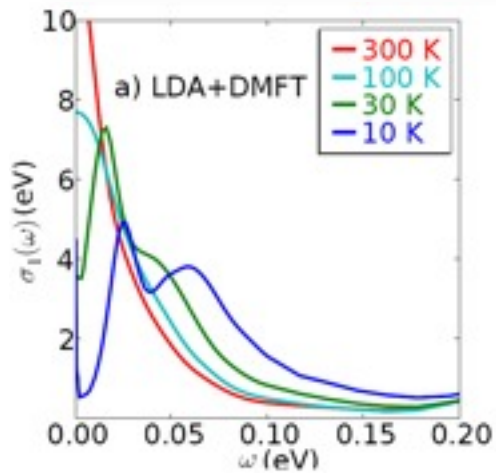
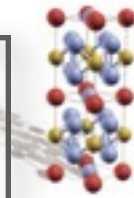


# Optical conductivity in LDA+DMFT

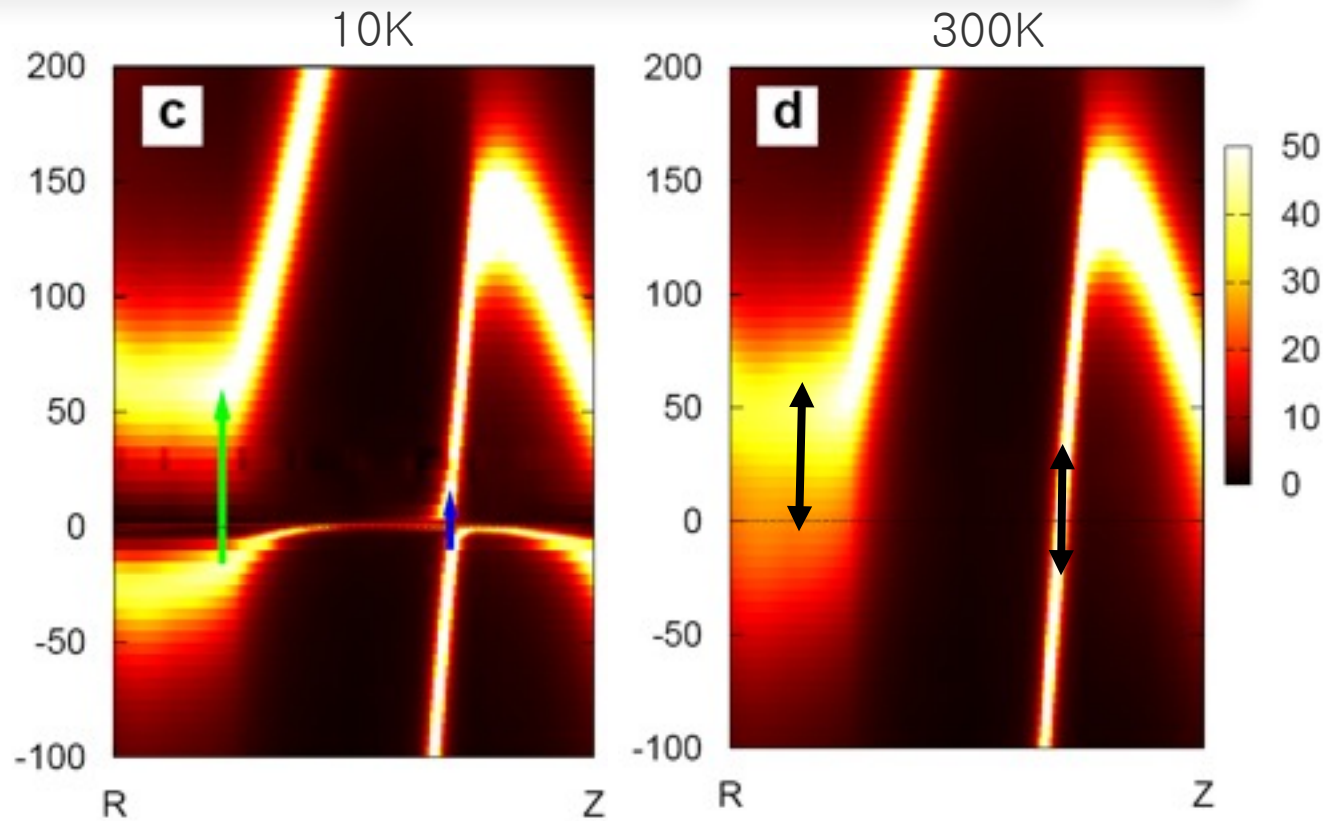
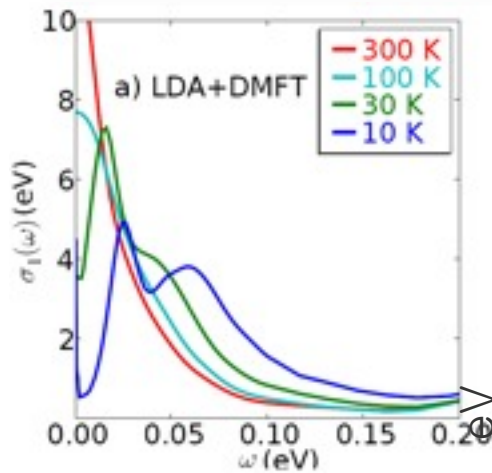


- At 300 K very broad Drude peak (e-e scattering, spd lifetime  $\sim 0.1$  eV)
- At 10 K:
  - very narrow Drude peak
  - First MI peak at  $0.03 \text{ eV} \sim 250 \text{ cm}^{-1}$
  - Second MI peak at  $0.07 \text{ eV} \sim 600 \text{ cm}^{-1}$

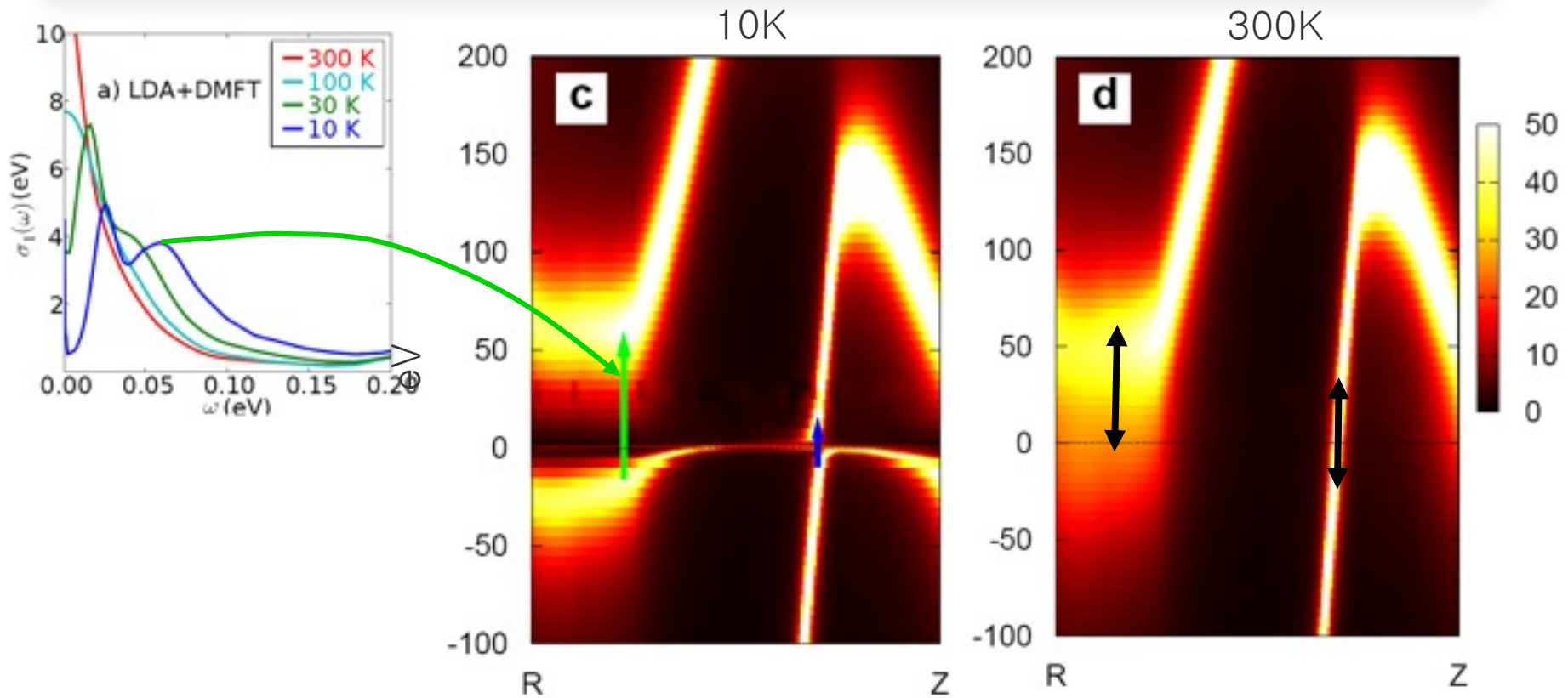
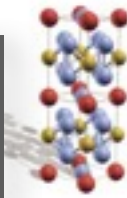
# Multiple hybridization gaps



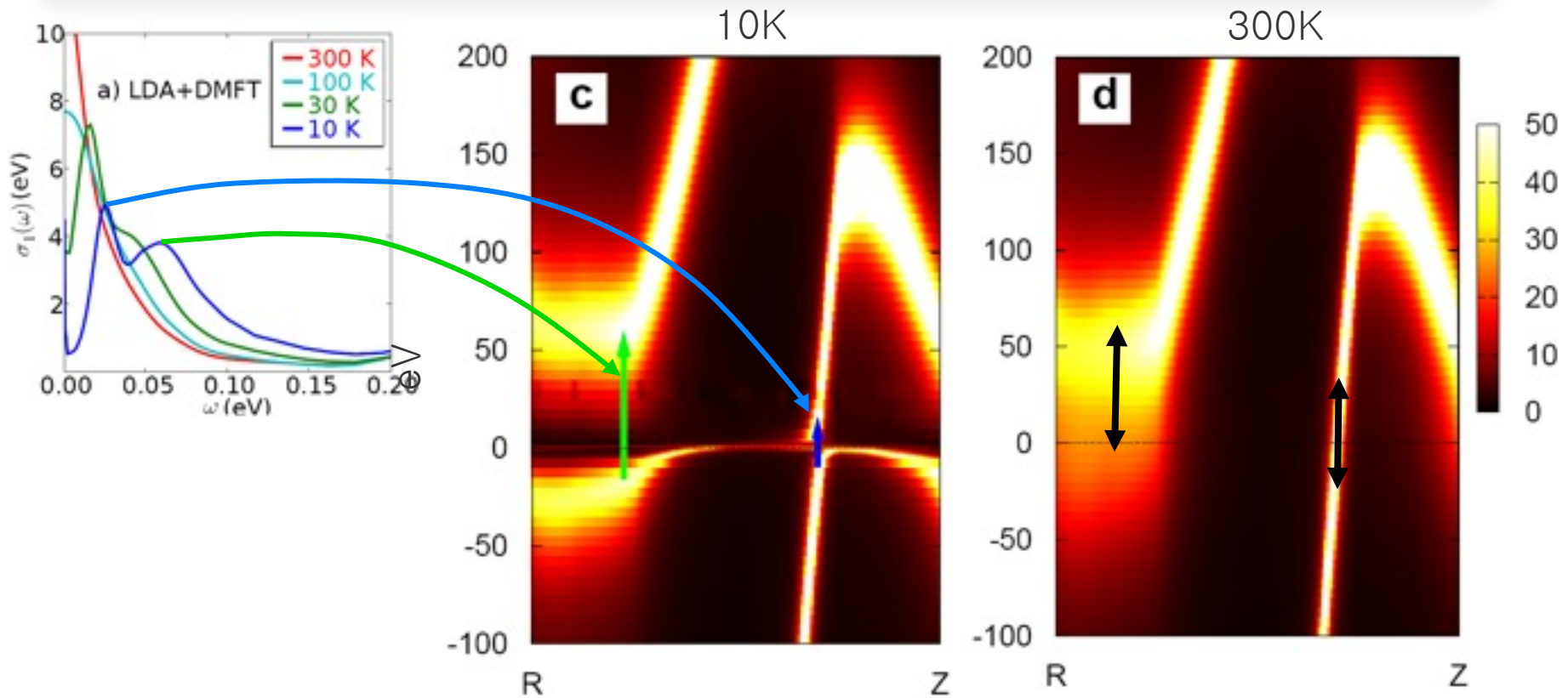
# Multiple hybridization gaps



# Multiple hybridization gaps

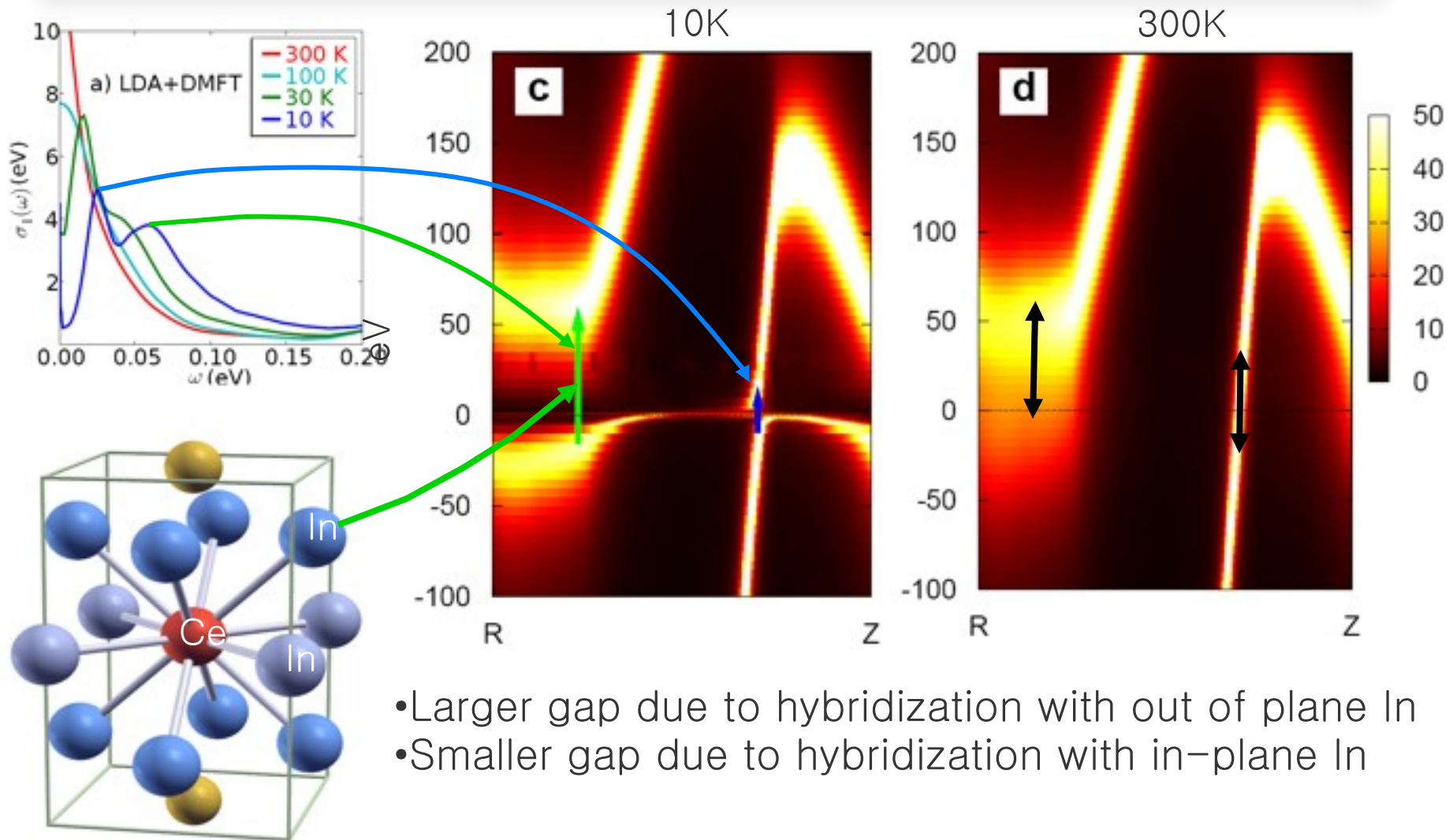
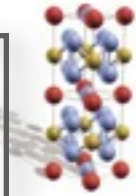


# Multiple hybridization gaps



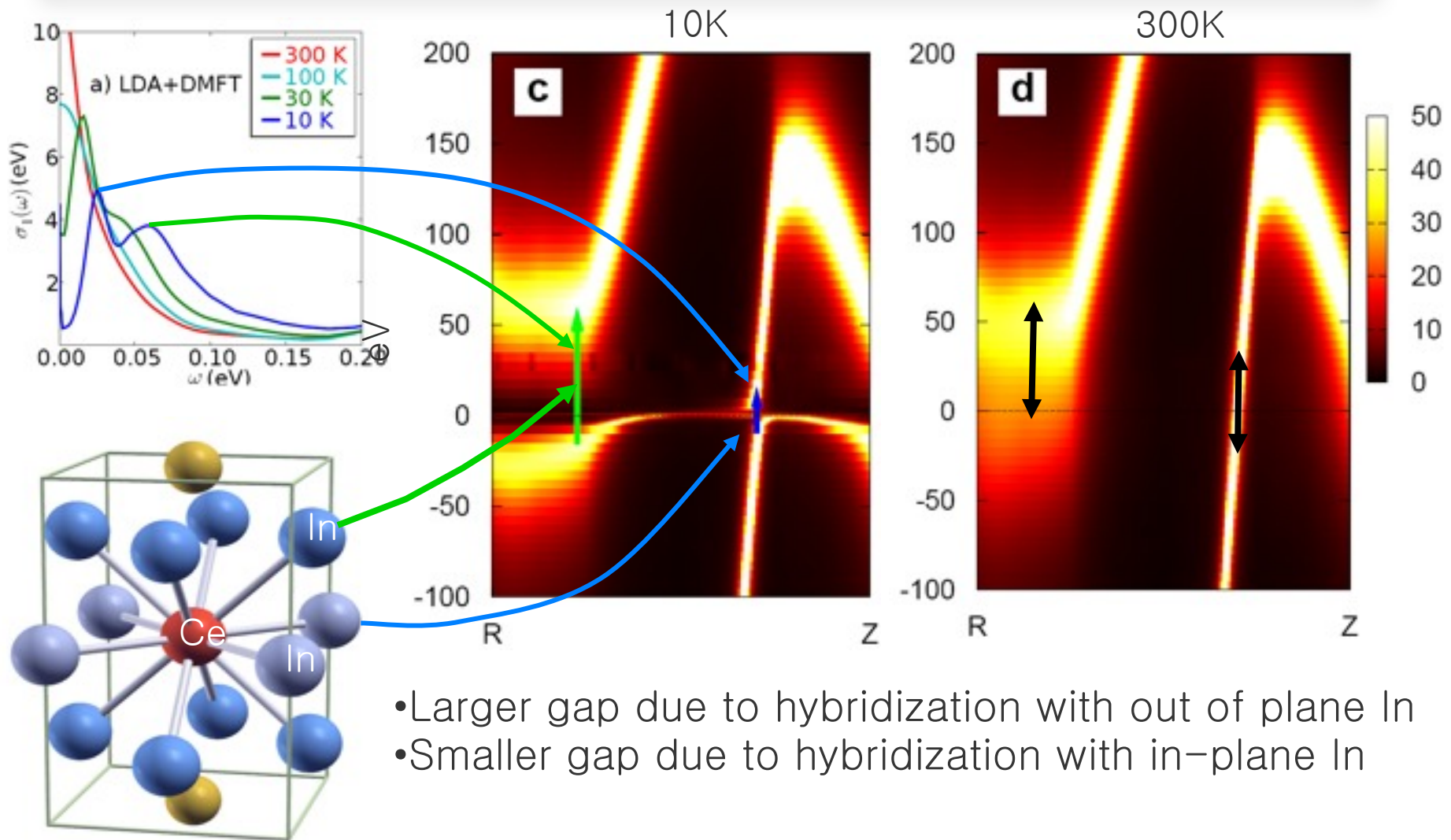
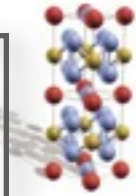


# Multiple hybridization gaps

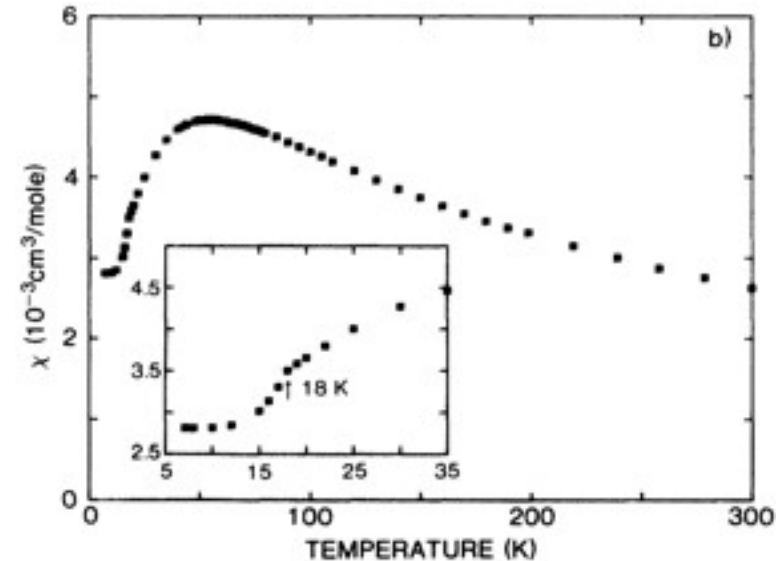
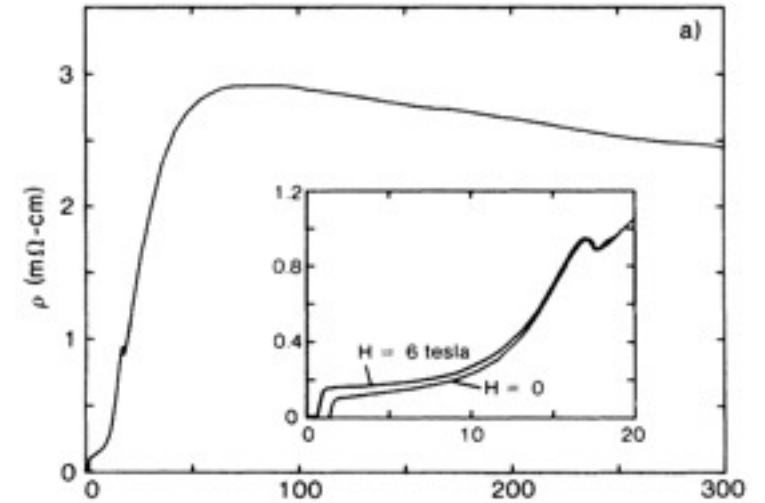
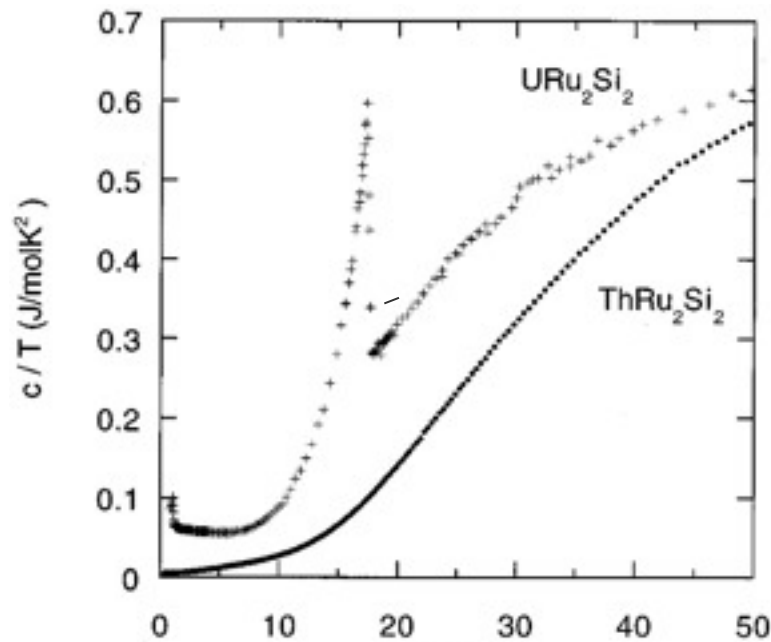
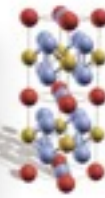




# Multiple hybridization gaps

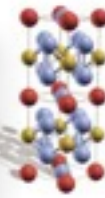


# URu<sub>2</sub>Si<sub>2</sub> heavy fermion with hidden order

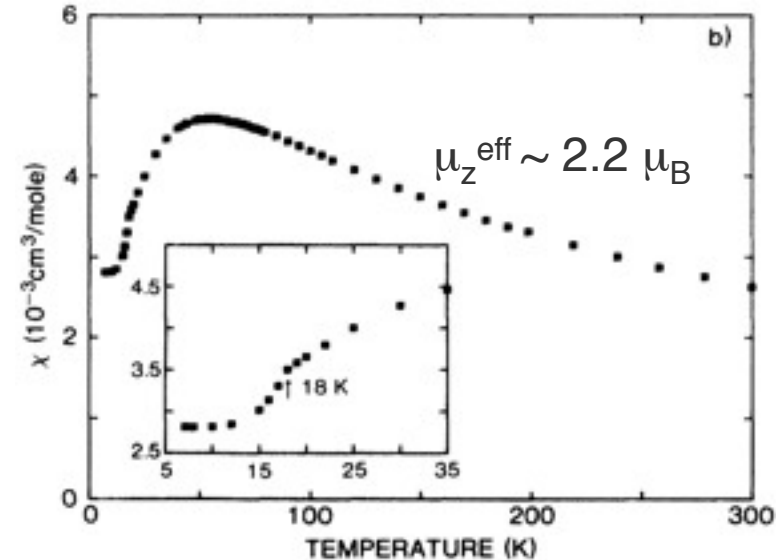
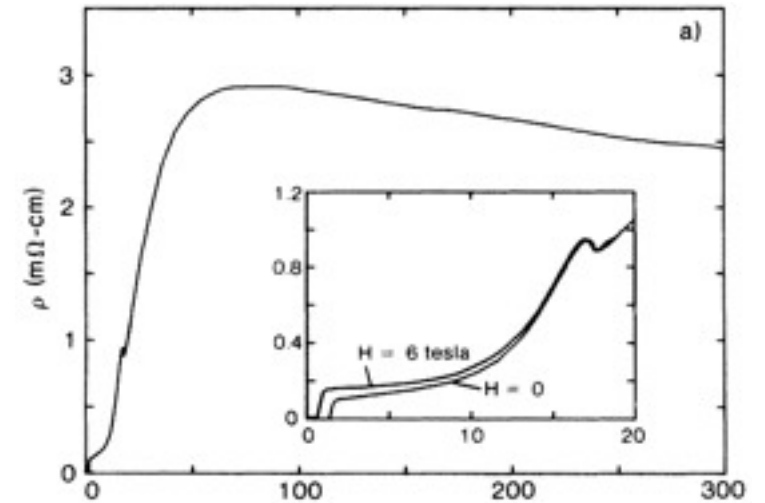
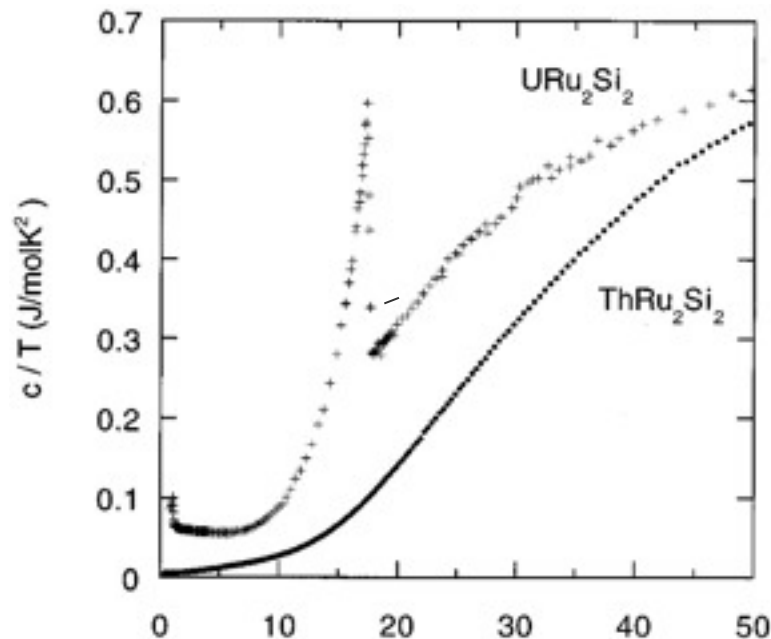


N. H. van Dijk, PRB 56, 14493 (1997).

# URu<sub>2</sub>Si<sub>2</sub> heavy fermion with hidden order

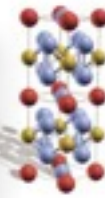


Curie-Weiss:  $\mu_z^{\text{eff}} \sim 2.2 \mu_B$



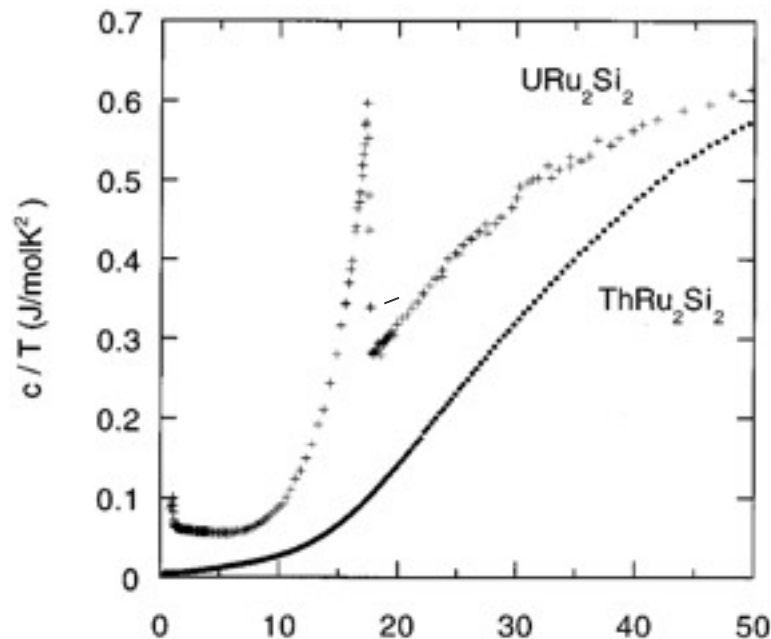
N. H. van Dijk, PRB 56, 14493 (1997).

# URu<sub>2</sub>Si<sub>2</sub> heavy fermion with hidden order

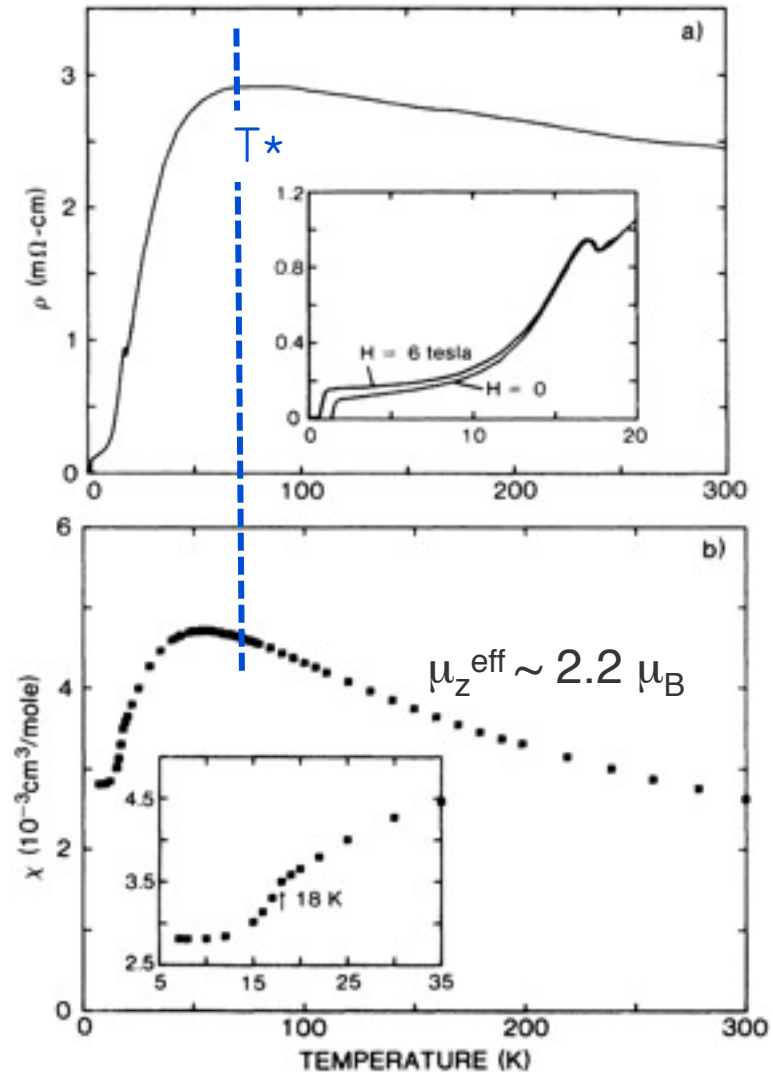


Curie-Weiss:  $\mu_z^{\text{eff}} \sim 2.2 \mu_B$

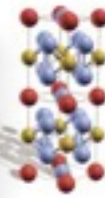
Coherence:  $T^* \sim 70\text{K}$



N. H. van Dijk, PRB 56, 14493 (1997).



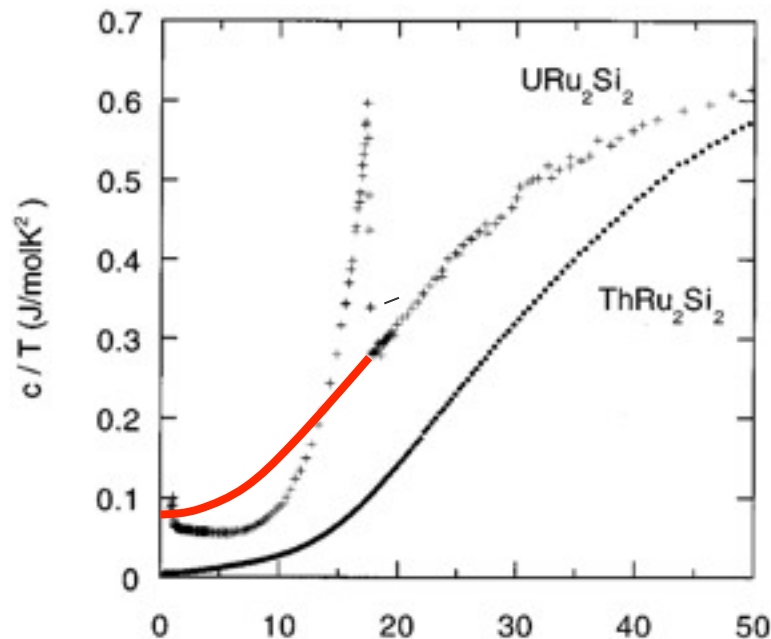
# URu<sub>2</sub>Si<sub>2</sub> heavy fermion with hidden order



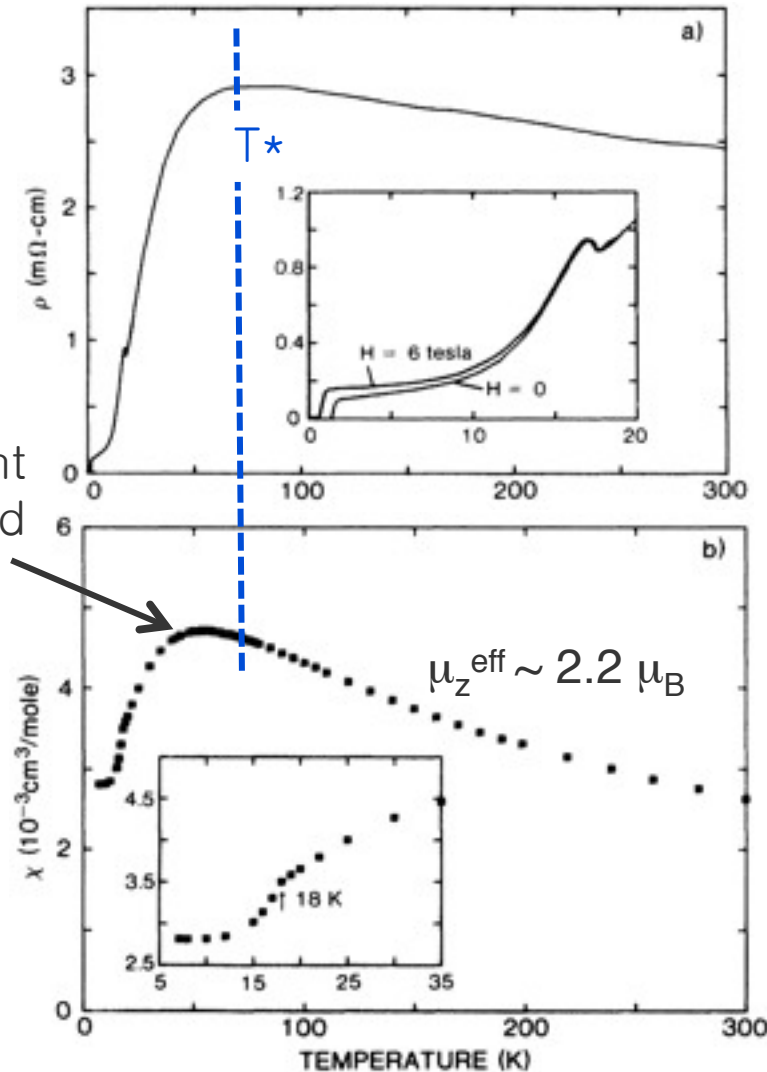
Curie-Weiss:  $\mu_z^{\text{eff}} \sim 2.2 \mu_B$

*Elec. cv:*  $\gamma \sim 70 \text{ mJ/mol K}^2$

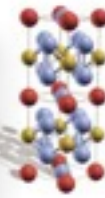
Coherence:  $T^* \sim 70 \text{ K}$



N. H. van Dijk, PRB 56, 14493 (1997).



# URu<sub>2</sub>Si<sub>2</sub> heavy fermion with hidden order



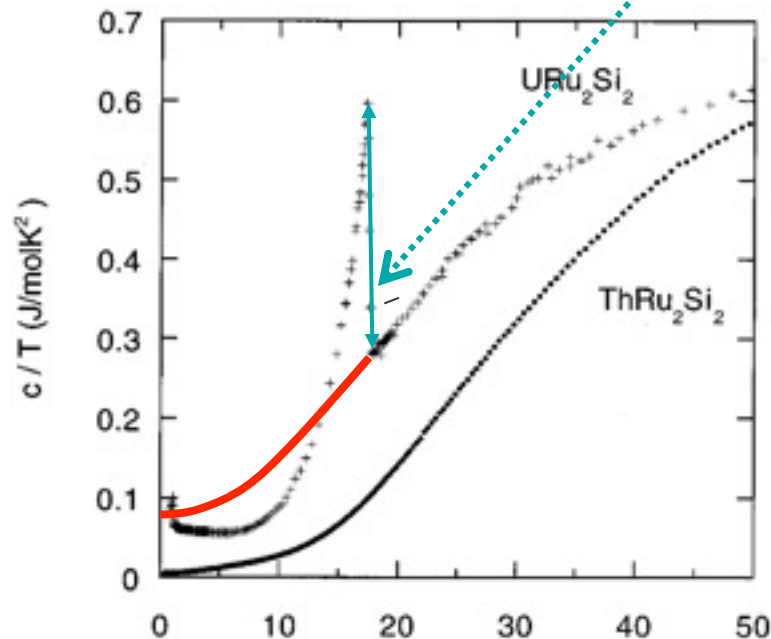
Curie-Weiss:  $\mu_z^{\text{eff}} \sim 2.2 \mu_B$

Second order phase transition

*Elec. cv:*  $\gamma \sim 70 \text{ mJ/mol K}^2$

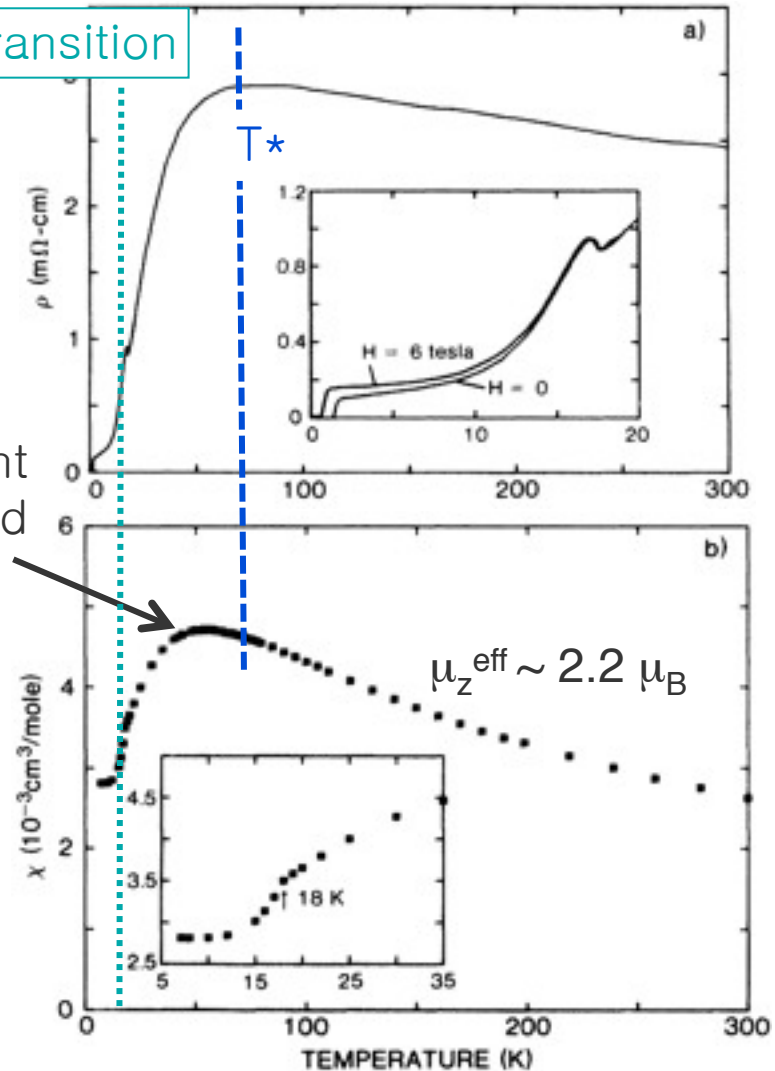
Coherence:  $T^* \sim 70 \text{ K}$

SOPT:  $T_0 \sim 17.8 \text{ K}$



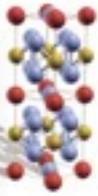
N. H. van Dijk, PRB 56, 14493 (1997).

Moment screened



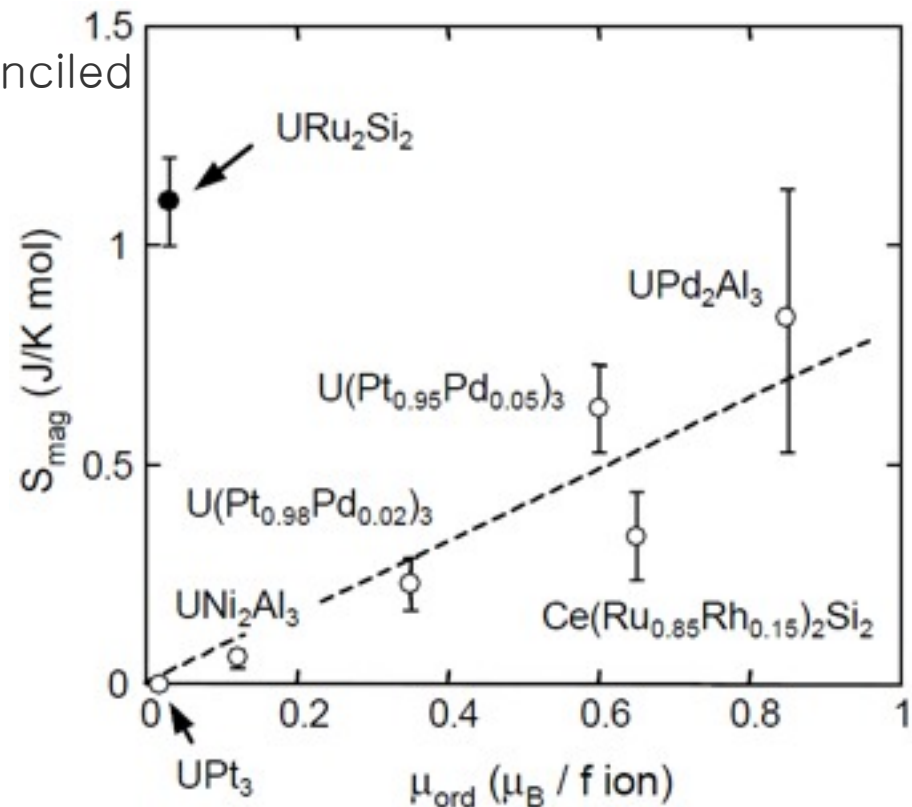


# Hidden Order: The CMT dark matter problem

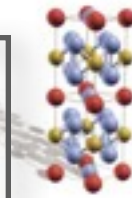


- Moment is tiny  
(likely small admixture of AFM phase)
- Large loss of entropy can not be reconciled  
by small moment
- Some other symmetry breaks.  
Hidden order parameter

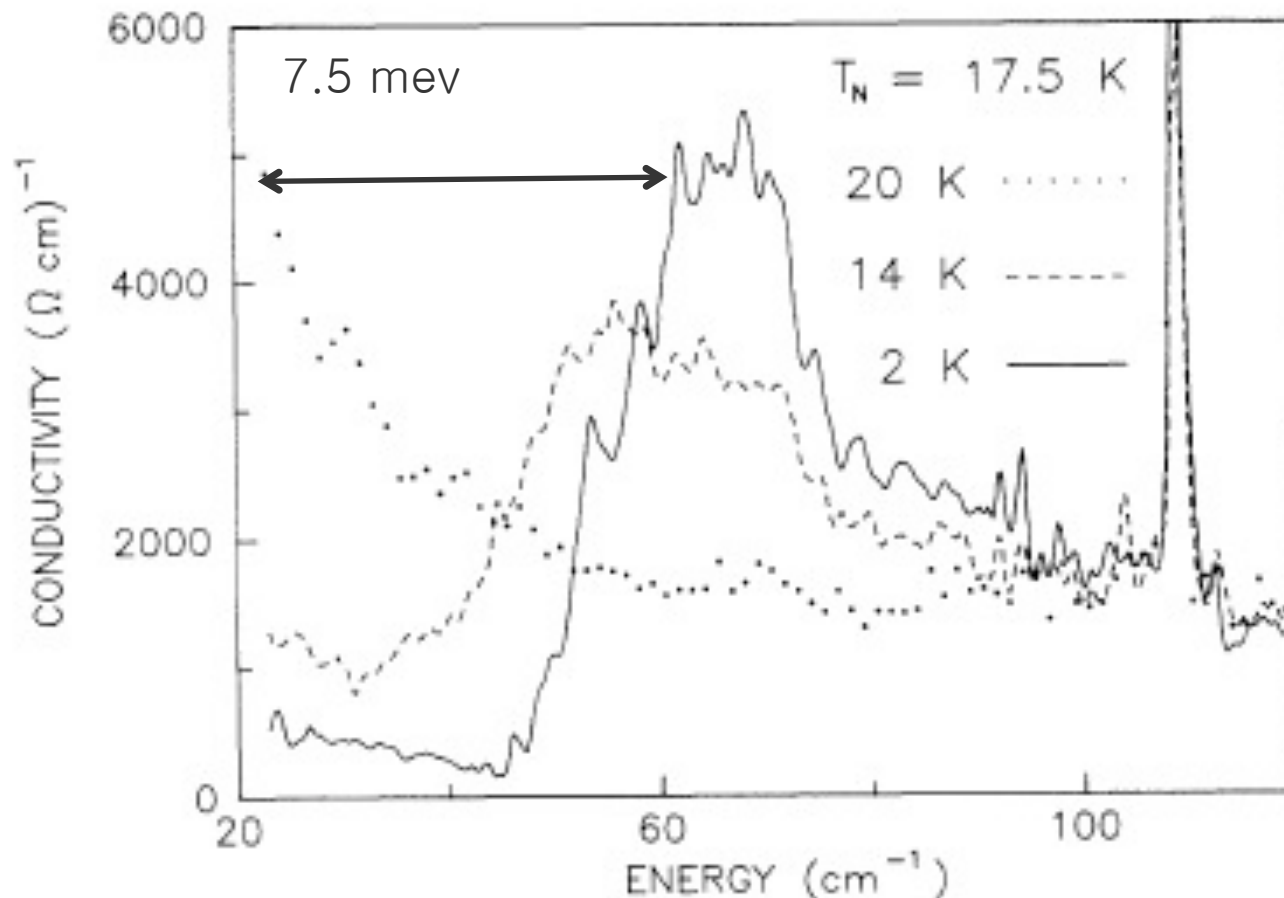
WHICH?



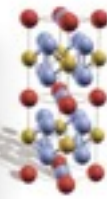
# Optical conductivity



Pseudo-gap opens at  $T_c$ : D. A. Bonn et al. PRL (1988).



# Adiabatic continuity between HO&AFM state



PRL 98, 166404 (2007)

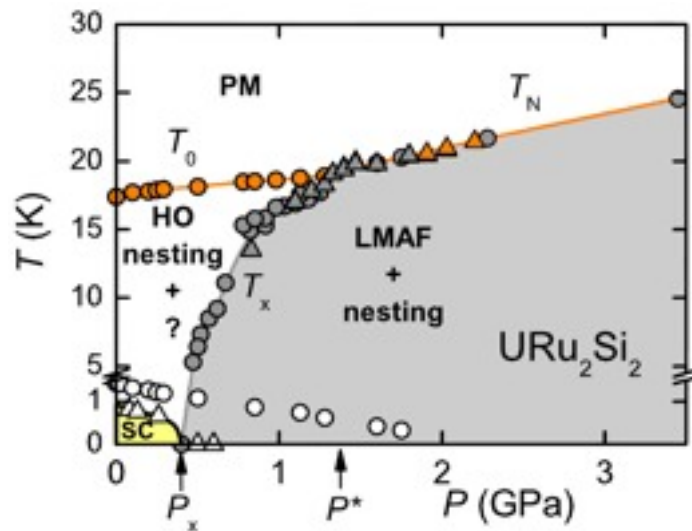
PHYSICAL REVIEW LETTERS

week ending  
20 APRIL 2007

## Field-Induced Fermi Surface Reconstruction and Adiabatic Continuity between Antiferromagnetism and the Hidden-Order State in $\text{URu}_2\text{Si}_2$

Y. J. Jo,<sup>1</sup> L. Balicas,<sup>1</sup> C. Capan,<sup>2</sup> K. Behnia,<sup>3</sup> P. Lejay,<sup>4</sup> J. Flouquet,<sup>5</sup> J. A. Mydosh,<sup>6</sup> and P. Schlottmann<sup>1</sup>

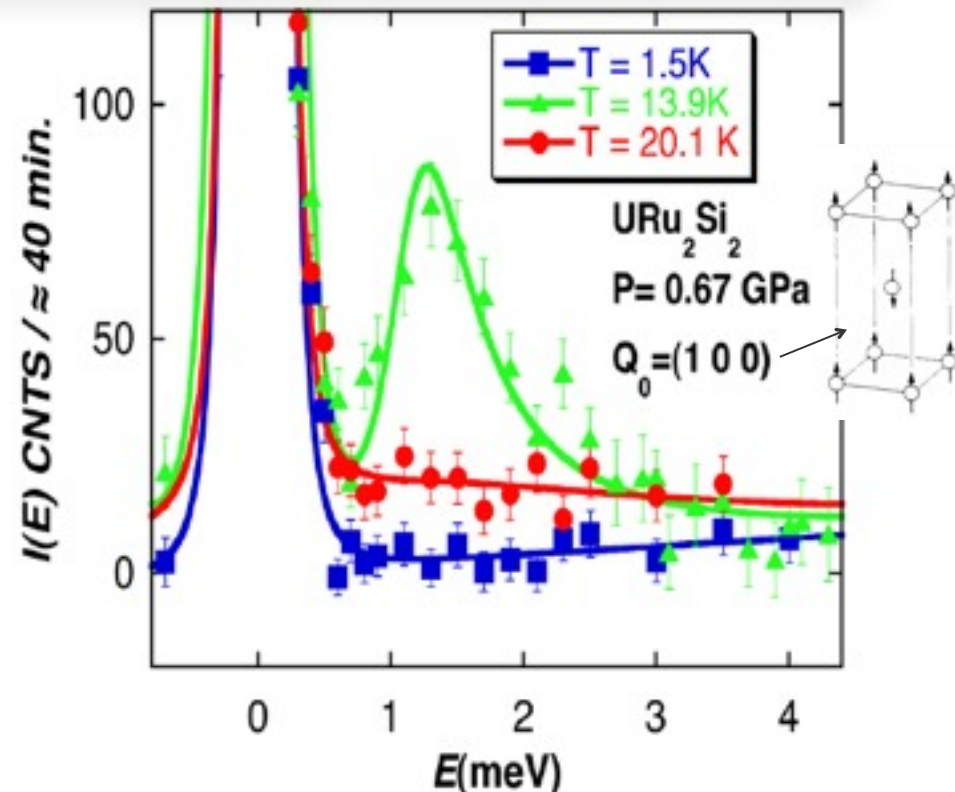
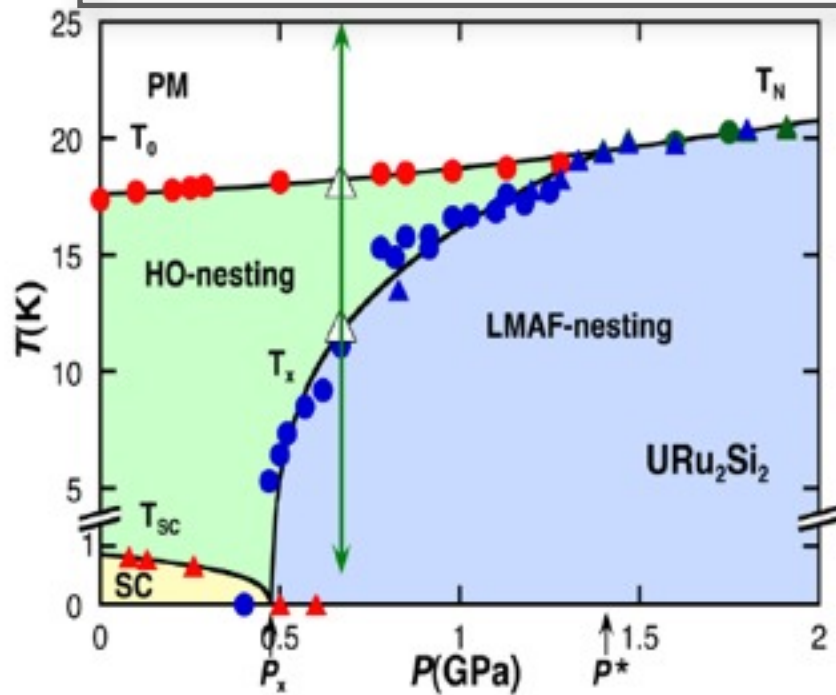
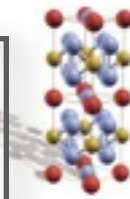
$H - T$  phase diagram. Instead of phase separation between HO and antiferromagnetism our observations indicate adiabatic continuity between both orderings with field and pressure changing their relative weight.



- HO under pressure converted to AFM phase through 1<sup>st</sup> order transition
- Similar  $T_0$  and  $T_N$
- Almost identical thermodynamic quantities (jump in  $C_v$ ), quantum osc

E. Hassinger et.al. PRL 77, 115117 (2008)

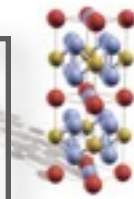
# Key experiment: Neutron scattering



The low energy resonance

A. Villaume, F. Bourdarot, E. Hassinger, S. Raymond, V. Taufour, D. Aoki, and J. Flouquet, PRB 78, 012504 (2008)

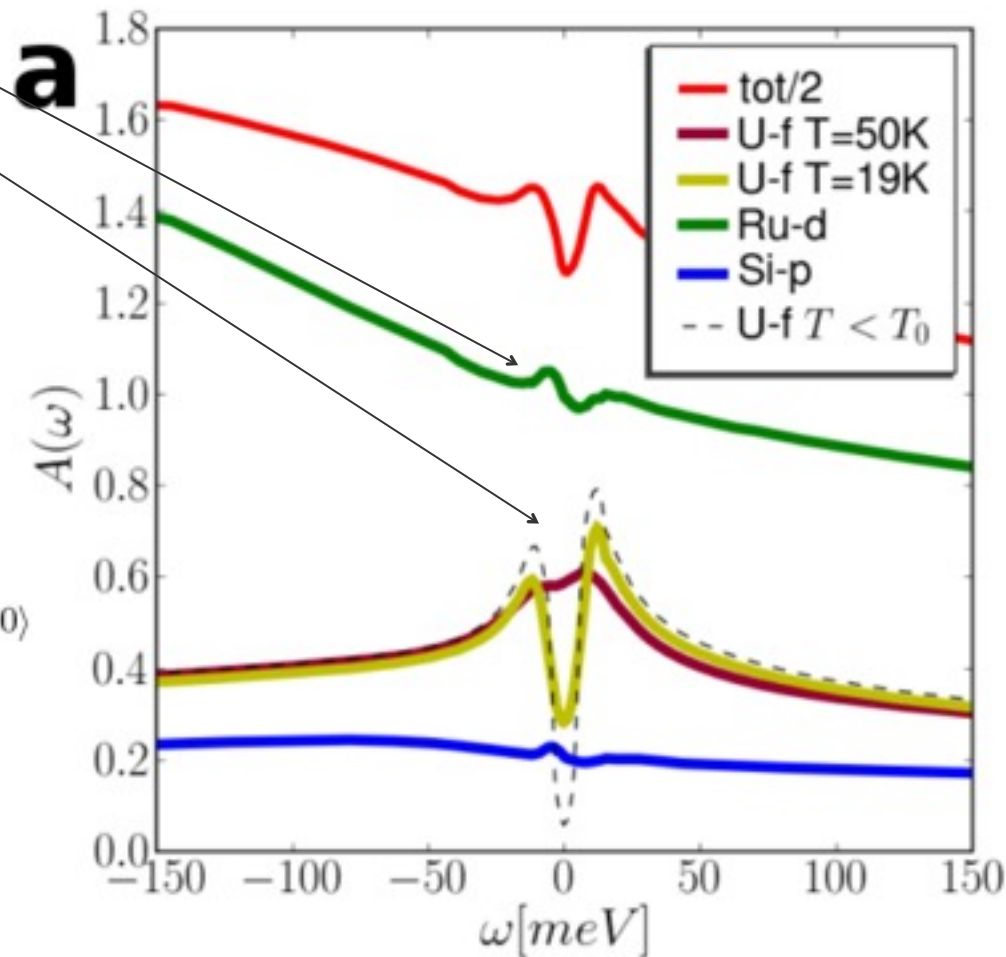
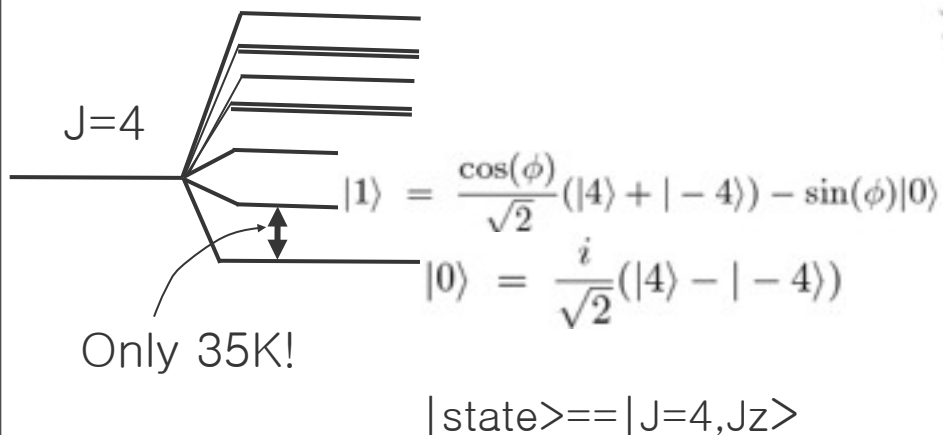
# Origin of gapping?



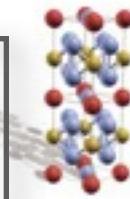
Partial DOS

Small effects on spd electrons  
Large effect on U-f's

Ground state atomic multiplet of  $f^2$   
configuration in tetragonal field



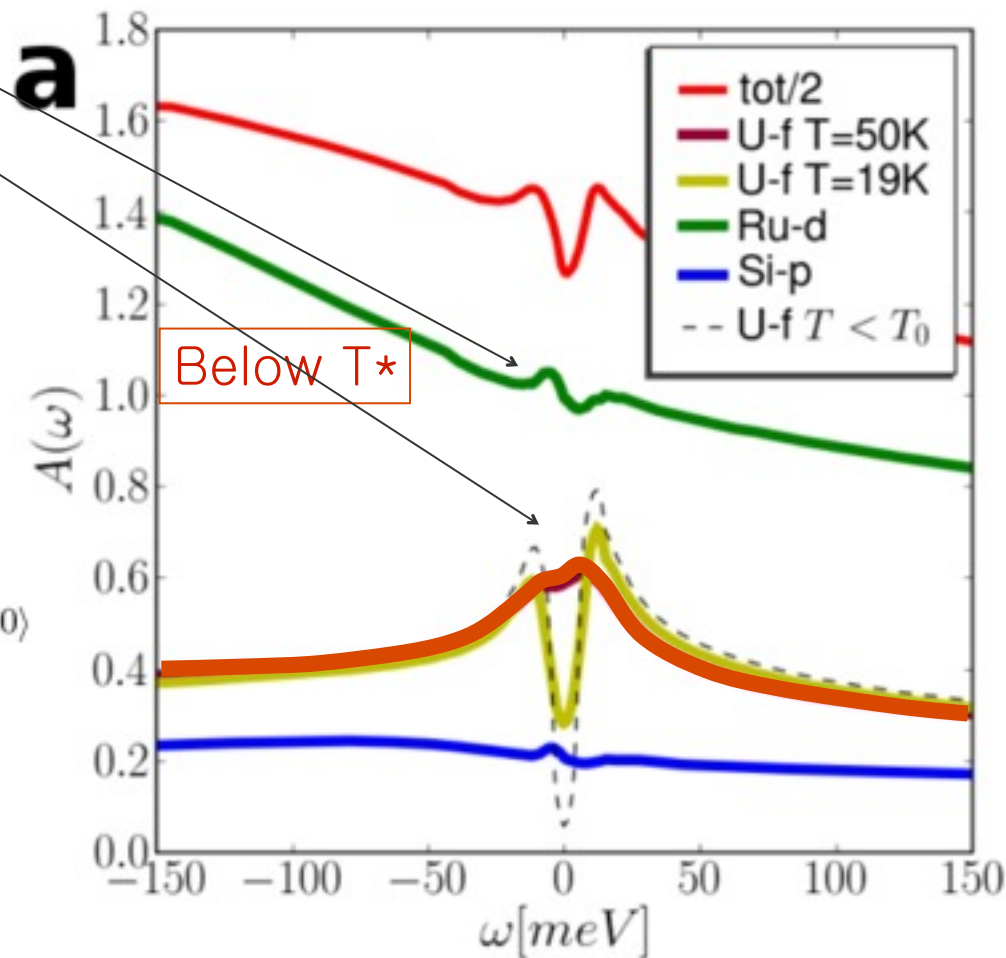
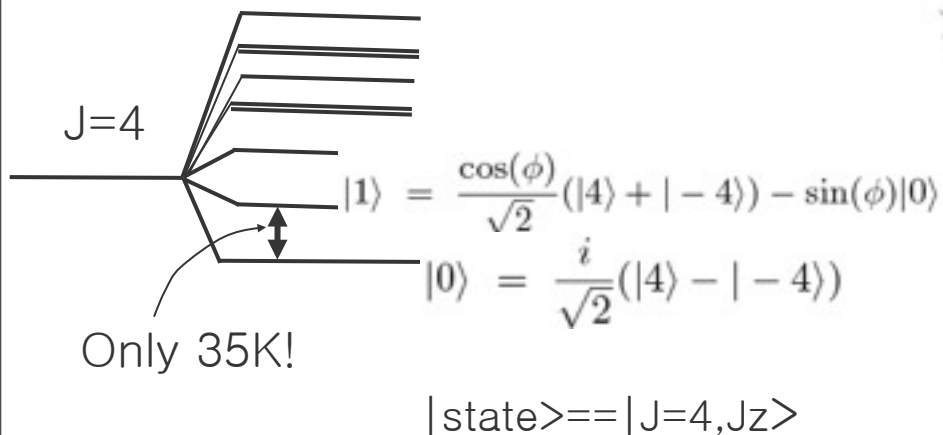
# Origin of gapping?



Partial DOS

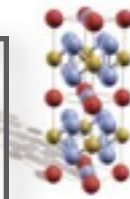
Small effects on spd electrons  
Large effect on U-f's

Ground state atomic multiplet of  $f^2$   
configuration in tetragonal field





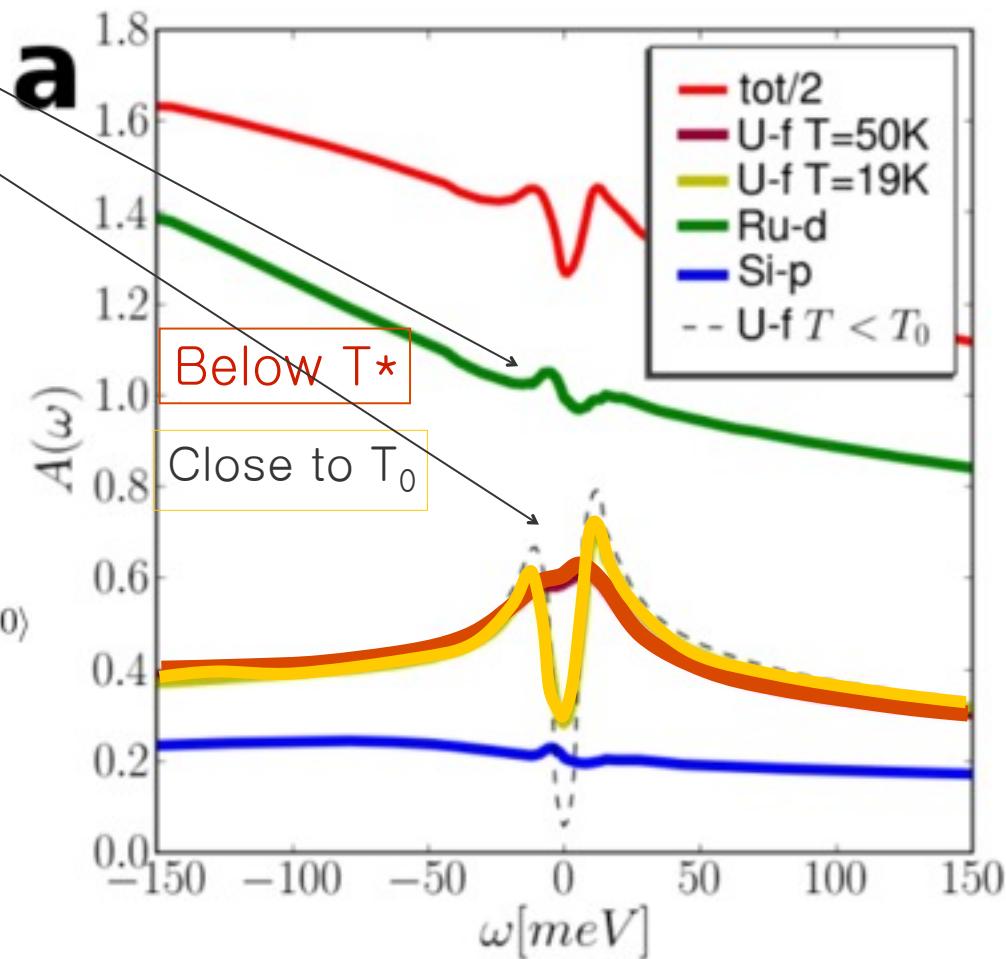
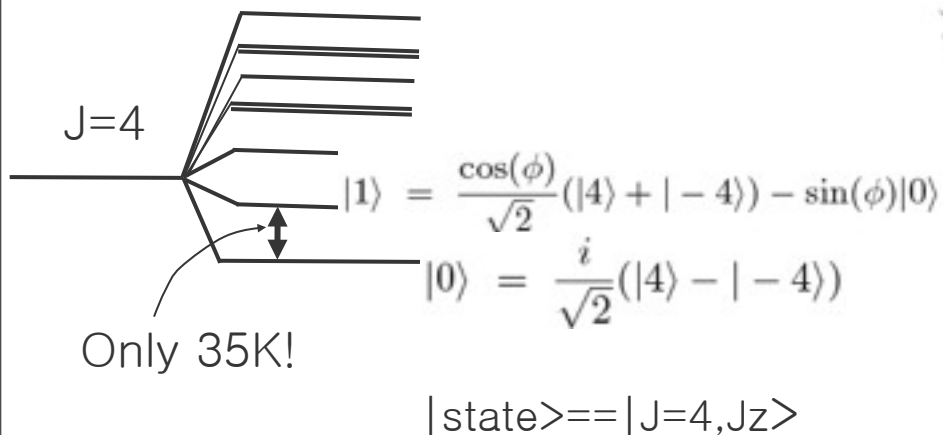
# Origin of gapping?



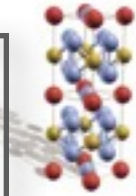
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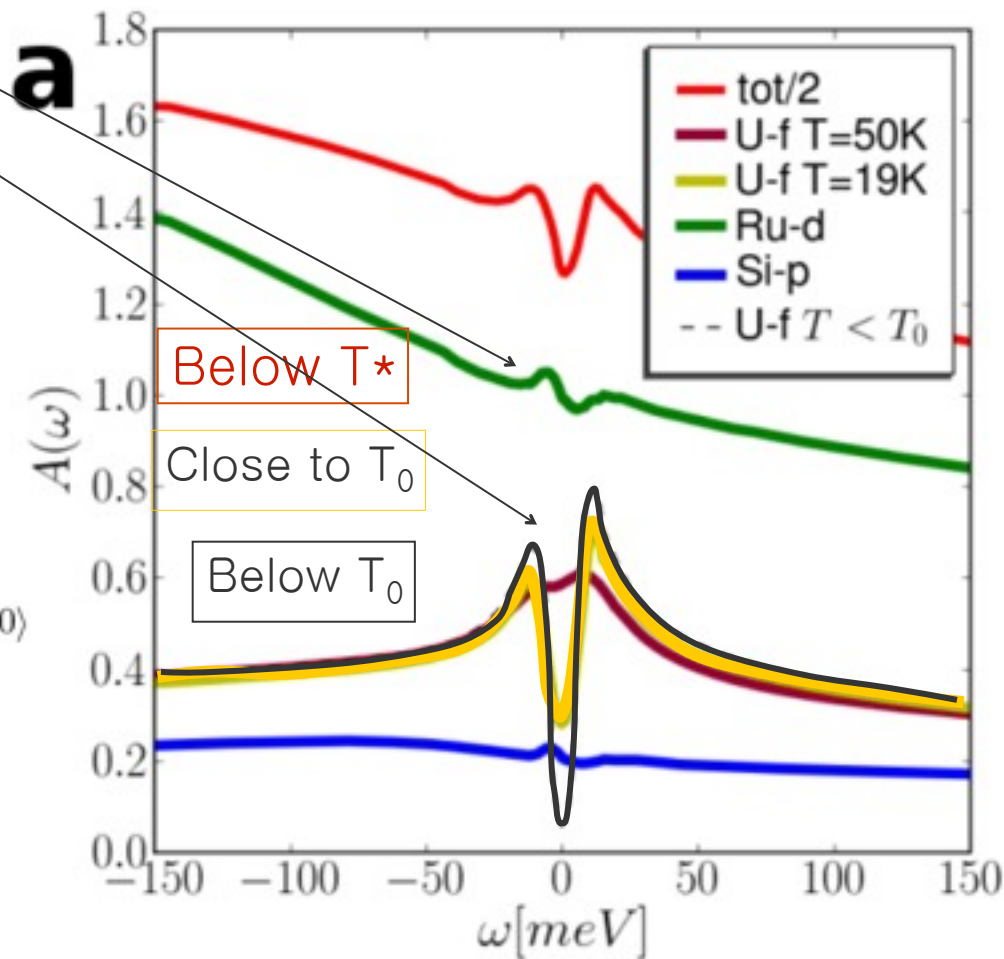
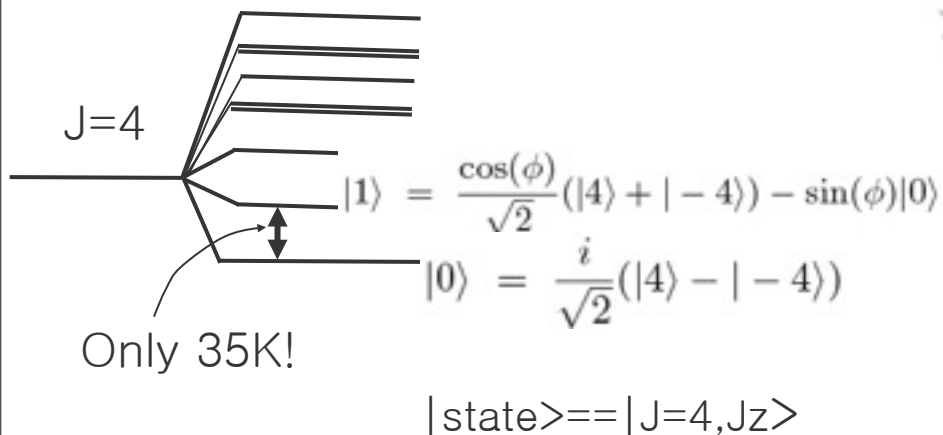
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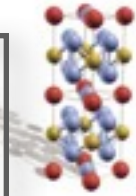
Partial DOS

Small effects on spd electrons  
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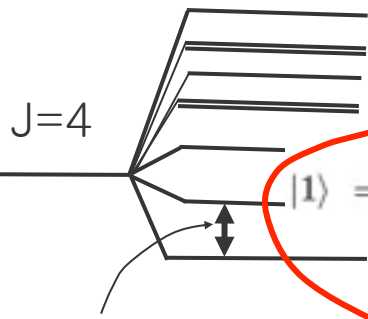
# Origin of gapping?



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Small effects on spd electrons  
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Ground state atomic multiplet of  $f^2$   
configuration in tetragonal field

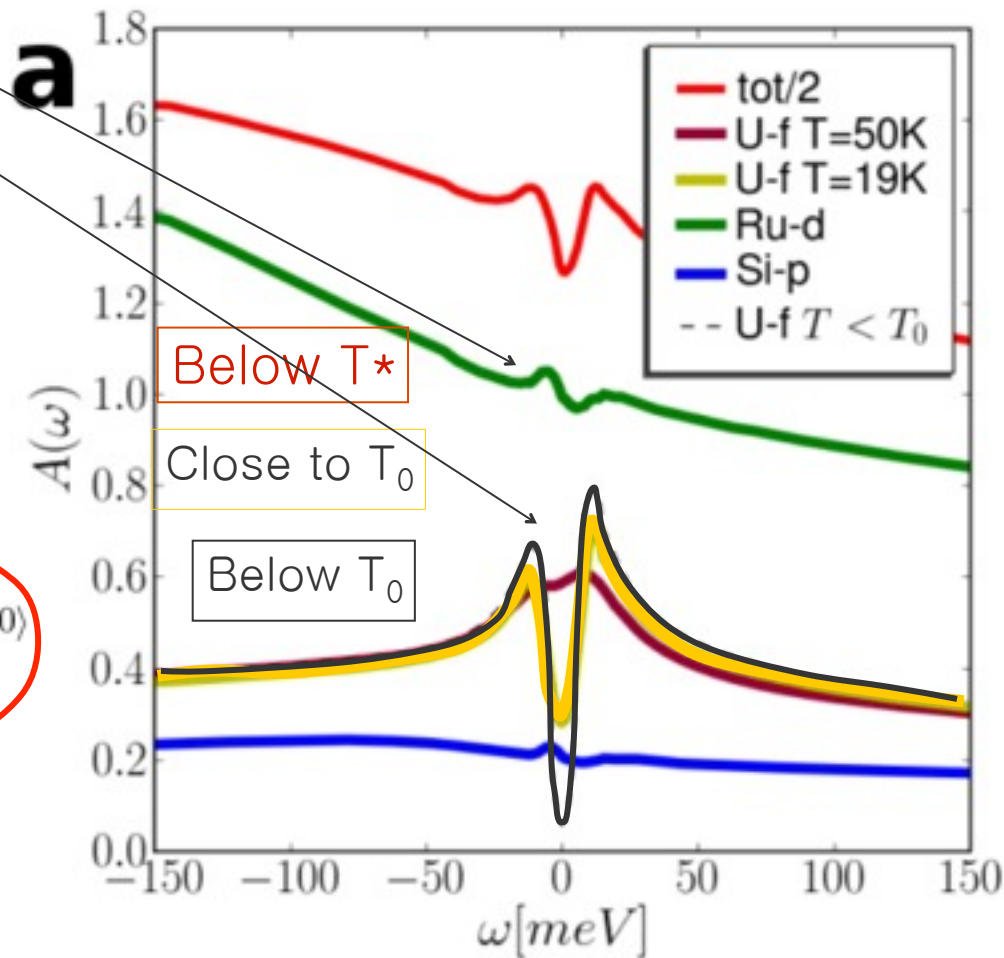


Only 35K!

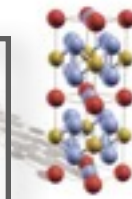
$$|1\rangle = \frac{\cos(\phi)}{\sqrt{2}}(|4\rangle + |-4\rangle) - \sin(\phi)|0\rangle$$

$$|0\rangle = \frac{i}{\sqrt{2}}(|4\rangle - |-4\rangle)$$

$$|\text{state}\rangle = |J=4, J_z\rangle$$

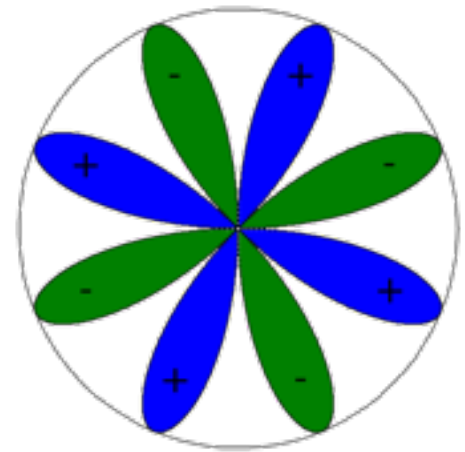


# DMFT order parameter



$$|0\rangle = \frac{i}{\sqrt{2}}(|4\rangle - |-4\rangle)$$

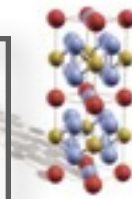
$$|1\rangle = \frac{\cos(\phi)}{\sqrt{2}}(|4\rangle + |-4\rangle) - \sin(\phi)|0\rangle$$



Order parameter:

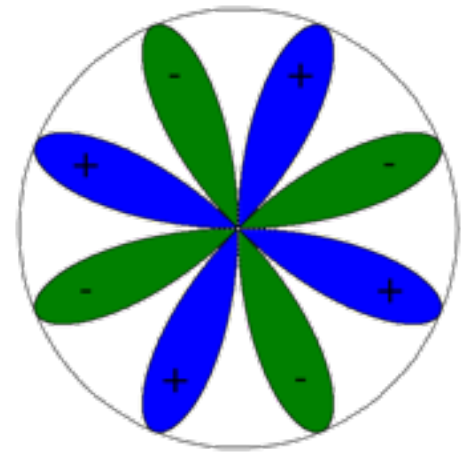
$$\psi_i = \langle X_{01}(\mathbf{R}_i) \rangle \begin{cases} \rightarrow \text{Im}\psi \propto \langle J_z \rangle \\ \rightarrow \text{Re}\psi \propto \langle (J_x J_y + J_y J_x)(J_x^2 - J_y^2) \rangle \end{cases}$$

# DMFT order parameter



$$|0\rangle = \frac{i}{\sqrt{2}}(|4\rangle - |-4\rangle)$$

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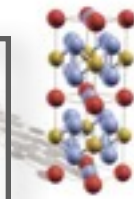


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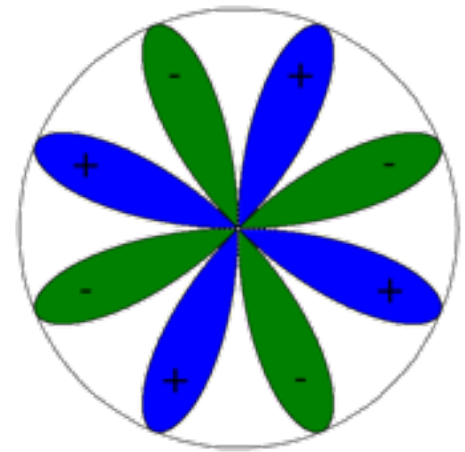
Different orientation gives different phases: adiabatic continuity explained!

# DMFT order parameter



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$$|1\rangle = \frac{\cos(\phi)}{\sqrt{2}}(|4\rangle + |-4\rangle) - \sin(\phi)|0\rangle$$



Order parameter:

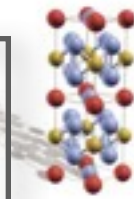
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Different orientation gives different phases: adiabatic continuity explained!

Does not break the time reversal, nor C4 symmetry. It breaks inversion symmetry.

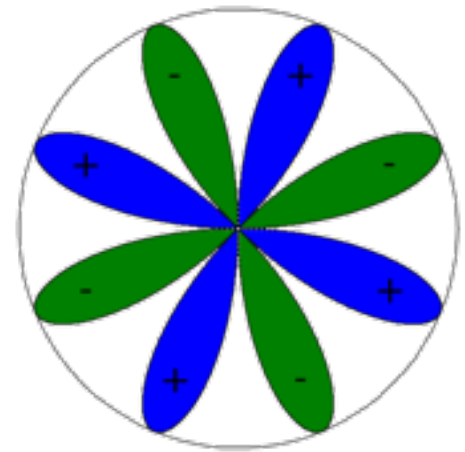


# DMFT order parameter



$$|0\rangle = \frac{i}{\sqrt{2}}(|4\rangle - |-4\rangle)$$

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Order parameter:

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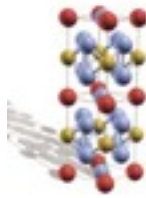
In the atomic limit:

$$|gs\rangle = \cos(\theta)|0\rangle + \sin(\theta)e^{i\varphi}|1\rangle$$

$$\langle gs|\mathbf{J}|gs\rangle = 4\cos(\phi)\sin(2\theta)\sin(\varphi)*(0, 0, 1)$$

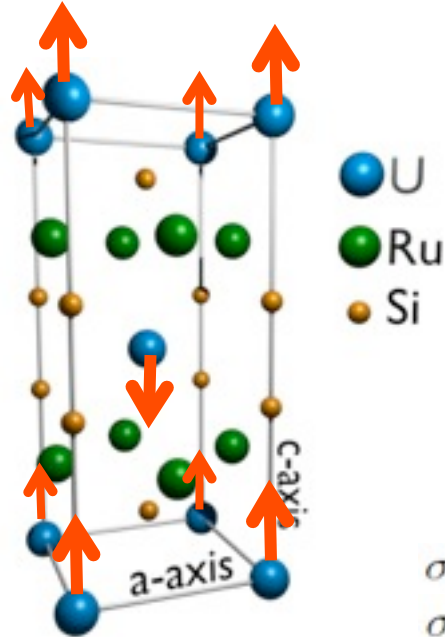
Moment only in z-direction!

# The two broken symmetry states



$$\text{Im}\psi \propto \langle J_z \rangle$$

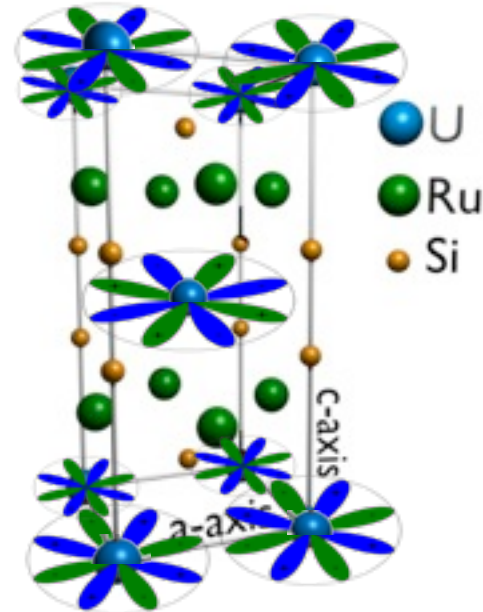
$$\text{Re}\psi \propto \langle (J_x J_y + J_y J_x)(J_x^2 - J_y^2) \rangle$$



A toy model

$$\begin{aligned}\sigma_3 &= |\emptyset\rangle\langle\emptyset| - |1\rangle\langle 1| \\ \sigma_1 &= |\emptyset\rangle\langle 1| + |1\rangle\langle\emptyset| \\ \sigma_2 &= i(|1\rangle\langle\emptyset| - |\emptyset\rangle\langle 1|)\end{aligned}$$

Magnetic moment:  
y-direction



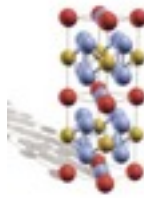
Hexadecapole:  
x-direction

crystal field: z direction

XY-Ising

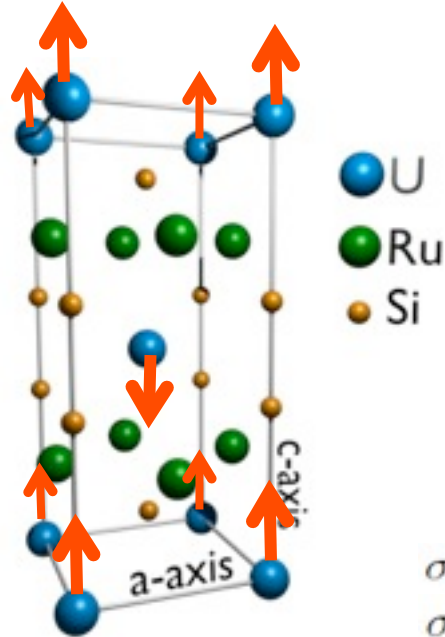
$$H = \sum_i -\frac{\Delta}{2}\sigma_3^i - \frac{1}{2}g\mu_B B|\langle 1|J_z|\emptyset\rangle|\sigma_2^i + \sum_{i,j} \frac{1}{2}(J_{ij}^1\sigma_1^i\sigma_1^j + J_{ij}^2\sigma_2^i\sigma_2^j)$$

# The two broken symmetry states



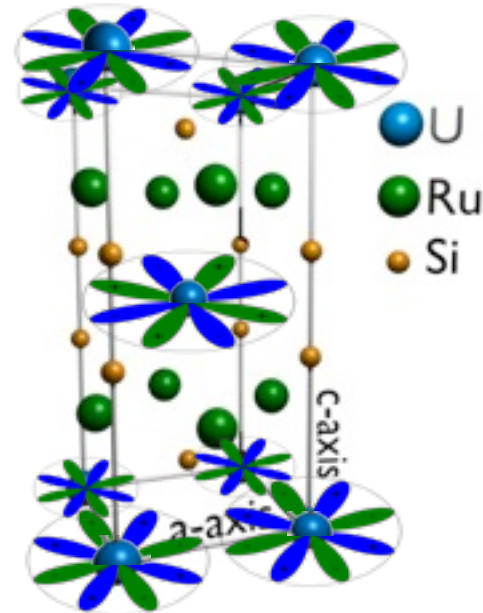
$$\text{Im}\psi \propto \langle J_z \rangle$$

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Magnetic moment:  
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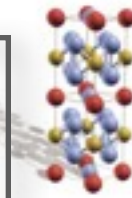
crystal field: z direction

Hexadecapole:  
x-direction

XY-Ising

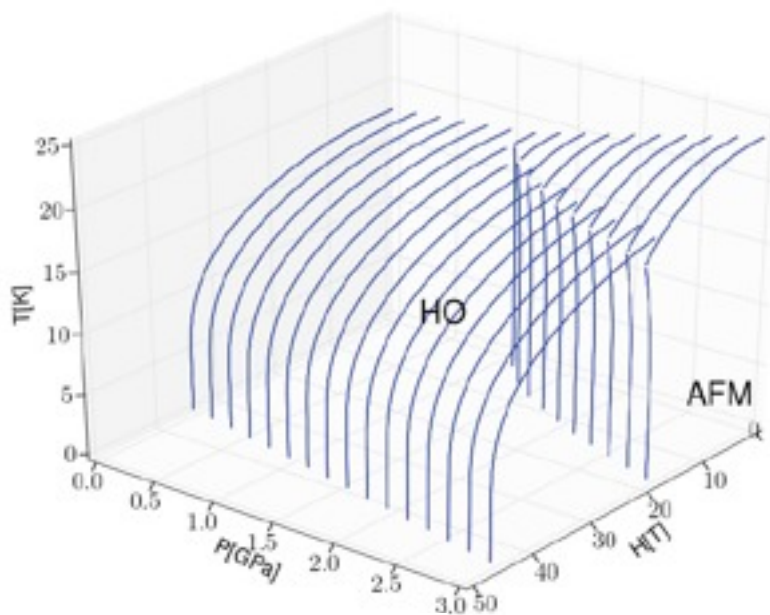
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# HO&AFM in magnetic field

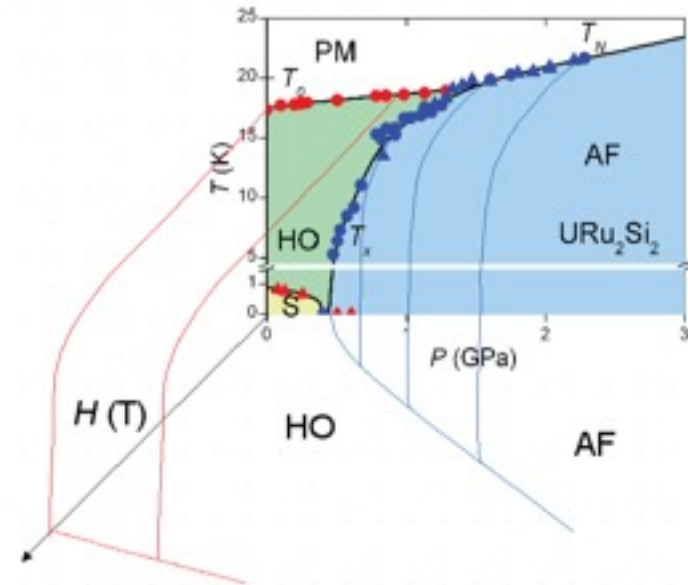


KH & G.Kotliar, arxiv: arXiv:0907.3892

$$F[h, \psi] = \frac{1}{2} \sum_{ij, \alpha=(1,2)} J_{ij}^{\alpha} \psi_i^{\alpha} \psi_j^{\alpha} - \sum_{i, \alpha=(1,2)} (h_i^{\alpha} + b^{\alpha}) \psi_i^{\alpha} - T \sum_i \log \left( \cosh \left( \beta \sqrt{(\Delta/2)^2 + (h_i^1)^2/2 + (h_i^2)^2/2} \right) \right)$$



Mean field



Exp. by E. Hassinger et.al. PRL 77, 115117 (2008)

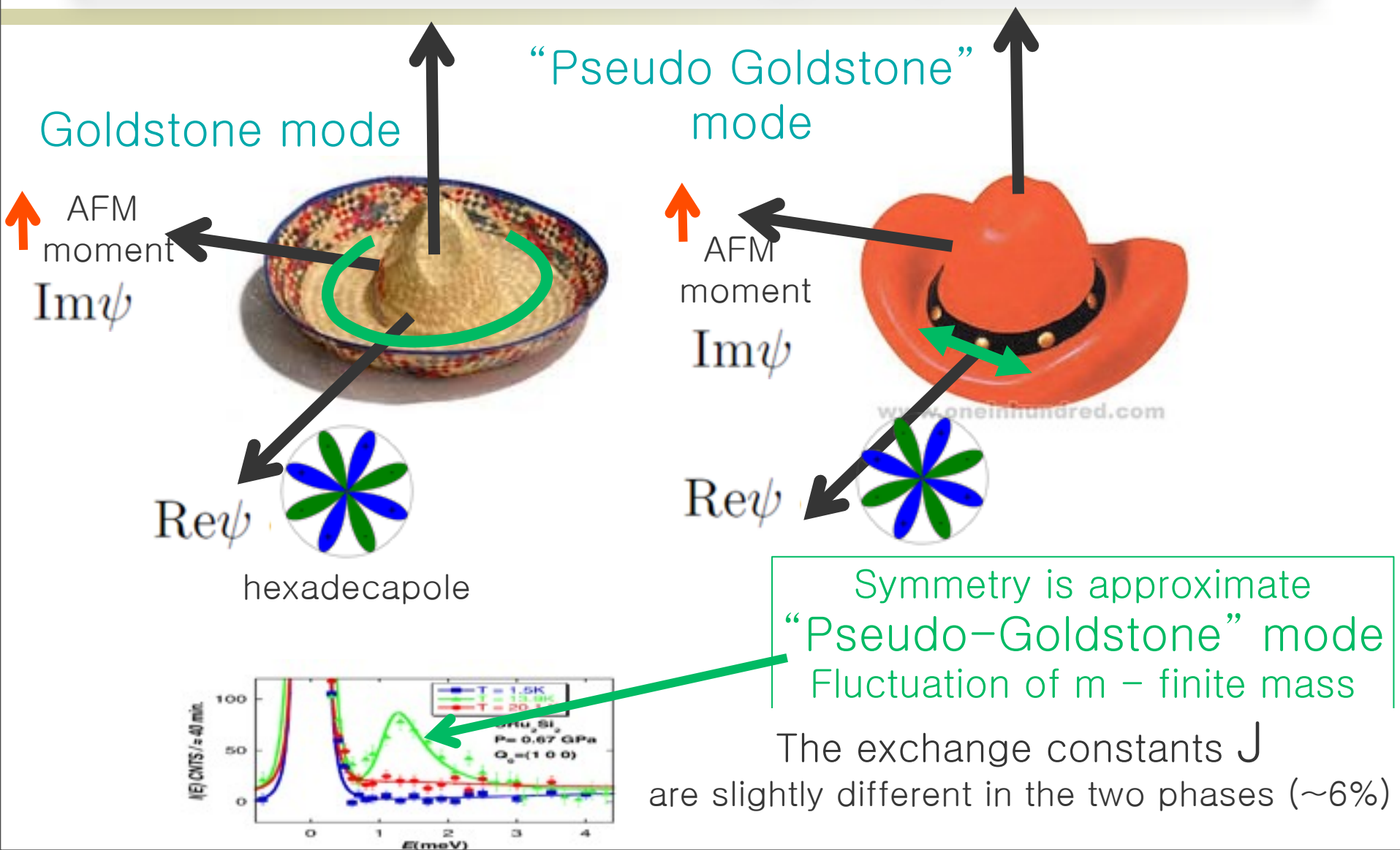
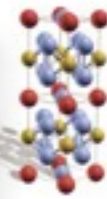
Only two fitting parameters:  $J_{\text{eff}}^1$ ,  $J_{\text{eff}}^2$   $J_{\text{eff}}^1 = \frac{\Delta}{\tanh(\Delta/(2T_0))}$

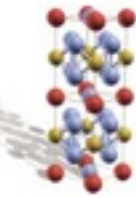
$$J_{\text{eff}} = 4|J_1| + 8J_2$$

determined by exp. transition temperature:  $J_{\text{eff}}^2 = \frac{\Delta}{\tanh(\Delta/(2T_N))}$



# Neutron scattering experiments



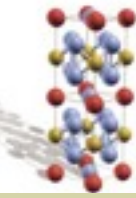


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THANKS!