





dmft1

$$\Sigma(\omega), \varepsilon_{\mathbf{k},i}^{DFT}, \psi_{\mathbf{k},i}^{DFT} \longrightarrow G_{local}, \Delta(\omega), E_{imp}$$

projector: $P(\mathbf{r}\mathbf{r}', \tau LL') \approx Y_L(\hat{\mathbf{r}}_\tau) \delta(r_\tau - r'_\tau) Y_{L'}^*(\hat{\mathbf{r}}'_\tau)$

self-energy in KS base: $\bar{\Sigma}_{\mathbf{k},ij}(\omega) = \sum_{\tau, L_1 L_2} P_{\mathbf{k}\tau}(ji, \tau L_2 L_1) (\Sigma_{L_1 L_2}^\tau(\omega) - E_{dc}^\tau)$

DMFT self-consistency condition:

$$G_{local}^\tau_{LL'} = \sum_{\mathbf{k}ij} P_{\mathbf{k}\tau}(ij, LL') \left[(i\omega + \mu - \epsilon_{\mathbf{k}} - \bar{\Sigma}_{\mathbf{k}}(\omega))^{-1} \right]_{ji}$$

$$= \left[\frac{1}{i\omega - E_{imp}^\tau - \Sigma^\tau(\omega) - \Delta^\tau(\omega)} \right]_{LL'}$$

dmft2

$$\Sigma(\omega), \epsilon_{\mathbf{k},i}^{DFT}, \psi_{\mathbf{k},i}^{DFT} \rightarrow \rho_{val}^{DMFT}(\mathbf{r}), E_{valence}$$

projector: $P(\mathbf{r}\mathbf{r}', \tau L L') \approx Y_L(\hat{\mathbf{r}}_\tau) \delta(r_\tau - r'_\tau) Y_{L'}^*(\hat{\mathbf{r}}'_\tau)$

self-energy in KS base: $\bar{\Sigma}_{\mathbf{k},ij}(\omega) = \sum_{\tau, L_1 L_2} P_{\mathbf{k}\tau}(ji, \tau L_2 L_1) (\Sigma_{L_1 L_2}^\tau(\omega) - E_{dc}^\tau)$

DMFT eigenvalues: $(-\nabla^2 + V_{KS}(\mathbf{r}) + \bar{\Sigma}_{\mathbf{k}}(\omega)) \psi_{\mathbf{k}\omega_n i}(\mathbf{r}) = \epsilon_{\mathbf{k}\omega_n i}^{DMFT} \psi_{\mathbf{k}\omega_n i}(\mathbf{r})$

The chemical potential: $N_{val} = T \sum_{\omega_n, i} \frac{1}{i\omega_n + \mu - \epsilon_{\mathbf{k}\omega_n i}}$

Valence charge density:

$$\rho_{val}^{DMFT} = \sum_{\mathbf{k}, ij} \psi_{\mathbf{k}i}^{DFT}(\mathbf{r}) \times T \sum_{\omega_n} \left[(i\omega_n + \mu - \epsilon_{\mathbf{k}} - \bar{\Sigma}_{\mathbf{k}}(\omega))^{-1} \right]_{ij} \times \psi_{\mathbf{k}j}^{DFT}(\mathbf{r})$$

total energy contribution: $E_{valence} = \text{Tr}((-\nabla^2 + V_{KS}) \rho_{val}^{DMFT})$

$$\Phi_{GW}(G, W) =$$

Diagram illustrating the GW approximation. It shows a self-energy loop on a Green's function $G(\mathbf{r}\mathbf{r}')$. The loop consists of a dashed line representing the Coulomb interaction V_C and a solid line representing the screened interaction $W(\mathbf{r}\mathbf{r}')$. The Green's function $G(\mathbf{r}\mathbf{r}')$ is shown as a circle with an arrow.

$$\Phi_{DMFT}(G, W) =$$

Diagram illustrating the DMFT approximation. It shows a self-energy loop on a local Green's function G_{loc} . The loop consists of a dashed line representing the interaction \mathcal{U} and a solid line representing the screened interaction W_{loc} . The diagram is followed by a plus sign and an ellipsis, indicating further terms in the expansion.

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